

# Intracellular transport of cargos: tug-of-war, anomalous diffusion, and lattice deformation

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# Collaboration

Univ. Paris-Sud



C. Appert-Rolland



Max  
Ebbinghaus



Sarah  
Klein

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Saarlandes



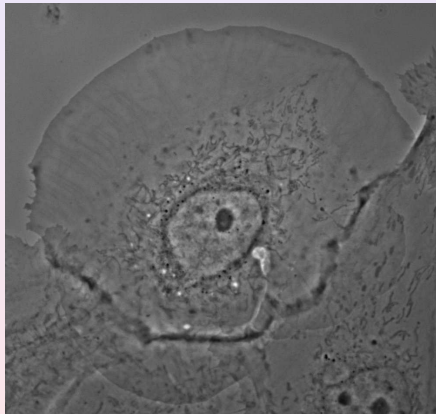
L. Santen

+ Inès Weber

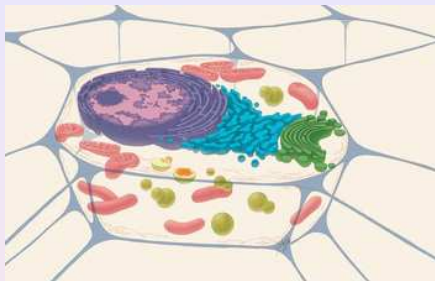
- Dynamics of cargo-motors complexes
  - Tug-of-war: Mean-Field model
  - Explicit Position Based model
  - Anomalous diffusion
  - External control
- Interplay between transport and lattice dynamics
  - Impact of lattice dynamics on collective cargo transport
  - Lattice deformation driven by active cross-linkers

# Intra-cellular transport

- Need for transport



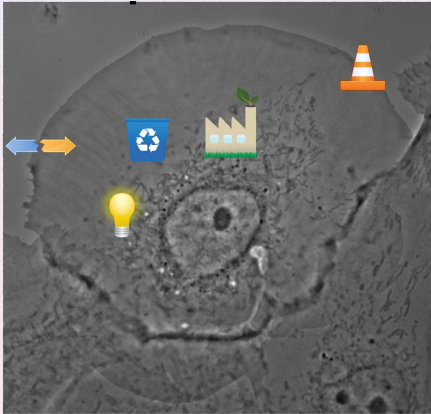
From [Wittmann et al, J. Cell Biol. 161:845 (2003)]



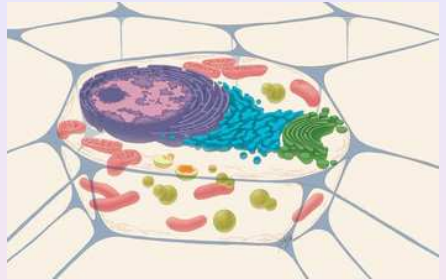
From [Judith Stoffer, NIGMS]

# Intra-cellular transport

- Need for transport



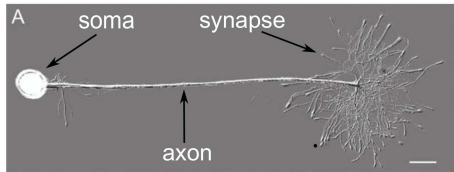
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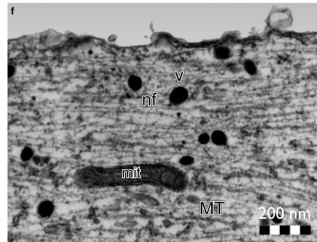
# Intra-cellular transport

Shemesh et al., *Traffic* **9**, 458 (2008)



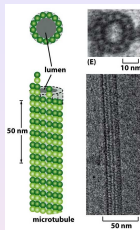
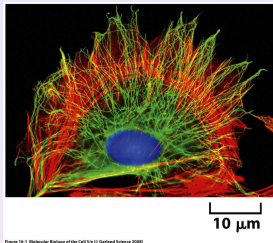
- Particular case: the axon
  - up to 1 m in human beings, a few microns for the diameter
  - crowded environment
- Link with neurodegenerative diseases

v: vesicle  
nf: neurofilament  
mit: mitochondrion  
MT: microtubule

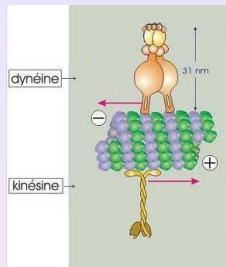


Shemesh & Spira, *Acta Neuropathol* **120**, 209 (2010)

# Intracellular transport

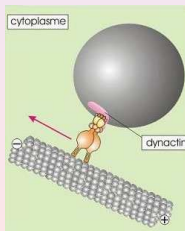


From [Alberts et al, *Molecular Biology of the Cell*, 5th ed. (2008)]

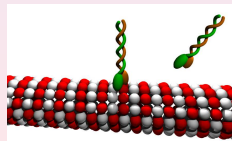


[Modified from  
[www.ulyse.u-bordeaux.fr/  
atelier/ikramer/  
biocell\\_diffusion](http://www.ulyse.u-bordeaux.fr/atelier/ikramer/biocell_diffusion)]

Microtubules are polarized



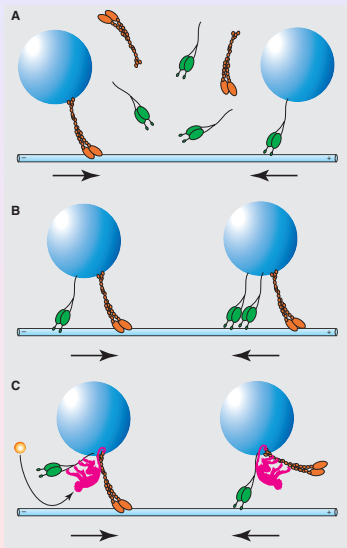
[From  
[www.ulyse.u-bordeaux.fr/atelier/ikramer/biocell\\_diffusion](http://www.ulyse.u-bordeaux.fr/atelier/ikramer/biocell_diffusion)]



[Modified from a wikipedia  
image by Kebes]

Motors can attach and detach

# Cargo-motor complexes



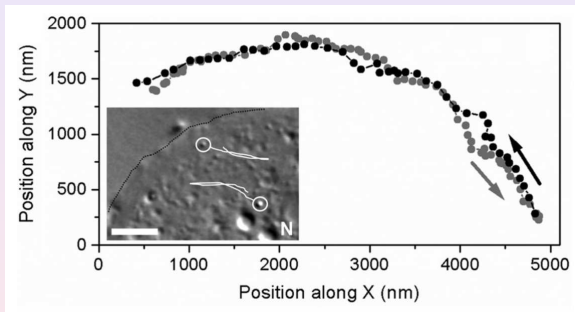
## Teams of motors

- Can apply stronger forces
- Increases processivity

[Welte (2004) Curr. Biol.]



