On some resolutions in the category $(H^{\bullet}V)_{fg} - \mathcal{U}$

Let V be an elementary abelian 2-group and X be a finite V-CW-complex. Using results of H.-W. Henn, we will show that if the equivariant cohomology $\mathrm{H}^{\bullet}_{V}(X;\mathbb{F}_{2})$ is free as a module over $\mathrm{H}^{\bullet}(V;\mathbb{F}_{2})$ then this equivariant cohomology admits a canonical resolution, of length dim V, in the category $(\mathrm{H}^{\bullet}V)_{\mathrm{fg}} - \mathcal{U}$ whose objects are the $\mathrm{H}^{\bullet}(V;\mathbb{F}_{2})$ -A-modules (A denoting the Steenrod algebra) which are finitely generated as $\mathrm{H}^{\bullet}(V;\mathbb{F}_{2})$ -modules.

This is joint work with D. Bourguiba, L. Schwartz and S. Zarati.