

Approaches to Quantum Gravity – a brief survey

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Why Quantum Gravity?

- Singularities in General Relativity (GR)
 - Black holes: gravitational collapse generically unavoidable
 - Singularity theorems: space and time ‘end’ at the singularity
 - Cosmological (“big bang”) singularity: what ‘happened’ at $t = 0$?
 - Structure of space-time at the smallest distances?

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 - Can be removed by infinite renormalizations order by order
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 - Therefore must look for an UV completion of the theory!
- Difficulties probably have common origin:
 - Space-time as a continuum (differentiable manifold)
 - Elementary Particles as exactly *pointlike* excitations
- Expect *something* to happen at $\ell_{Planck} \sim 10^{-33}cm$!

Different Attitudes

- Hypothesis 1:

Quantum Gravity essentially *is* the (non-perturbative) quantization of Einstein Gravity (in metric/connection/loop or discrete formalism). Thus GR, suitably treated and eventually complemented by the Standard Model of Particle Physics or its possible extensions, correctly describes the physical degrees of freedom also at the very smallest distances.

- Hypothesis 2:

GR is an effective (low energy) theory arising at large distances from a more fundamental Planck scale theory whose basic degrees of freedom are very different from either GR or QFT, and as yet unknown. GR, and with it, space-time itself as well as general covariance, are thus assumed to be ‘emergent’, much like macroscopic physics ‘emerges’ from the quantum world of atoms and molecules.

A Basic Fact

Perturbative quantum gravity is **non-renormalizable**

$$\Gamma_{div}^{(2)} = \frac{1}{\varepsilon} \frac{209}{2880} \frac{1}{(16\pi^2)^2} \int dV C_{\mu\nu\rho\sigma} C^{\rho\sigma\lambda\tau} C_{\lambda\tau}{}^{\mu\nu}$$

[Goroff& Sagnotti(1985); van de Ven(1992)]

Two possible conclusions:

- Consistent quantization of gravity requires a radical modification of Einstein's theory at short distances, in particular inclusion of supersymmetric matter; or
- UV divergences are artefacts of perturbative treatment \Rightarrow disappear upon a proper *non-perturbative* quantization of Einstein's theory.

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No approach to quantum gravity can claim complete success that does not explain *in detail* the ultimate fate of this divergence and other divergences!

Gravity and Matter [\rightarrow Hermann Weyl (1918)]

Einstein's equations according to Einstein:

$$\underbrace{R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R}_{\text{Marble}} = \underbrace{\kappa T_{\mu\nu}}_{\text{Timber?}}$$

Question: can we understand the r.h.s. geometrically?

- *Kaluza-Klein theories?*
- *Supersymmetry and Supergravity?*

Gravity vs. quantum mechanics: do we need to change the rules of quantum mechanics?

- *Black hole evaporation and information loss?*
- *Emergent space and time vs. quantum non-locality?*

Scales and Hierarchies

Gravitational force is much weaker than matter interactions \Rightarrow the ‘Hierarchy Problem’.