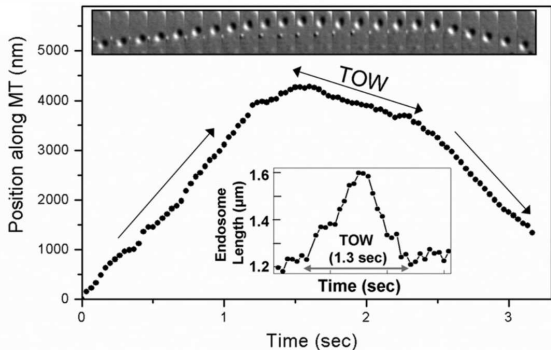
# Tug-of-war



Endosome inside  
Dictyostelium cells.

[Soppina et al (2009) PNAS]

# Tug-of-war

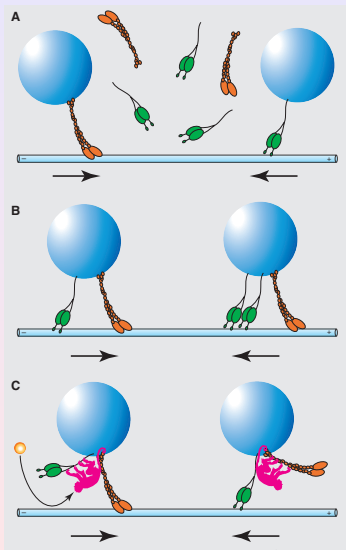


Endosome inside Dictyostelium cells.

[Soppina et al (2009) PNAS]



# Cargo-motor complexes



## Teams of motors

- Dynamics of cargo-motors complexes
- Comparison with experimental data
- Consequences in terms of transport properties

[Welte (2004) Curr. Biol.]

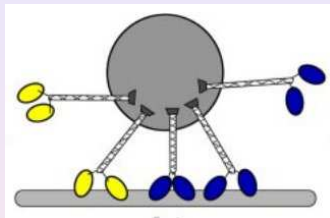
- Dynamics of cargo-motors complexes
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# Tug-of-war, symmetric motors

[Müller, Klumpp, and Lipovsky (2008) PNAS]

## Variables

Number of attached motors  
of each type



## Mean field model

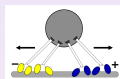
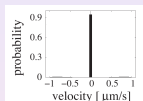
➔ Equal sharing of the force among  
attached motors of one given type

## Motor Dynamics:

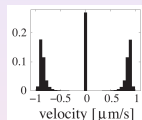
- detachment rate  $\omega = \omega(F_i)$
- motor velocity  $v = v(F_i)$

# Tug-of-war, symmetric motors

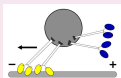
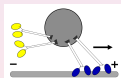
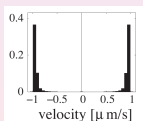
- If motors stop walking before detaching



- Intermediate case



- If motors detach before stall



**MF prediction**

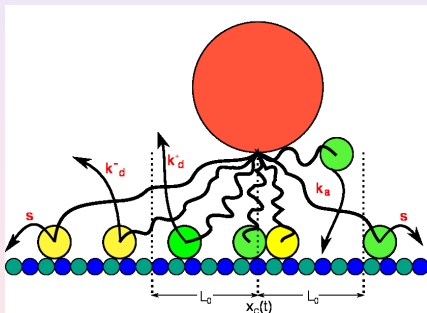
Symmetric bimodal/trimodal distributions of the velocity

- Dynamics of cargo-motors complexes
  - Tug-of-war: Mean-Field model
  - **Explicit Position Based model**
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# Explicit Position Based Model

## EPB-model

- Motor positions are explicitly taken into account
- Motors are linked by springs to the cargo



See Kunwar et al;  
Bouzat et al;

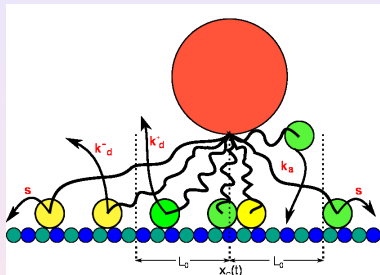
## Variables

Position of each attached motor

Position  $\implies$  Force



# Explicit Position Based Model



## Stochastic Motor Dynamics:

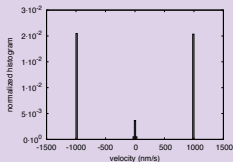
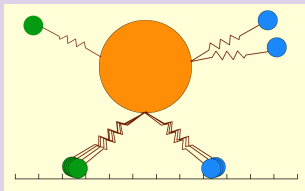
- attachment rate  $\tilde{\omega}$
- stepping rate  $\rho = \rho(F_i)$
- detachment rate  $\omega = \omega(F_i)$

## Cargo dynamics

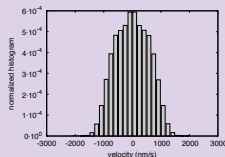
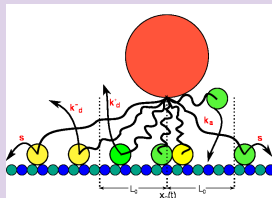
$$m \frac{\partial^2 x_C(t)}{\partial t^2} = -\beta \frac{\partial x_C(t)}{\partial t} + F(x_C, \{x_i\})$$

# Tug-of-war, symmetric motors

## Mean field model



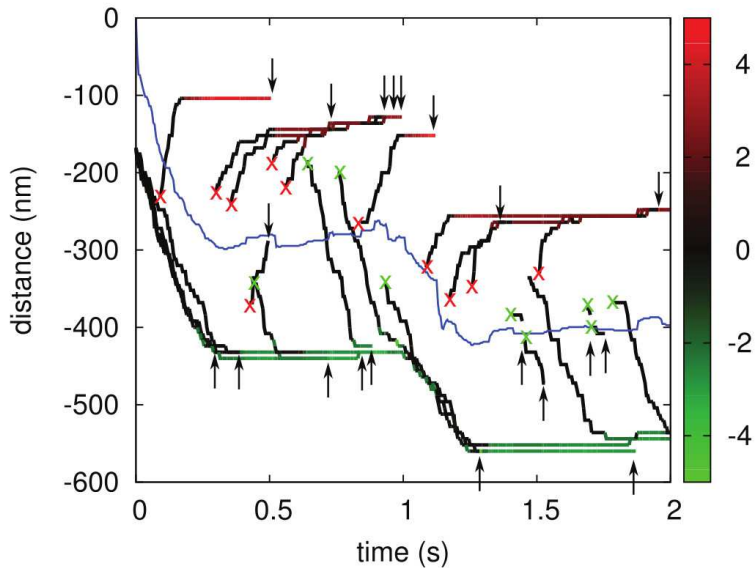
## Non mean field model



For the same motors

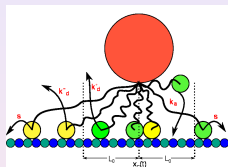
[S. Klein et al, Eur. Phys. J. Special Topics, 223 (2014) 3215]

