**Computer Algebra for Functional Equations in Combinatorics and Physics** 



ID de Contribution: 17

Type: Non spécifié

## Stretched exponentials and beyond by Michael Wallner

lundi 4 décembre 2023 11:00 (1 heure)

Abstract. The appearance of a stretched exponential term  $\mu^{n^{\sigma}}$  with  $\mu > 0$  and  $\sigma \in (0, 1)$  in a counting sequence  $(c_n)_{n\geq 0}$  is not common, although more and more examples are appearing lately. Proving that a sequence has a stretched exponential is often quite difficult. This is in part because such a sequence cannot be "very nice": its generating function cannot be algebraic, and it can only be D-finite if it has an irregular singularity. Previously, the saddle-point method was the only generic method for proving such a phenomenon, but it requires detailed information about the generating function. Recently, together with Andrew Elvey Price and Wenjie Fang, we have developed a new method at the level of recurrences to prove stretched exponentials. I will introduce the basics of this method and show how it can be extended to other problems. Then I will summarize recent progress (new bijections, limit laws, etc.) in the study of compacted trees, a subclass of directed acyclic graphs. Finally, I will give an outlook on how these results now allow an in-depth study of limit shapes and open many new avenues for further research.