This fact is reflected in the relevant mass scales

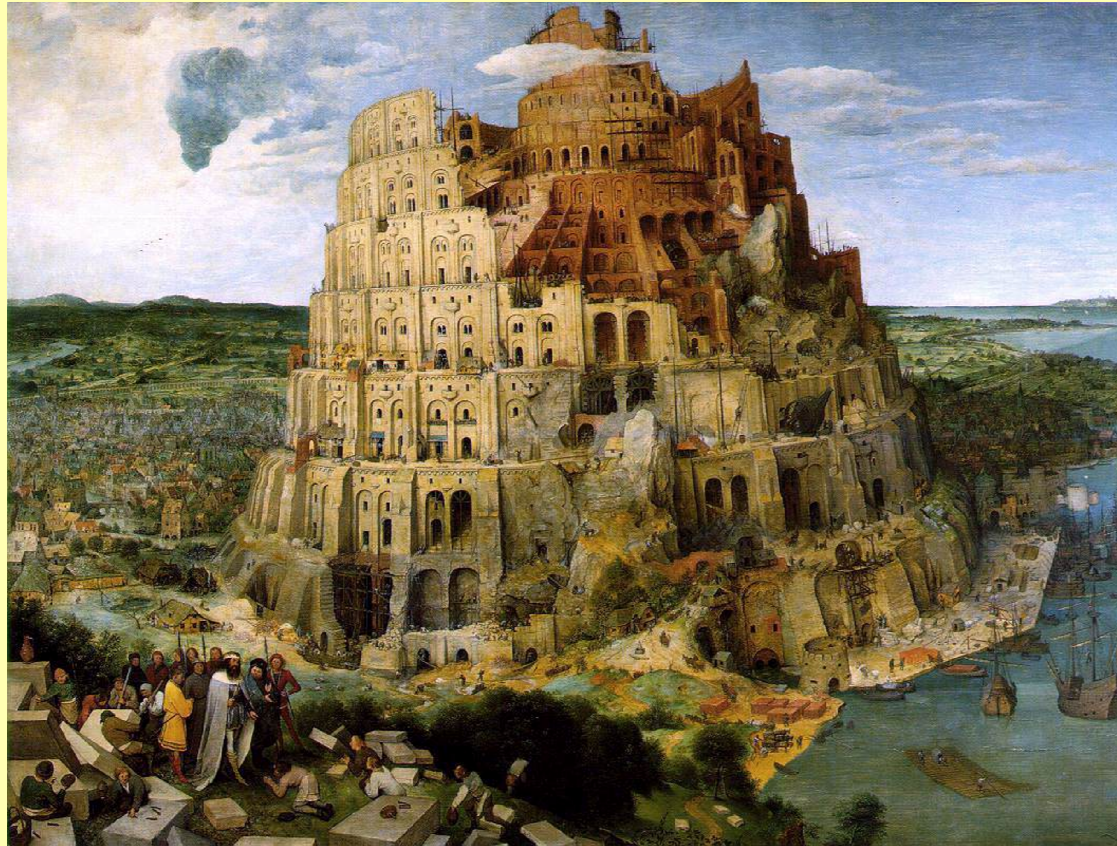
- Known elementary particles cover a large mass range:
 - Light neutrinos ~ 0.01 eV , electron ~ 0.5 MeV
 - Light quarks ~ 1 MeV , top quark ~ 173 GeV
 - Electroweak scale $\sim m_Z \sim 90$ GeV
- ... but still tiny *vis-à-vis* Planck Scale $M_{Pl} \sim 10^{19}$ GeV !

A key challenge for any proposed theory of Quantum Gravity: offer *quantifiable criteria to confirm or falsify the theory*. These must in particular allow to discriminate the given proposal against alternative ones!

Approaches to Quantum Gravity

- Supergravity, Superstrings and M Theory
- AdS/CFT and Holography
- Path integrals: Euclidean, Lorentzian, matrix models,...
- Canonical Quantization (metric formalism)
- Loop Quantum Gravity
- Discrete Quantum Gravity: Regge calculus, (C)DT
- Discrete Quantum Gravity: spin foams, group field theory,...
- Non-commutative geometry and non-commutative space-time
- Asymptotic Safety and RG Fixed Points
- Causal Sets, emergent (Quantum) Gravity
- Cellular Automata ('computing quantum space-time')

The steady progress of Quantum Gravity?



Asymptotic Safety: is standard QFT enough?

[Weinberg(1979), Reuter (1995), Percacci(2006), Niedermaier(2007), Reuter&Saueressig(2012)]

Approach is closest in spirit to conventional QFT ideas (RG flow, RG group, etc.), **but does not require anything special to happen to continuum space-time below ℓ_{Pl} !** More specifically:

- Is the UV limit of gravity determined by a **non-Gaussian fixed point (NGFP)** of the **gravitational renormalisation group (RG) flow** which controls the behaviour of theory at high energies and renders it safe from unphysical divergences?
- Aim: construct **scale dependent effective action Γ_k**

$$\lim_{k \rightarrow \infty} \Gamma_k = \text{bare action} \quad , \quad \lim_{k \rightarrow 0} \Gamma_k = \text{effective low energy action}$$

\Rightarrow approach is essentially *agnostic about microscopic theory*, all the information is in *universality classes* of RG flows.