# Tug-of-war, symmetric motors



# Tug-of-war, asymmetric motors

$N_+$ ,  $N_-$  motors attached to the cargo, among which  $n_+$ ,  $n_-$  attached to the filament

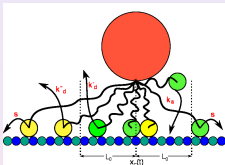


## Asymmetric teams

Kinesins and dyneins behave differently

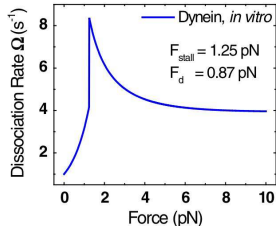
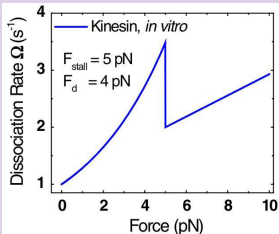
# Tug-of-war, asymmetric motors

$N_+$ ,  $N_-$  motors attached to the cargo, among which  $n_+$ ,  $n_-$  attached to the filament



## Stochastic motor dynamics

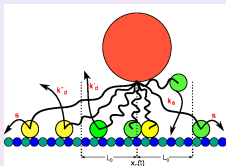
### Detachment rate



From [Kunwar et al (2011) PNAS]

# Tug-of-war, asymmetric motors

$N_+$ ,  $N_-$  motors attached to the cargo, among which  $n_+$ ,  $n_-$  attached to the filament



## Stochastic motor dynamics

- Stepping rate (for  $F_i$  below stall force) :

$$s(|F_i|, [ATP]) = \frac{k_{\text{cat}}(|F_i|)[ATP]}{[ATP] + k_{\text{cat}}(|F_i|)k_b(|F_i|)^{-1}},$$

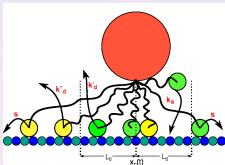
## Michaelis-Menten kinetics

From [Schnitzer et al (2000) Nat. Cell Biol.]

- Stepping rate (for  $F_i$  above stall force) :  
backward stepping  $s_b = v_b/d$

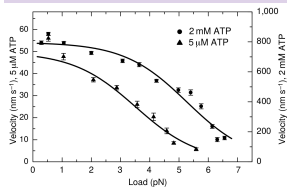
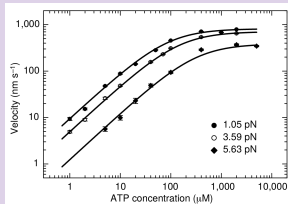
# Tug-of-war, asymmetric motors

$N_+$ ,  $N_-$  motors attached to the cargo, among which  $n_+$ ,  $n_-$  attached to the filament



## Stochastic motor dynamics

[ATP] and force dependence



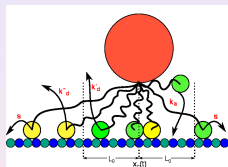
## Comparison for kinesin

From [Schnitzer et al (2000) Nat. Cell Biol.]

From [Visscher et al (1999) Nature]

# Tug-of-war, asymmetric motors

$N_+$ ,  $N_-$  motors attached to the cargo, among which  $n_+$ ,  $n_-$  attached to the filament



How does this cargo-motors complex behave?



- Dynamics of cargo-motors complexes
  - Tug-of-war: Mean-Field model
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# Anomalous diffusion

Preliminary remarks:

## Mean Square Displacement

$$\text{MSD} \equiv \langle (X(t + \Delta t) - X(t))^2 \rangle$$

- Ballistic :  $\text{MSD} \sim \Delta t^2$
- Purely diffusive without bias :  $\text{MSD} \sim \Delta t$
- Anomalous diffusion:  
 $\text{MSD} \sim \Delta t^\gamma$  with  $\gamma < 1$  or  $1 < \gamma < 2$ .

$\langle \rangle$  = average over  $t$ .

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At finite time:

Apparent superdiffusion ( $\gamma > 1$ )

- ➔ biased but uncorrelated motion ?
- ➔ positive temporal correlations of the displacements ?

$\langle \rangle$  = average over  $t$ .

# Anomalous diffusion

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## Variance

$$\begin{aligned} \text{Var} &= \langle (X(t + \Delta t) - X(t))^2 \rangle \\ &- \langle (X(t + \Delta t) - X(t)) \rangle^2. \end{aligned}$$

$\langle \rangle$  = average over  $t$ .

At finite time:

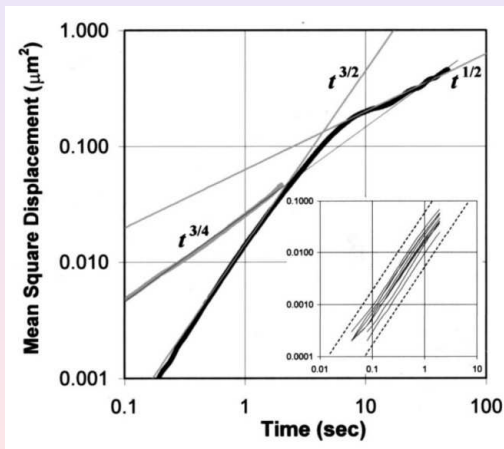
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# Anomalous diffusion

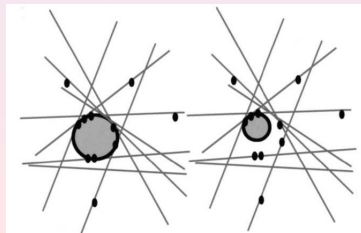
[Caspi et al, PRE (2002) 22, 011916]

