

The Galois Group of the Category of Mixed Hodge-Tate Structures

Tuesday, October 10, 2023 3:15 PM (1 hour)

This talk is based on the joint work with Guangyu Zhu.

The category of rational mixed Hodge-Tate structures is canonically equivalent to the category of finite-dimensional graded comodules over a graded commutative Hopf algebra H over \mathbb{Q} . The latter is the algebra of functions on the Galois group of the category.

Since the category has homological dimension 1, the Hopf algebra H is isomorphic to the commutative graded Hopf algebra given by the tensor algebra of the direct sum of over $n > 0$ of $C/Q(n)$, placed in the degree n , with the shuffle product.

However this isomorphism is not natural, e.g. does not work in families. We give a natural explicit construction of the Hopf algebra H .

Generalizing this, we define a Hopf dg-algebra, describing a dg-model of the derived category of variations of Hodge-Tate structures on a complex manifold X . Its cobar complex is a dg-model for the rational Deligne cohomology of X .

Here is an application. Periods of weight n variations of mixed Hodge-Tate structures are multivalued functions, e.g. the weight n polylogarithms. We define refined periods. They are single-valued, and take values in the tensor product of the multiplicative group of complex numbers and $n-1$ copies of the abelian group of complex numbers.

We also consider a p -adic variant of the construction which starts from Fontaine's crystalline / semi-stable period rings and produces graded / dg Hopf algebras, related to the p -adic Hodge theory.

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