- M_{Planck} analogous to Λ_{QCD} : *lower end* of asymptotic scaling regime \Rightarrow observable effects only if some prediction can be made about IR limit as theory flows down from NGFP.

Canonical Quantum Gravity

Non-perturbative and background independent approach:
quantum metric fluctuations and quantum geometry.

- Hamiltonian approach: manifest space-time covariance is lost through split (‘foliation’) of space-time as $\mathcal{M} = \Sigma \times \mathbb{R}$.
- \rightarrow Space-time geometry is viewed as the *evolution of spatial geometry in time* according to Einstein’s equations.
- **Geometrodynamics**: canonical *dynamical* degrees of freedom

$$g_{mn}(t, \mathbf{x}) \quad \text{and} \quad \Pi^{mn}(t, \mathbf{x}) = \frac{\delta \mathcal{S}_{\text{Einstein}}}{\delta \dot{g}_{mn}(t, \mathbf{x})}$$

- Dynamics defined by *constraints* (via shift and lapse): **Hamiltonian constraint** $\mathcal{H}(\mathbf{x})$ and **diffeomorphism constraints** $\mathcal{D}_m(\mathbf{x})$
- **Quantum Constraint Algebra** from classical Poisson algebra:

$$\{\mathcal{D}, \mathcal{D}\} \sim \mathcal{D} \quad \{\mathcal{D}, \mathcal{H}\} \sim \mathcal{H} \quad \{\mathcal{H}, \mathcal{H}\} \sim \mathcal{D} \ ,$$

possibly modulo anomalies (cf. Witt vs. Virasoro algebra).

\Rightarrow **Quantum space-time covariance must be proven!**

New Variables, New Perspectives?

- New canonical variables: replace g_{mn} by connection

$$A_m^a = -\frac{1}{2}\epsilon^{abc}\omega_{m bc} + \gamma K_m^a$$

[$\omega_{m bc}$ = spatial spin connection, K_m^a = extrinsic curvature]

- New canonical brackets [Ashtekar (1986)]

$$\begin{aligned}\{A_m^a(\mathbf{x}), E_b^n(\mathbf{y})\} &= \gamma \delta_b^a \delta_m^n \delta^{(3)}(\mathbf{x}, \mathbf{y}) , \\ \{A_m^a(\mathbf{x}), A_n^b(\mathbf{y})\} &= \{E_a^m(\mathbf{x}), E_b^n(\mathbf{y})\} = 0\end{aligned}$$

with conjugate variable E_a^m = inverse densitized dreibein

\Rightarrow for $\gamma = \pm i$ constraints become polynomial

$$E_a^n F_{mn}^a(A) \approx 0 , \quad \epsilon^{abc} E_a^m E_b^n F_{mnc}(A) \approx 0 , \quad D_m(A) E_a^m \approx 0$$

with $SU(2)$ field strength $F_{mna} \equiv \partial_m A_{na} - \partial_n A_{ma} + \varepsilon_{abc} A_m^b A_n^c$.