Engulfed 2 and 3  $\mu\text{m}$  beads, in living cells,  
driven by microtubule-associated motors



black line: 3  $\mu\text{m}$  beads

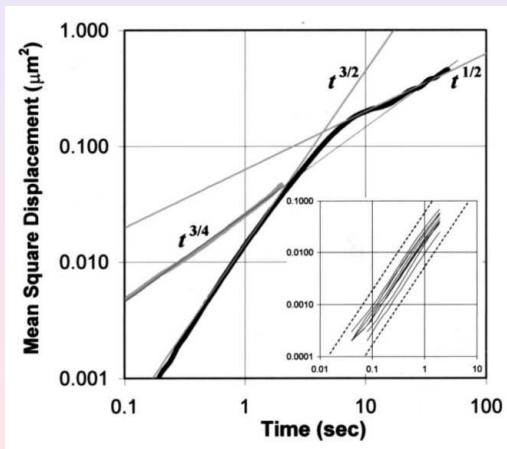
- Enhanced diffusion scaling as  $t^{3/2}$  at short times
- Ordinary (small spheres) or subdiffusive (large) scaling at long times



# Anomalous diffusion

[Caspi et al, PRE (2002) 22, 011916]

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black line: 3  $\mu\text{m}$  beads

- Enhanced diffusion scaling as  $t^{3/2}$  at short times
- Ordinary (small spheres) or subdiffusive (large) scaling at long times

(see also in grey: subdiffusive motion of nondriven lipid spheres granules naturally appearing in these cells)

# Anomalous diffusion

[Salman et al, Chem. Phys. (2002) 284, 389]

*In vitro* experiment with egg extract;  
3  $\mu\text{m}$  beads coated with motors and moving along MTs

$$MSD \sim \Delta t^\gamma$$

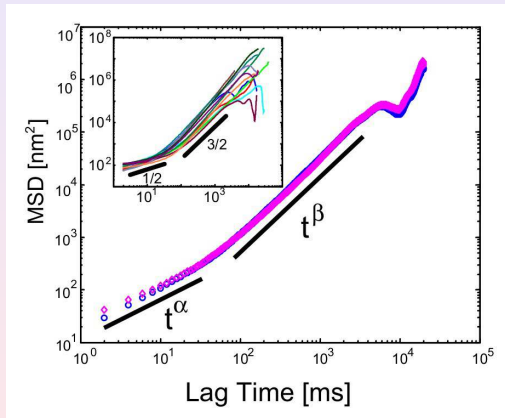
Type of filament	$\gamma$	
MT + actin	$\gamma \simeq 3/2$	superdiffusive
MT (no actin)	$\gamma \simeq 3/2$	superdiffusive
Actin (no MT)	$\gamma \simeq 3/4$	subdiffusive
no MT, no actin	$\gamma \simeq 1$	diffusive

*“the  $t^{3/2}$  behavior comes about due to a hindrance to ballistic motion”*

# Anomalous diffusion

[Kulic et al (2008) PNAS **105**, 10011]

Peroxisome trajectories in *Drosophila* S2 cells



- ➔ At short time scales (below 30ms): subdiffusion
- ➔ At intermediate times: superdiffusion
- ➔ At longer time scales: diffusion or subdiffusion.

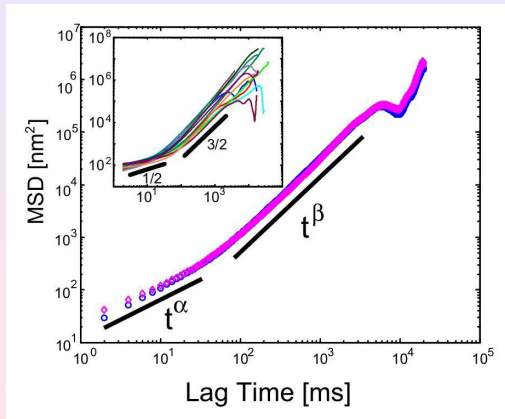
$$\alpha = 0.59 \pm 0.28 \text{ and } \beta = 1.62 \pm 0.29$$



# Anomalous diffusion

[Kulic et al (2008) PNAS **105**, 10011]

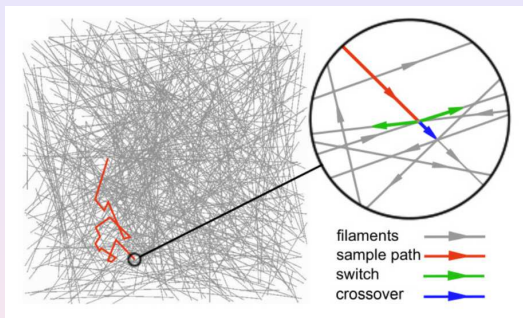
Peroxisome trajectories in *Drosophila* S2 cells



$$\alpha = 0.59 \pm 0.28 \text{ and } \beta = 1.62 \pm 0.29$$

*“an exponent close to 1.5, an observation challenging the simple motor-hauling-a-cargo and random motor switching model and indicating the movements of microtubules”*

# Network Effects



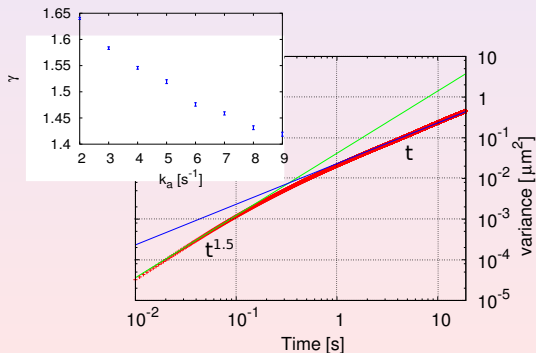
- On a branched network, purely ballistic motion also shows  $\text{Var}[X] \sim \Delta t^\gamma$  with  $1 < \gamma < 2$  depending on the turning angle distribution

[Shaebani et al (2014) PRE 90, 030701(R)]

# Anomalous diffusion

## Cargo dynamics

$$m \frac{\partial^2 x_C(t)}{\partial t^2} = -\beta \frac{\partial x_C(t)}{\partial t} + F(x_C(t), \{x_i\})$$

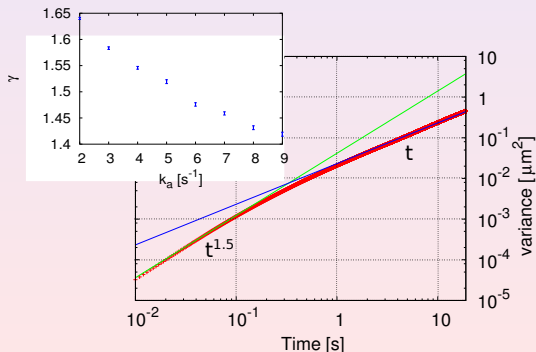


[Klein et al, EPL (2014)]

