

# THE MASSIVE BINARY BLACK HOLE POPULATION ACROSS COSMIC TIME SEEN UNDER A SEMI-ANALYTICAL PERSPECTIVE

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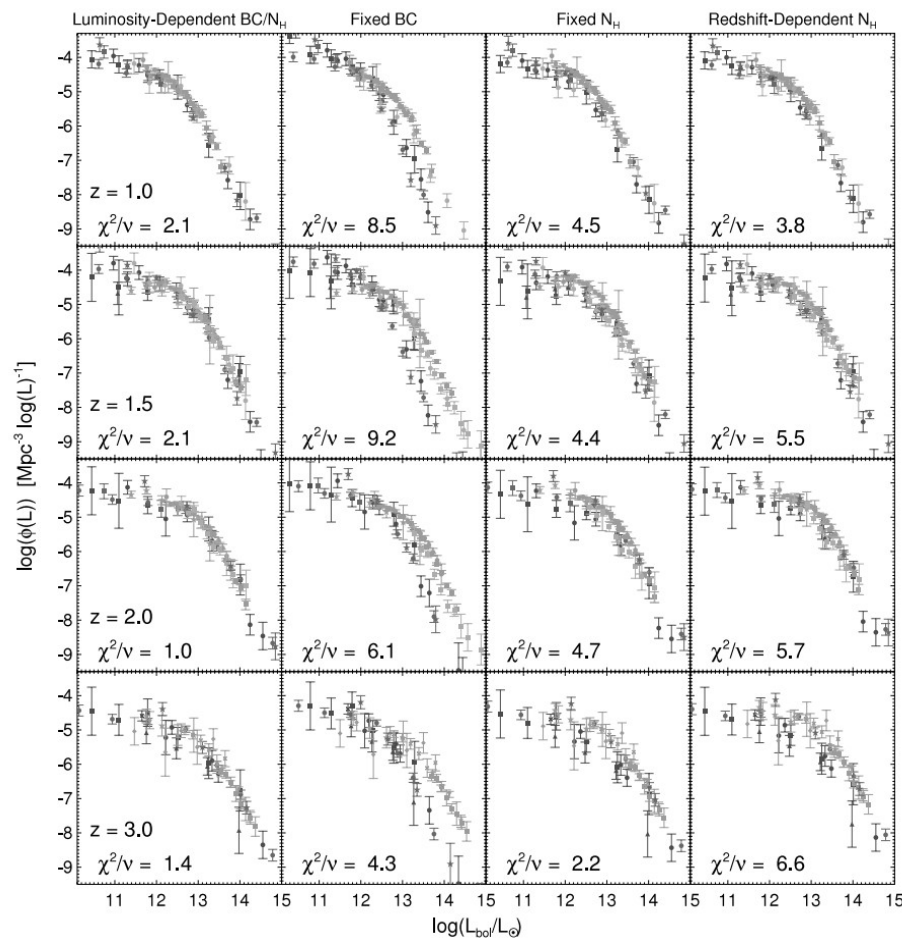
Silvia Bonoli (DIPC)

# OUTLINE

- \* Introduction : Massive black holes and massive binary black holes
- \* The model used to study the massive (binary) black holes in a cosmological context
- \* Results
- \* Conclusions

# INTRODUCTION

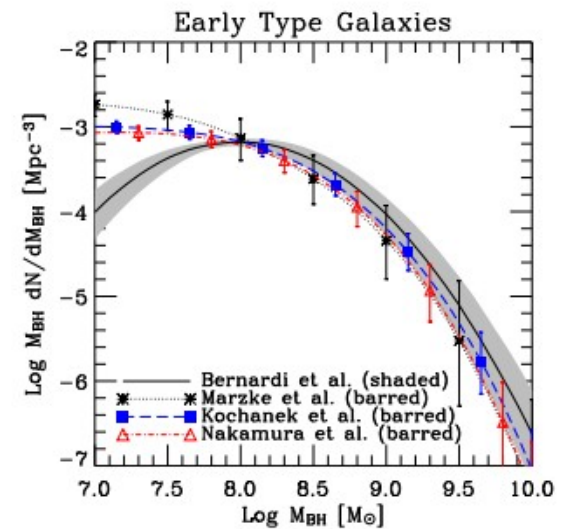
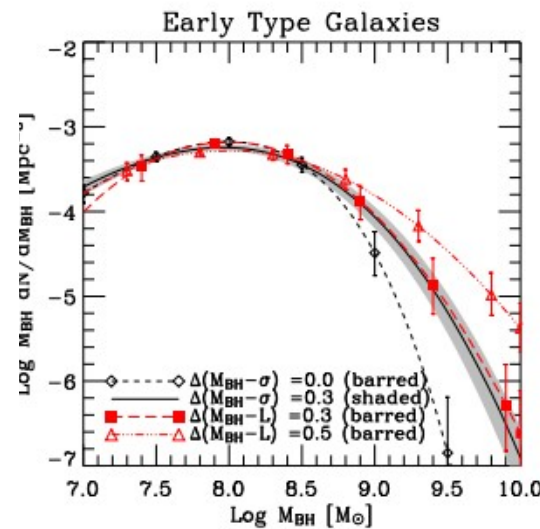
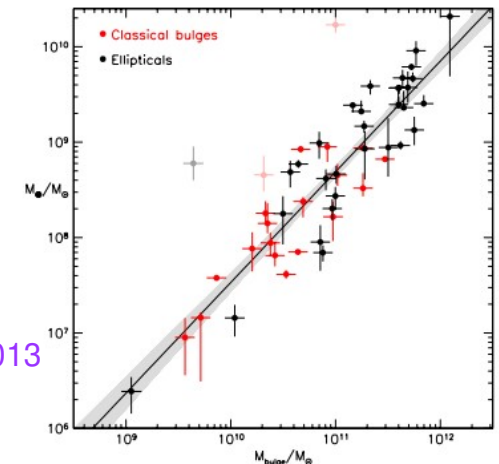
- \* Our relationship with massive black holes started in 1963 when Schmidt M. found the first quasar
- \* More and more people studied the population of quasars: Luminosity functions, scaling relations ...