- But reality constraint difficult to elevate to quantum theory
 $\rightarrow \gamma$ is nowadays taken real ('Barbero-Immirzi parameter')

Loop Quantum Gravity (LQG)

- Modern canonical variables: **holonomy** (along edge e)

$$h_e[A] = \mathcal{P} \exp \int_e A$$

- Conjugate variable = **flux** through area element S

$$F_S^a[E] := \int_S dF^a = \int_S \epsilon_{mnp} E_a^m dx^n \wedge dx^p$$

- act on wave functionals $\Psi_{\{\Gamma, C\}}[A] = f_C(h_{e_1}[A], \dots, h_{e_n}[A])$ with **spin network** Γ (graph consisting of *edges* e and *vertices* v).
- **New feature:** Kinematical Hilbert space \mathcal{H}_{kin} can be defined, but is *non-separable* \Rightarrow operators not weakly continuous.
Cf. ordinary quantum mechanics: replace $\langle x|x' \rangle = \delta(x - x')$ by $\langle x|x' \rangle = 1$ if $x = x'$ and $= 0$ if $x \neq x' \rightarrow$ ‘pulverize’ real line!
- \Rightarrow No UV divergences (and thus no anomalies)?
- \Rightarrow No negative norm states? [cf. Narnhofer&Thirring (1992)]

Status of Hamiltonian constraint

- Diffeomorphism constraint solved formally: $\mathcal{X}_\Gamma = \sum_{\phi \in \text{Diff}} \Psi_{\Gamma \circ \phi}$
- \Rightarrow Hamiltonian constraint not defined on \mathcal{H}_{kin} , but on distribution space \mathcal{S} ('habitat') = dual of dense subspace $\subset \mathcal{H}_{kin}$.
- **Main success:** definition of regulated Hamiltonian (with $\epsilon > 0$) by means of kinematical operators (volume, etc.) [Thiemann(2000)]

$$\begin{aligned} \hat{H}[N, \epsilon] = & \sum_{\alpha} N(v_{\alpha}) \epsilon^{mnp} \text{Tr} \left((h_{\partial P_{mn}(\epsilon)} - h_{\partial P_{mn}(\epsilon)}^{-1}) h_p^{-1} [h_p, V] \right) \\ & + \frac{1}{2} (1 + \gamma^2) \sum_{\alpha} N(v_{\alpha}) \epsilon^{mnp} \text{Tr} \left(h_m^{-1} [h_m, \bar{K}] h_n^{-1} [h_n, \bar{K}] h_p^{-1} [h_p, V] \right) \end{aligned}$$

- Proper definition relies on diffeomorphism invariance of states $\mathcal{X} \in \mathcal{S} \Rightarrow$ limit $\epsilon \rightarrow 0$ exists (at best) as a *weak limit*:

$$\langle H^*[N] \mathcal{X} | \Psi \rangle = \lim_{\epsilon \rightarrow 0} \langle \mathcal{X} | \hat{H}[N, \epsilon] \Psi \rangle, \quad \mathcal{X} \in \mathcal{S}$$

- *Ultralocal* action of unregulated Hamiltonian adds 'spider-webs' (of size $\epsilon \rightarrow 0$) to spin network Γ , but cumbersome to evaluate (on \mathcal{S}) even for the simplest examples.

Summary and Critique

Non-perturbative approaches (LQG, spin foams,...) put main emphasis on general concepts underlying GR:

- (Spatial) Background Independence
- Diffeomorphism Invariance

However, these approaches so far do not incorporate essential insights and successes of standard QFT:

- Consistency restrictions from anomalies?
- Quantization ambiguities?
- Matter couplings: anything goes?

These issues will be hard to settle without a detailed understanding of how standard QFT and the semi-classical limit (Einstein equations, *etc.*) emerge.

The Superworld

Basic strategy: render gravity perturbatively consistent (i.e. finite) by modifying GR at short distances.

- Supersymmetry: matter (fermions) *vs.* forces (bosons)
- (Partial) cancellation of UV infinities
- The *raison d'être* for matter to exist?
- Maximally symmetric point field theories
 - $D = 4, N = 8$ Supergravity
 - $D = 11$ Supergravity
- Supersymmetric extended objects
 - No point-like interactions \Rightarrow no UV singularities?
 - IIA/IIB und heterotic superstrings ($D = 10$)
 - Supermembranes and M(atrix)-Theory ($D = 11$)

String Theory

Cf. Costas Bachas' talk

Very much modelled on concepts from particle physics
(hence no problem with semi-classical limit):

- Not simply a theory of one-dimensional extended objects: D-branes, M-branes, ...
 - Microscopic BH Entropy: $S = \frac{1}{4}A$ (+ corrections)
 - Holography: the key to quantum gravity?
 - New ideas for physics beyond the Standard Model:
 - Low energy supersymmetry and the MSSM
 - Large extra dimensions and brane worlds (but $D = 4??$)
 - Multiverses and the string landscape
- a new El Dorado for experimentalists?