# Anomalous diffusion

## Cargo dynamics

$$m \frac{\partial^2 x_C(t)}{\partial t^2} = -\beta \frac{\partial x_C(t)}{\partial t} + F(x_C(t), \{x_i\})$$



[Klein et al, EPL (2014)]

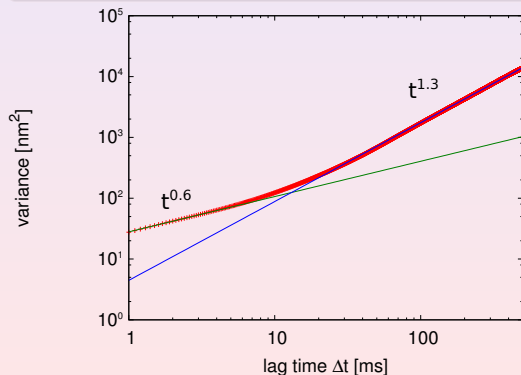
No need for further ingredient

Superdiffusion can be explained by cargo-motors dynamics

# Anomalous diffusion

## Cargo dynamics with thermal noise

$$m \frac{\partial^2 x_C(t)}{\partial t^2} = -\beta \frac{\partial x_C(t)}{\partial t} + F(x_C(t), \{x_i\}) + \sqrt{2k_B T \beta} \xi(t)$$



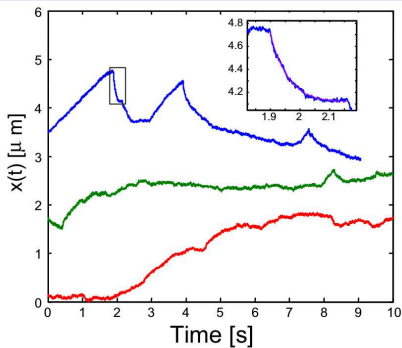
[Klein et al, EPJST (2014)]

$v_f = 1000$  nm/s

$d = 8$  nm

Crossover time  $\simeq$  delay  
between steps

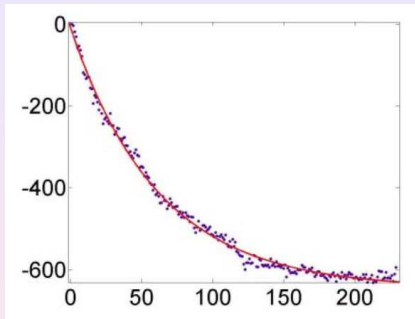
# Relaxation phenomenon



*“These velocity relaxation events indicated the presence of an elastic component in the system and suggested that bent and buckled microtubules could influence peroxisome transport”*

[Kulic et al (2008) PNAS **105**,  
10011]

# Relaxation phenomenon

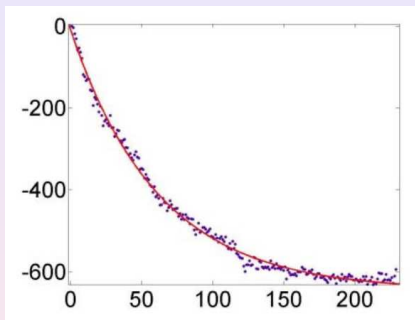


Time (ms)

*“These velocity relaxation events indicated the presence of an elastic component in the system and suggested that bent and buckled microtubules could influence peroxisome transport”*

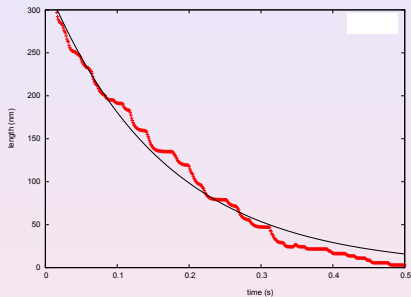
[Kulic et al (2008) PNAS **105**,  
10011]

# Relaxation phenomenon



Time (ms)

[Kulic et al (2008) PNAS **105**,  
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EPB Model

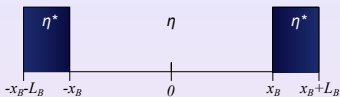
Elastic energy can be stored and  
released when a motor detaches



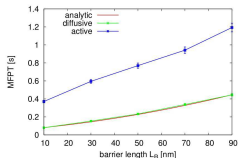
# Dynamics of cargo-motors complexes along a single filament

- The EPB model allows to reproduce some experimental observations:
  - anomalous diffusion
  - elastic relaxation events
- Why is it interesting for the cell to have these cargo-motors complexes?

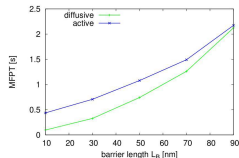
# Active transport versus diffusion



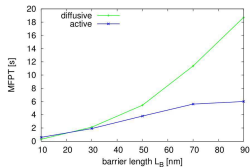
- (a)  $\eta^* = \eta$ ,
- (b)  $\eta^* = 10\eta$ ,
- (c)  $\eta^* = 100\eta$



(a)



(b)



(c)

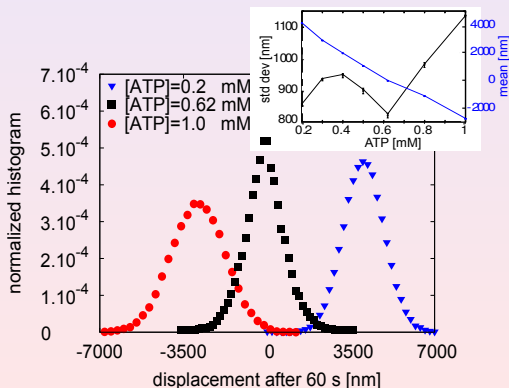
[Klein et al, EPJST (2014)]

- Dynamics of cargo-motors complexes
  - Tug-of-war: Mean-Field model
  - Explicit Position Based model
  - Anomalous diffusion
  - External control
- Interplay between transport and lattice dynamics
  - Impact of lattice dynamics on transport
  - Lattice deformation driven by active cross-linkers

# Control by fuel supply

## Stall force ATP dependence

- Kinesin: constant  $F_s = 2.6$  pN
- Dynein:  $F_s$  varies linearly from 0.3 pN at vanishing [ATP] to 1.2 pN for saturating [ATP]



$$N_+ = N_- = 5$$

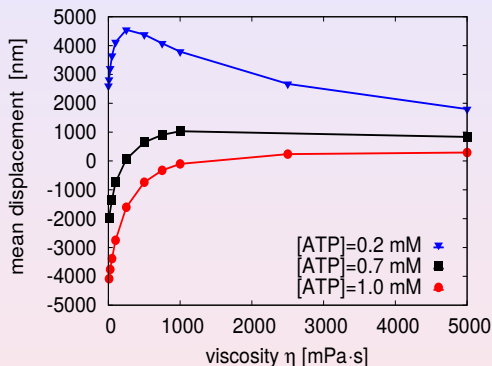
From [Klein et al (2014) EPL]

