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Border rank, homogeneity and de-bordering paradigms in GCT by Pranjali Dutta

Tuesday, September 26, 2023 2:00 PM (1 hour)

Abstract. Border (or approximative) complexity of polynomials plays an integral role in GCT (Geometric Complexity Theory) approach to $P \stackrel{?}{=} NP$. This raises an important basic question: can arbitrary approximations of simple polynomials involve exponential-precision which may not be efficiently simulable? Circuits of depth 3 or 4, are a good testing ground for this question. Recently, Kumar proved that *any* polynomial f can be approximated arbitrarily well by restrictions of the polynomial $x_1 \dots x_n - 1$ for n large enough. In this talk, we will see a stronger connection (& reverse) of this result with the border rank of f , and how homogeneity can play an important role in border complexity.

Furthermore, we will see the border of constant top-fanin depth-3 circuits (which is far more general than $x_1 \dots x_n - 1$) is relatively easy & hierarchical - it can be computed by a polynomial-size algebraic branching program (ABP).

This is based on the joint works with – 1) Prateek Dwivedi & Nitin Saxena (FOCS'21) 2) Nitin Saxena (FOCS'22) 3) Fulvio Gesmundo, Christian Ikenmeyer, Gorav Jindal and Vladimir Lysikov (submitted).