String Theory: open questions

- Struggling to reproduce SM *as is*
- Struggling to incorporate $\Lambda > 0$
- Perturbative finiteness: obvious, but unprovable?
- Role of maximally extended $N = 8$ supergravity?

Recent advances transcend perturbation theory, but

- No convincing scenario for resolution of space-time singularities in GR (e.g. via AdS/CFT ?)
- Or: what ‘happens’ to space and time at ℓ_{PL} ?
- The real question: **what *is* string theory?**

A Key Issue: Non-Uniqueness

Existing approaches suffer from a very large number of ambiguities, so far preventing any kind of prediction with which the theory will stand or fall:

- Superstrings: 10^{500} ‘consistent’ vacua and the multiverse?
- LQG: 10^{500} ‘consistent’ Hamiltonians/spin foam models?
- Discrete Gravity: 10^{500} ‘consistent’ lattice models?
- Asymptotic Safety: 10^{500} ‘consistent’ RG flows?

Question: does Nature pick the ‘right’ answer at random from a huge variety of possibilities, or are there criteria to narrow down the number of choices?

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In order to discriminate between a growing number of diverging ideas on quantum gravity better to start looking for *inconsistencies*...

... or else *ansätze* may remain ‘fantasy’ [G.W. Gibbons]!

Forward to the Past: $N = 8$ Supergravity?

Very recent work has shown that $N = 8$ supergravity

- is much more finite than expected (behaves like $N = 4$ super-Yang-Mills up to four loops)

[Bern,Carrasco,Dixon,Johansson, Roiban, PRL103(2009)081301]

- ... and could thus be finite to all orders!
- However: efforts towards five loops seem to be stuck.

In string theory as well there appear difficulties starting *at five loops*: super-moduli space is no longer ‘split’ [Grushevsky,Witten,...]

But even if $N=8$ Supergravity is finite:

- what about *non-perturbative* quantum gravity?
- is there any relation to *real physics*?

If no new spin- $\frac{1}{2}$ degrees of freedom are found at LHC, the following curious fact could also become relevant:

A strange coincidence?

$SO(8) \rightarrow SU(3) \times U(1)$ breaking and ‘family color locking’

$(u, c, t)_L :$	$\mathbf{3}_c \times \bar{\mathbf{3}}_f \rightarrow \mathbf{8} \oplus \mathbf{1} ,$	$Q = \frac{2}{3} - q$
$(\bar{u}, \bar{c}, \bar{t})_L :$	$\bar{\mathbf{3}}_c \times \mathbf{3}_f \rightarrow \mathbf{8} \oplus \mathbf{1} ,$	$Q = -\frac{2}{3} + q$
$(d, s, b)_L :$	$\mathbf{3}_c \times \mathbf{3}_f \rightarrow \mathbf{6} \oplus \bar{\mathbf{3}} ,$	$Q = -\frac{1}{3} + q$
$(\bar{d}, \bar{s}, \bar{b})_L :$	$\bar{\mathbf{3}}_c \times \bar{\mathbf{3}}_f \rightarrow \bar{\mathbf{6}} \oplus \mathbf{3} ,$	$Q = \frac{1}{3} - q$
$(e^-, \mu^-, \tau^-)_L :$	$\mathbf{1}_c \times \mathbf{3}_f \rightarrow \mathbf{3} ,$	$Q = -1 + q$
$(e^+, \mu^+, \tau^+)_L :$	$\mathbf{1}_c \times \bar{\mathbf{3}}_f \rightarrow \bar{\mathbf{3}} ,$	$Q = 1 - q$
$(\nu_e, \nu_\mu, \nu_\tau)_L :$	$\mathbf{1}_c \times \bar{\mathbf{3}}_f \rightarrow \bar{\mathbf{3}} ,$	$Q = -q$
$(\bar{\nu}_e, \bar{\nu}_\mu, \bar{\nu}_\tau)_L :$	$\mathbf{1}_c \times \mathbf{3}_f \rightarrow \mathbf{3} ,$	$Q = q$