## ATP dependence

- More energy (ATP) can slow down the cargo
- It can also reverse cargo velocity

# Control by External Force

## Effective viscosity dependence



$$N_+ = N_- = 5$$

## Viscosity dependence

- Increase of viscosity can speed up the cargo
- It can also reverse cargo velocity

## Advantage

Easy control of the cargo-motors complex by a single external parameter

From [Klein et al (2014) EPL]

# Conclusion

- Many experimental observations can already be explained by the stochastic motion of cargo-motors complexes along a single microtubule.
- Highly controllable system.
- Our predictions for [ATP] dependence or external force control could be tested experimentally.

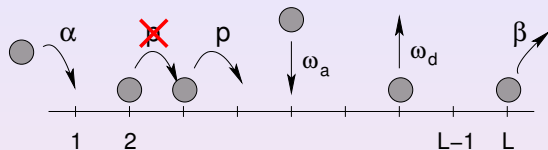
## Challenges

- Need of well controlled experiments to check tug-of-war scenarios
- In vitro / in vivo differences?

- Dynamics of cargo-motors complexes
  - Tug-of-war: Mean-Field model
  - Explicit Position Based model
  - Anomalous diffusion
  - External control
- Interplay between transport and lattice dynamics
  - **Impact of lattice dynamics on transport**
  - Lattice deformation driven by active cross-linkers

# Collective effects

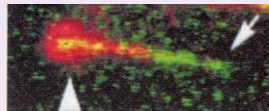
## Cellular automata models with one type of motors



[Lipowsky, Klumpp, & Nieuwenhuizen, P.R.L. (2001)]  
[Parmeggiani, Franosch, & Frey, P.R.L. (2003)]  
[J. Tailleur, M. Evans, & Y. Kafri, P.R.L. (2009)]

### *In vitro*

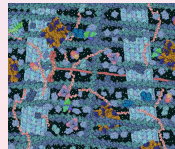
- well suited for motility assays, predicts the experimentally observed bulk localization of high and low density domains



[Nishinari, Okada, Schadschneider, & Chowdhury, P.R.L. (2005)]

### *In vivo*

- Crowded environment
- No infinite diffusion



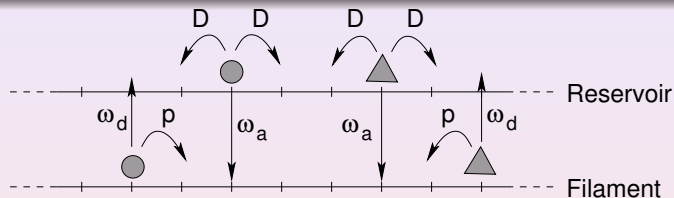
[by Tim Vickers]



# Collective effects in bidirectional intracellular transport

## Ingredients

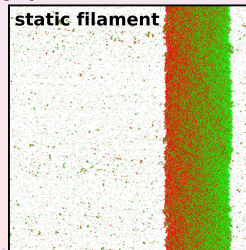
- Two types of complexes going in opposite directions
- Confined diffusion in the surrounding cytoplasm



[M. Ebbinghaus and L. Santen, J. Stat. Mech. (2009)]

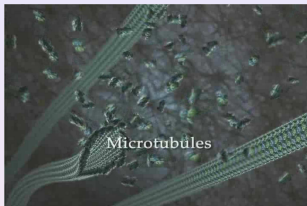
## Jamming

- ➔ No transport in thermodynamic limit
- ➔ Offering multiple filaments enhances cluster formation.



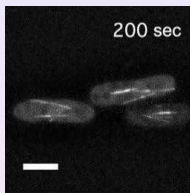
# Intra-cellular traffic - Dynamic instability

MTs exhibit stochastic switching between a shrinking and a growing state



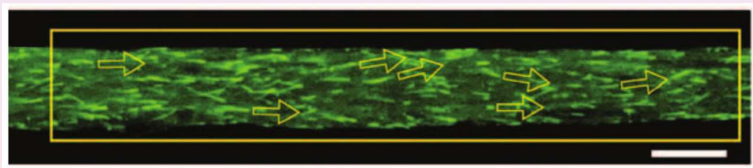
[A. Viel, R. A. Lue and J. Liebler, BioVisions project, <http://multimedia.mcb.harvard.edu>]

Microtubules seen by fluorescence in *S. pombe* (yeast)



Scale bar = 5  $\mu\text{m}$

[M. Erent, D.R. Drummond, R.A. Cross (2012) PLoS ONE 7(2): e30738]

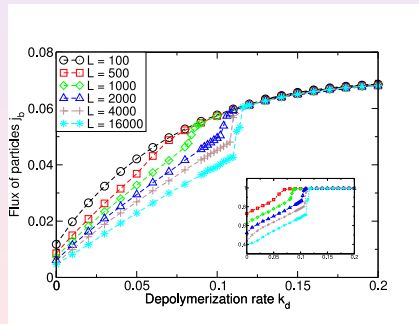
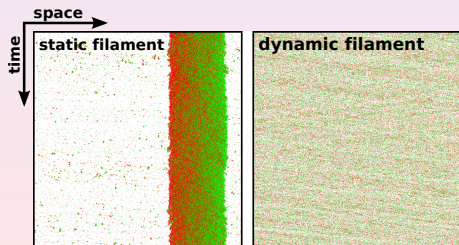
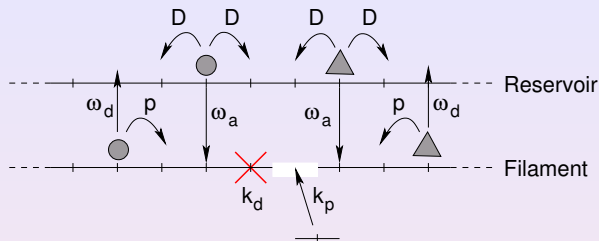


[Shemesh, Erez, Ginzburg, Spira. *Traffic* (2008)]

1s (video) = 120s (real time)

Scale bar = 10  $\mu\text{m}$

# Dynamics of the lattice



[Ebbinghaus, Appert, Santen, PRE 82 (2010) 040901]