Hopkins et al. 2009

Kormendy & Ho et al. 2013

Marconi et al. 2004



- \* We reached the CONCLUSION that

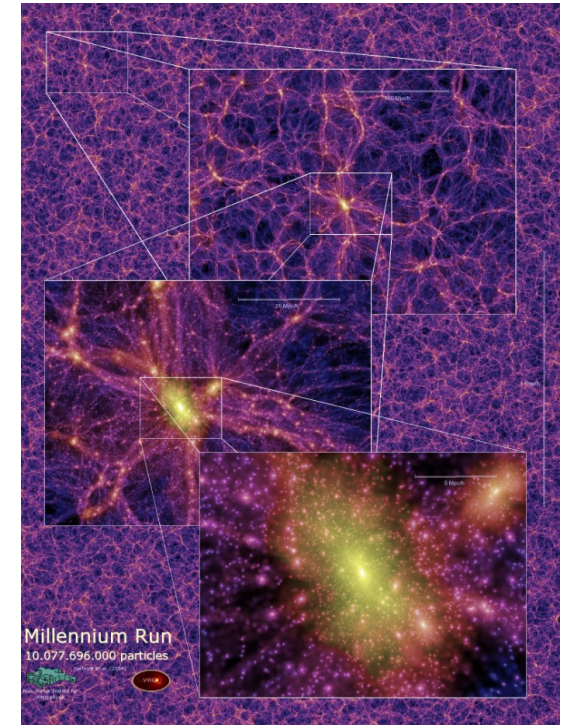
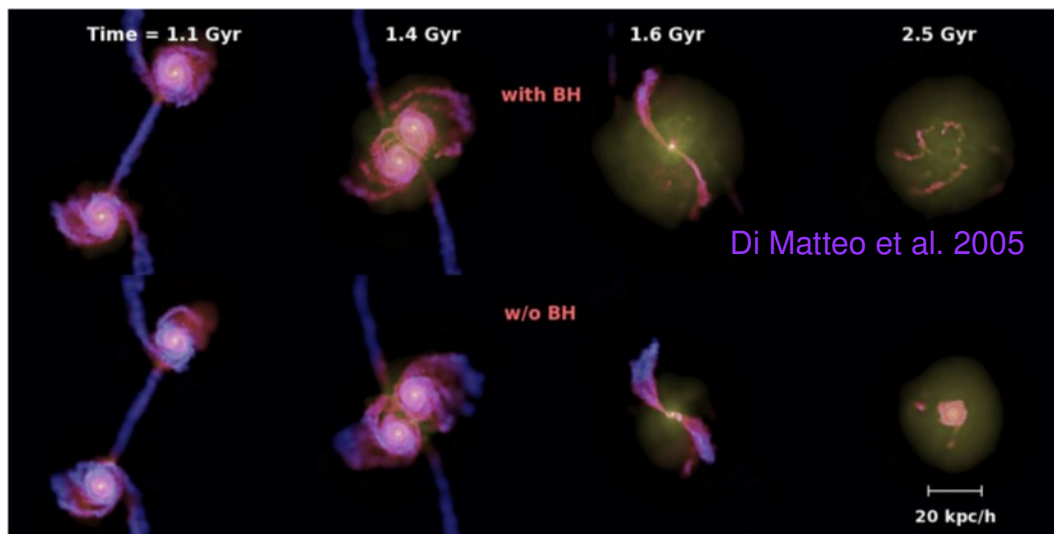
MASSIVE BLACK HOLES ( $>10^6 M_{\text{sun}}$ ) ARE UBIQUITOUS IN ALL GALAXIES