Supergravity and Standard Model assignments agree
if spurion charge is chosen as $q = \frac{1}{6}$ [Gell-Mann (1983)]

Realized at $SU(3) \times U(1)$ stationary point! [Warner,HN: NPB259(1985)412]

Mismatch of $\pm \frac{1}{6}$ can be fixed by deforming $U(1)$ [Meissner,HN:1412.1715]

Yet more symmetries...

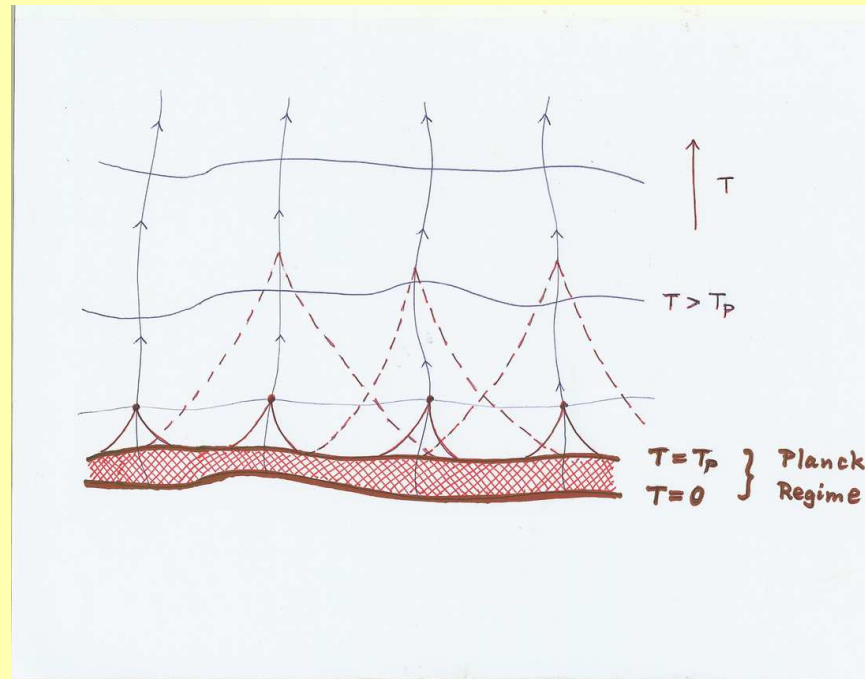
- $N = 8$ Supergravity possesses an unexpected (‘hidden’) duality symmetry: $E_{7(7)}$ [Cremmer, Julia, 1979]
- An unexpected link with the *exceptional groups* G_2, F_4, E_6, E_7, E_8 , the solitary members of the Lie group classification.
- ‘Dimensional reduction’ \equiv metamorphoses space-time symmetries into internal symmetries:

$$\cdots \subset E_6 \subset E_7 \subset E_8 \subset E_9 \subset E_{10}$$

with the ∞ -dimensional ‘prolongations’ E_9 and E_{10}

- E_{10} = maximally extended hyperbolic Kac–Moody Symmetry – a mathematical ENIGMA!
- \Rightarrow ‘De-Emergence’ of space (and time) !?!

Another hint: BKL and Spacelike Singularities



For $T \rightarrow 0$ spatial points decouple and the system is effectively described by a continuous *superposition of one-dimensional systems* \rightarrow **effective dimensional reduction to $D = 1$!** [Belinski, Khalatnikov, Lifshitz (1972)]

Habitat of Quantum Gravity?