- ☞ Drugs modifying the dynamics of the microtubules induce jams
  - video 1: microtubule dynamics with and without drugs (Paclitaxel)

[*Shemesh and Spira, Acta Neuropathol (2010) 119:235*]

- ☞ Drugs modifying the dynamics of the microtubules induce jams
  - video 2: microtubule dynamics and pinocytotic vesicles transport without drugs

[*Shemesh and Spira, Acta Neuropathol (2010) 119:235*]

- ☞ Drugs modifying the dynamics of the microtubules induce jams
  - video 3: microtubule dynamics and pinocytotic vesicles transport with drugs

[*Shemesh and Spira, Acta Neuropathol (2010) 119:235*]

# Challenges

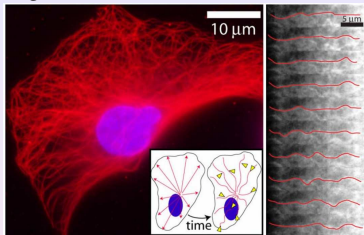
- A full picture of the axonal MT network is still missing
- Understanding the mechanisms of transport breakdown in neurodegenerative diseases

- Dynamics of cargo-motors complexes
  - Tug-of-war: Mean-Field model
  - Explicit Position Based model
  - Anomalous diffusion
  - External control
- Interplay between transport and lattice dynamics
  - Impact of lattice dynamics on collective cargo transport
  - Lattice deformation driven by active cross-linkers



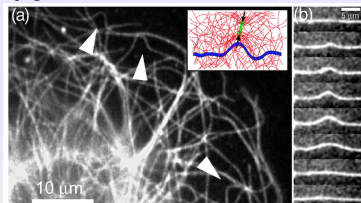
# MT deformation: Observations

*In vivo*



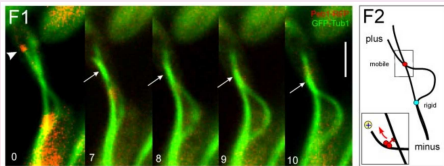
[Brangwynne et al, PNAS (2007)]

*In vitro*



[Brangwynne et al, PRL (2008)]

MT embedded in actomyosin gel



[Straube et al, Molec. Biol. of the Cell (2006)]

MT-MT interactions mediated by conventional kinesin (fungus *Ustilago maydis*)

**In vitro measurements**

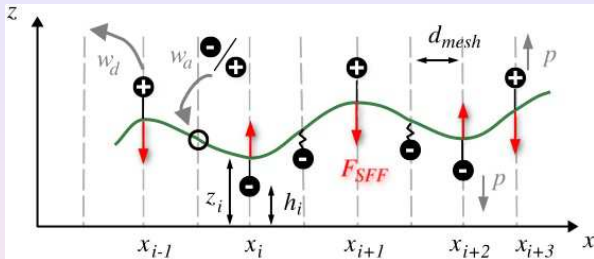
Persistence length of a free MT  
= a few mm

**In vivo measurements**

Persistence length of MTs = 30  
 $\mu\text{m}$

# Model definition

[Ines Weber, Cécile Appert-Rolland, Grégory Schehr, and Ludger Santen, "Non-equilibrium fluctuations of a semi-flexible filament driven by active cross-linkers" (2017) submitted]

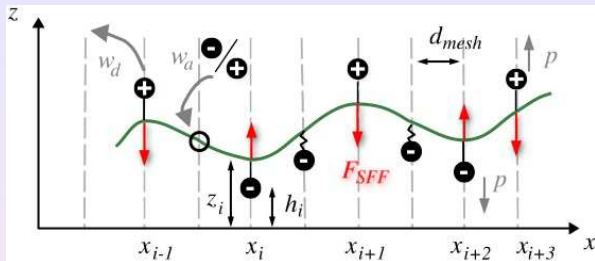


## Model

- Semi-flexible filament  $E = k \int_0^L \left(\frac{\partial \theta}{\partial s}\right)^2 ds$
- Connected to a background network by active cross-linkers
- Stochastic dynamics for the cross-linkers
- Cross-linkers feel a force  $F_{SFF}$  only for elongated chain

$k$  = bending rigidity

# Model definition



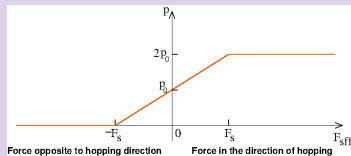
## Active Cross-linkers

- bind at available sites with rate  $\omega_a$
- ➔ Polarity of the background filament chosen at each attachment event

- unbind with rate

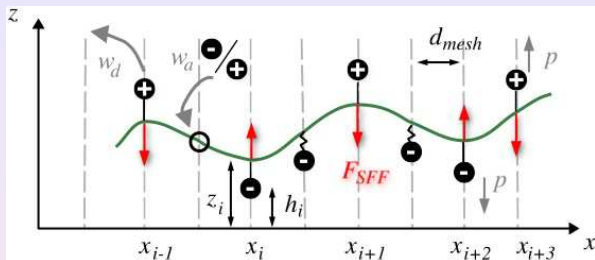
$$\omega_d = \omega_{d0} \exp\left(\frac{|F_{SFF}|}{F_d}\right)$$

- step with rate  $\rho(F_{SFF})$



$F_s$  = stall force.

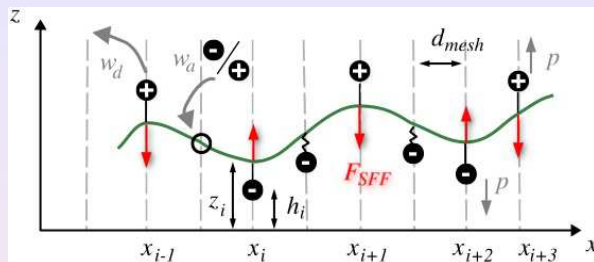
# Model definition



## Coupling SFF / linkers

- $\{x_i\}$  = positions of pulling linkers (elongated chains)
- Between  $x_i$  and  $x_{i+1}$ :  $F$  = Force / unit length  
 $E_i = k \int_{x_i}^{x_{i+1}} [\partial_x^2 u_i(x)]^2 dx$       and       $F \sim \partial_x^4 u_i(x)$
- Equilibrium shape  
 $F = 0 \Rightarrow u_i(x) = a_i(x - x_i)^3 + b_i(x - x_i)^2 + c_i(x - x_i) + d_i$

