

A Γ -convergence result for non-self dual U(1)-Yang–Mills–Higgs energies of Ginzburg–Landau type

Tuesday, July 5, 2022 4:00 PM (30 minutes)

Let $E \rightarrow M$ be a Hermitian complex line bundle with structure group $U(1)$ over a closed smooth orientable connected Riemannian manifold M . Fix a smooth metric connection D_0 on E and consider, for $\varepsilon > 0$, the non-self dual U(1)-Yang–Mills–Higgs energies

$$G_\varepsilon(u_\varepsilon, A_\varepsilon) := \int_M \frac{1}{2} |D_{A_\varepsilon} u_\varepsilon|^2 + \frac{1}{4\varepsilon^2} (1 - |u_\varepsilon|^2)^2 + \frac{1}{2} |F_{A_\varepsilon}|^2 \text{vol}_g,$$

where $(u, A) \in W^{1,2}(M, E) \times W^{1,2}(M, T^*M)$, $D_A := D_0 - iA$, and F_A denotes the curvature form of D_A . The functionals G_ε arise as natural generalisation of the usual Ginzburg–Landau energy on domains of \mathbb{R}^n .

The aim of the talk is to illustrate the following Γ -convergence result, obtained in collaboration with G. Canevari and G. Orlandi (Università di Verona): as $\varepsilon \rightarrow 0$, the rescaled functionals $\frac{G_\varepsilon}{|\log \varepsilon|}$ Γ -converge, in the flat topology of Jacobians, to $(\pi$ times) the codimension two area functional.

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