- Cosmological evolution as **one-dimensional motion** in the moduli space of 3-geometries [Wheeler, DeWitt, ...]

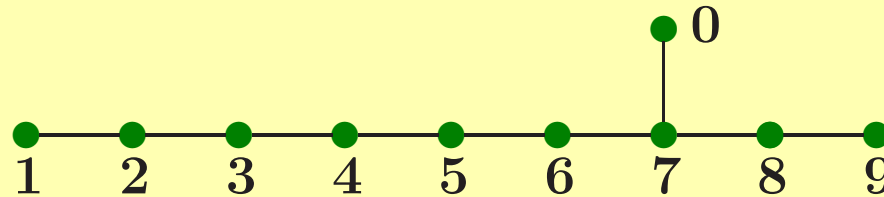
$$\mathcal{M} \equiv \mathcal{G}^{(3)} = \frac{\{\text{spatial metrics } g_{ij}(\mathbf{x})\}}{\{\text{spatial diffeomorphisms}\}}$$

- Formal canonical quantization leads to **WDW equation** (“Schrödinger equation of quantum gravity”)
- Unification of space-time, matter and gravitation: configuration space \mathcal{M} for quantum gravity should consistently incorporate matter degrees of freedom.
- Can we understand and ‘simplify’ \mathcal{M} by means of embedding into a group theoretical coset $G/K(G)$?
- Proposal: $G = E_{10}$ with involutory subgroup $K(E_{10})$.

[Damour, Henneaux, Kleinschmidt, HN (since 2002)]

A candidate symmetry: $G = E_{10}$?

E_{10} is the ‘group’ associated with the Kac-Moody Lie algebra $\mathfrak{g} \equiv \mathfrak{e}_{10}$ defined via the Dynkin diagram [e.g. Kac]



Defined by **generators** $\{e_i, f_i, h_i\}$ and **relations** via **Cartan matrix** A_{ij} (‘Chevalley-Serre presentation’)

$$\begin{aligned} [h_i, h_j] &= 0, & [e_i, f_j] &= \delta_{ij} h_i, \\ [h_i, e_j] &= A_{ij} e_j, & [h_i, f_j] &= -A_{ij} f_j, \\ (\text{ad } e_i)^{1-A_{ij}} e_j &= 0 & (\text{ad } f_i)^{1-A_{ij}} f_j &= 0. \end{aligned}$$

\mathfrak{e}_{10} is the free Lie algebra generated by $\{e_i, f_i, h_i\}$ modulo these relations \rightarrow infinite dimensional as A_{ij} is *indefinite* \rightarrow Lie algebra of *exponential growth* !

$SL(10)$ level decomposition of E_{10}

- Decomposition w.r.t. to $SL(10)$ subgroup in terms of $SL(10)$ tensors \rightarrow *level expansion*

$$\alpha = \ell\alpha_0 + \sum_{j=1}^9 m^j \alpha_j \quad \Rightarrow \quad E_{10} = \bigoplus_{\ell \in \mathbb{Z}} E_{10}^{(\ell)}$$

- Up to $\ell \leq 3$ basic fields of $D = 11$ SUGRA together with their magnetic duals (spatial components)

$\ell = 0$	G_{mn}	Graviton
$\ell = 1$	A_{mnp}	3-form
$\ell = 2$	$A_{m_1 \dots m_6}$	dual 6-form
$\ell = 3$	$h_{m_1 \dots m_8 n}$	dual graviton

- Analysis up to level $\ell \leq 28$ yields 4 400 752 653 representations (Young tableaux) of $SL(10)$ [Fischbacher, HN:0301017]
- Lie algebra structure (structure constants, etc.) understood only up to $\ell \leq 4$. **Also: no matter where you stop it will get even more complicated beyond!**

