

# Braid group action on the cohomology of Deligne-Lusztig varieties

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If  $B$  is the braid group associated with the Weyl group  $W$  of a split reductive group  $G$  over  $F_q$ , and if  $b$  is in  $B$ , we construct a categorical action of the centralizer  $C_B(b)$  on the cohomology of the Deligne-Lusztig variety  $X(b)$  associated with  $b$ . If  $b=1$ , we retrieve the classical algebraic action of the Hecke algebra on the permutation representation of the finite flag variety. As another particular case, we retrieve a geometric action defined by Broué-Michel in 1996.

In this talk, we explain the construction of this action, some of its properties (action of the Frobenius, compatibility with Deligne-Lusztig parabolic induction, ...) and we investigate natural questions (for instance, does the image of  $C_B(b)$  generate the endomorphism algebra?).

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