# Model definition



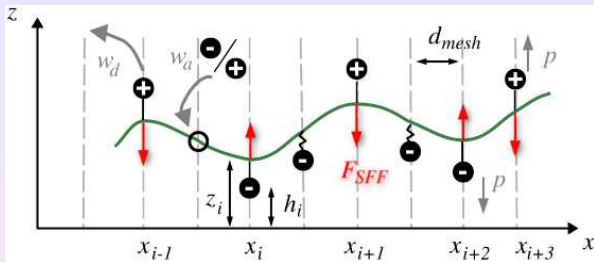
## Coupling SFF / linkers

- We put end-to-end these segments with boundary conditions :

$$\begin{aligned}u_i(x_i) &= z_i, & u_i(x_{i+1}) &= z_{i+1} \\ \partial_x u_i(x_i) &= v_i, & \partial_x u_i(x_{i+1}) &= v_{i+1}\end{aligned}$$

- $z_i$  = vertical displacement of the SFF imposed at position  $x_i$
- $v_i$  = the local slope  $\rightarrow$  differentiability of the global polynomial

# Model definition



## Coupling SFF / linkers

- For each set of positions  $\{x_j\}$ , we find
  - ➔ the global equilibrium shape of the SFF
  - ➔ the local force exerted at each attachment point:

$$F_k = \frac{\partial E}{\partial z_k} = 24k \left( \frac{\Delta z_{k-1}}{\Delta x_{k-1}^3} - \frac{\Delta z_k}{\Delta x_k^3} \right) - 12k \left\{ v_k \left( \frac{1}{\Delta x_{k-1}^2} - \frac{1}{\Delta x_k^2} \right) \right\} - 12k \left\{ \frac{v_{k-1}}{\Delta x_{k-1}^2} - \frac{v_{k+1}}{\Delta x_k^2} \right\}$$

## Update scheme

- We update the system of linkers with a tower sampling algorithm and perform stochastic events until the occurrence of an event that modifies the force exerted on the SFF
  - Then the new equilibrium shape of the SFF is calculated
  - The new forces exerted on the linkers are obtained and the value of force-dependent rates is calculated for each linker.
- ➔ Can model cascades of detachment
- ➔ Understanding how deformations originate from microscopic discrete forcing

# Non-equilibrium fluctuations of a SFF driven by active cross-linkers

## Results

- ➔ Obtain deformation spectrum
- ➔ Obtain persistence length
- ➔ Investigate the role of parameters (rigidity, mesh size, etc)
- ➔ Compare thermal and active linkers to identify geometrical effects



# Deformation spectrum

## Decomposition into cosine modes

$$\theta(s) = \sqrt{2/L} \sum_{n=0}^{\infty} a(q) \cos(qs)$$

with the wavenumber  $q = (n\pi/L)$

## Thermal fluctuations in 2D

The variance of cosine modes' amplitudes is known to vary with  $q$  as

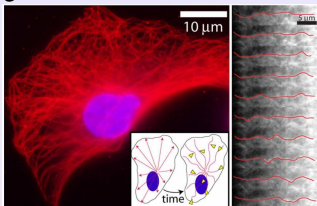
$$\text{Var}(a(q)) \equiv \langle a(q)^2 \rangle = \frac{1}{L_p} \frac{1}{q^2} \quad \text{with} \quad L_p^{\text{thermal}} = \frac{2k}{k_B T}.$$

## Non-thermal fluctuations

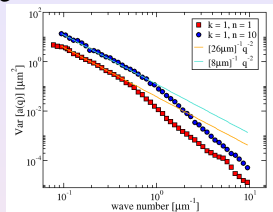
No reason to have  $q^{-2}$  dependence

# Deformation spectrum

*In vivo*



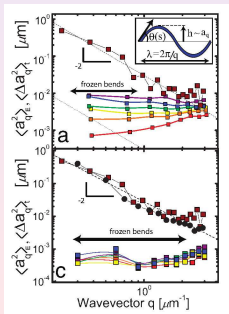
*In silico*



[I. Weber et al, submitted (2017)]

Red squares: parameters inspired by biological system. The  $q^{-2}$  behavior (orange line) for small  $q$  can be associated with a persistence length of  $26\mu\text{m}$ .

Generic: no clear  $q^{-2}$  behavior.



[Brangwynne et al, PNAS (2007)]

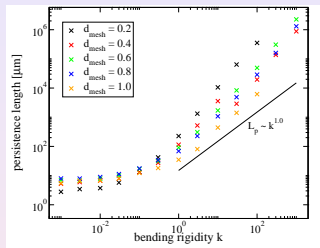
## For two dimensional fluctuations

Auto-correlation of the tangent angle  $\theta$

$$\langle \cos (\theta(s) - \theta(s')) \rangle = \exp (-|s - s'|/(2L_p))$$

$$L_p^{thermal} = \frac{2k}{k_B T}$$

# Persistence length



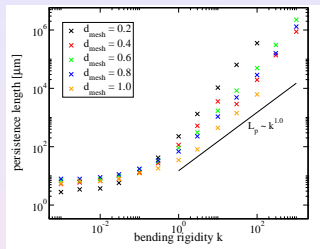
$$k = 1 \text{ for MTs}$$

Straight line = the linear increase expected for purely thermal fluctuations

## Rigidity dependence

- For small  $k$ , deformations are limited by the mesh size.
- For  $k \geq 1$ , super-linear increase of the persistence length up to, and beyond the SFF length.

# Persistence length



$$k = 1 \text{ for MTs}$$

Straight line = the linear increase expected for purely thermal fluctuations

## Mesh size dependence (fixed number of linkers)

- ➔ For small  $k$ , the persistence length slightly decreases with  $d_{\text{mesh}}$  (This dependence is linear in  $d_{\text{mesh}}$ )
- ➔ For large  $k$ , it is the contrary! When  $d_{\text{mesh}}$  decreases, the curvature induced by a single linker step is more pronounced. At high  $k$ , this results into strong load forces, which most likely the linker will not be able to sustain. Therefore, it is difficult to deform the stiff SFF at all, if the density of cross-linkers is too high.

# Non-equilibrium fluctuations of a SFF driven by active cross-linkers

- Model allowing to couple the dynamics of a SFF with the stochastic dynamics of active linkers.
  - Deformation spectrum
  - investigate the role of parameters (rigidity, mesh size, etc)
- Can be generalized to other types of cross-linkers.
- We could have expected that one type of motors could pull off the other. This is not the case.
  - ➡ cf Tug-of-war

## Challenges

- In vitro experiments in simplified geometry?

For more details:

[http://www.th.u-psud.fr/page\\_perso/Appert/](http://www.th.u-psud.fr/page_perso/Appert/)

# Thank-you