The $E_{10}/K(E_{10})$ σ -model

Basic Idea: map evolution according to $D = 11$ SUGRA equations of motion onto null geodesic motion of a point particle on $E_{10}/K(E_{10})$ coset manifold [DHN:0207267]

$$\mathcal{V}(t) = \exp \left(h_{ab}(t) S^{ab} + \frac{1}{3!} A_{abc}(t) E^{abc} + \frac{1}{6!} A_{abcdef}(t) E^{abcdef} + \dots \right)$$

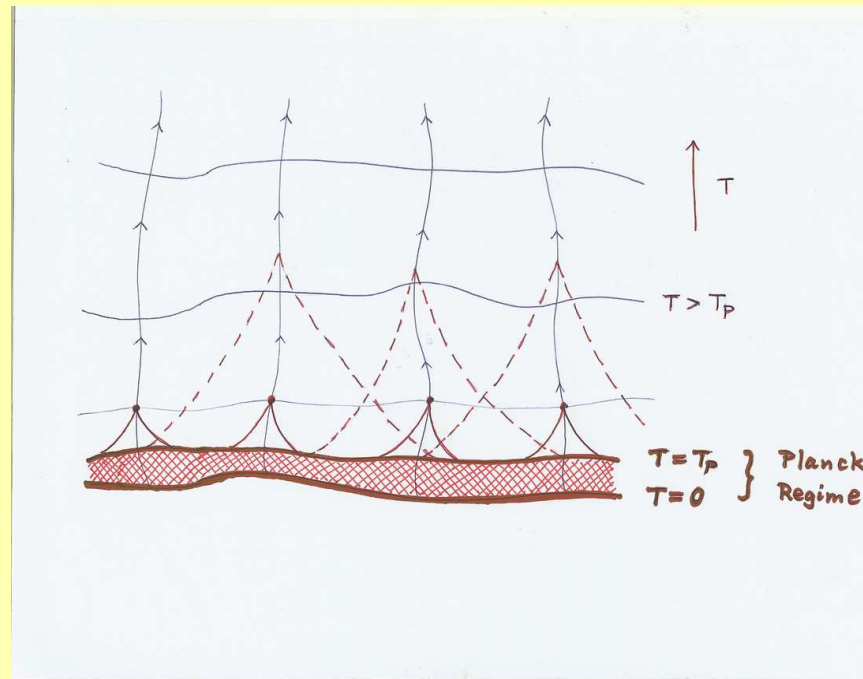
and then work out Cartan form $\mathcal{V}^{-1} \partial_t \mathcal{V} = Q + P \rightarrow \sigma$ -model dynamics up to $\ell \leq 3$ matches with supergravity equations of motion when truncated to first order spatial gradients.

Conjecture: information about spatial dependence gets ‘spread’ all over E_{10} Lie algebra \Leftrightarrow level expansion contains complete set of *gradient representations* for all $D = 11$ fields and their duals.

Last but not least: $U(1)_q$ deformation required to match quark and lepton charges with $N = 8$ supergravity belongs to $K(E_{10})$!

[Kleinschmidt,HN, arXiv:1504.01586]

E_{10} : The Basic Picture



Conjecture: for $0 < T < T_P$ space-time ‘de-emerges’, and space-time based (quantum) field theory is replaced by quantised ‘spinning’ $E_{10}/K(E_{10})$ σ -**model**.

[Damour,Henneaux,Kleinschmidt, HN: since 2002]

Outlook

- Incompleteness of the SM and GR are strongest arguments in favor of quantizing gravity.
- **Main Question:** how are short distance singularities resolved in **GR and QFT**, and how can this resolution be reconciled with classical Einstein equations in continuum space-time?
 - Dissolving pointlike interactions (strings, branes,...)
 - Cancellation of UV infinities (e.g. $N = 8$ supergravity)?
 - Fundamental discreteness (LQG, discrete gravity)?
 - Other mechanism (e.g. AS, non-commutative space-time)?
- Symmetry-based approach offers new perspectives: $N = 8$ supergravity and E_{10} are uniquely distinguished.
- ... but there is still a long way to go !