# INTRODUCTION

\* MASSIVE BLACK HOLES ( $>10^6 M_{\text{sun}}$ ) ARE UBIQUITOUS IN ALL GALAXIES

HIERARCHICAL GROWTH OF THE STRUCTURES:

Mergers are one of the main drivers of galaxy evolution



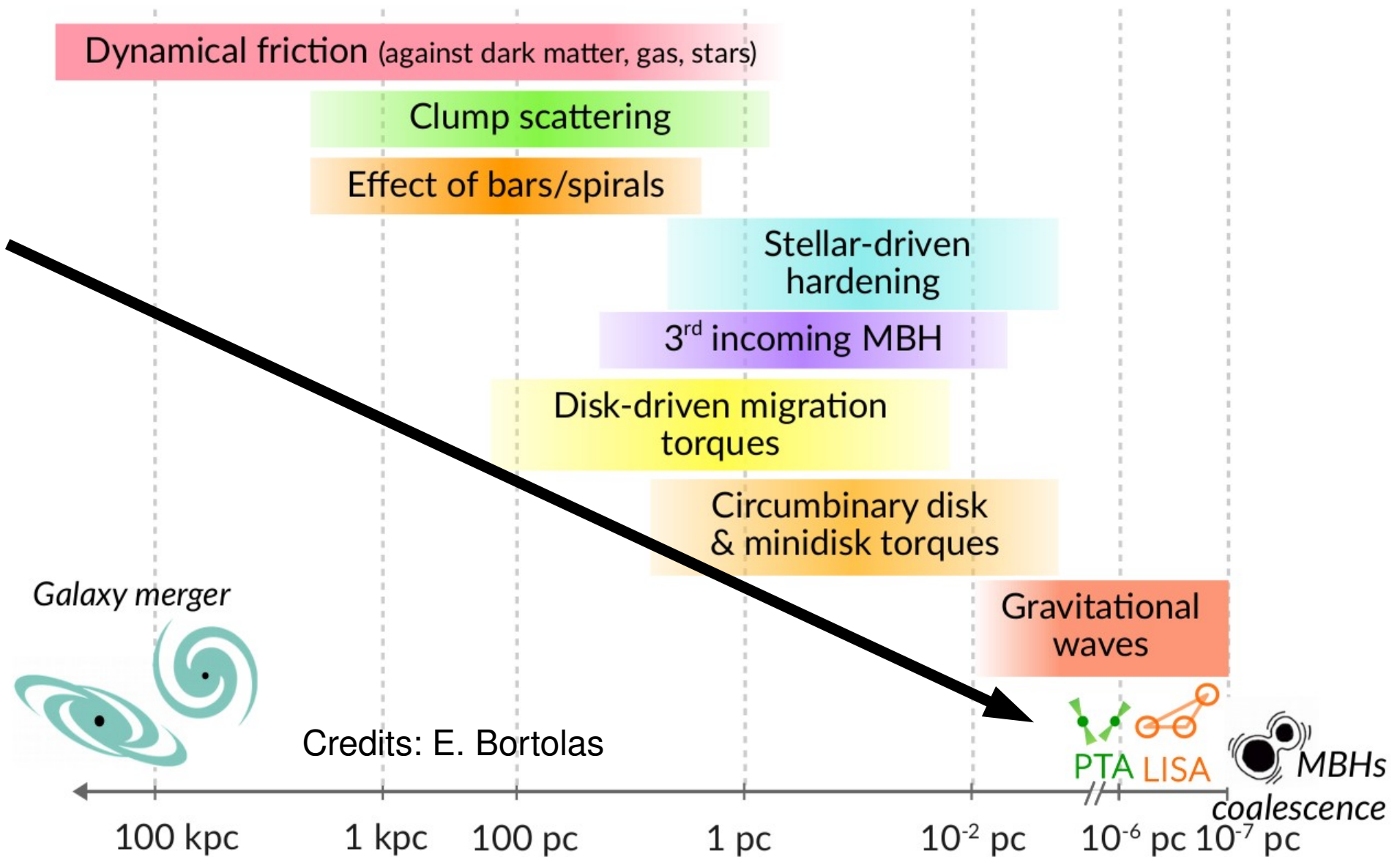
GALAXIES MIGHT HOST **MORE** THAN ONE MASSIVE BLACK HOLE

BLACK HOLES ARE DEPOSITED FAR AWAY ( $> \text{kpc}$ )

IS POSSIBLE BRING THE TWO BLACK HOLES TOGETHER ( $\sim \text{pc}$ ) ?

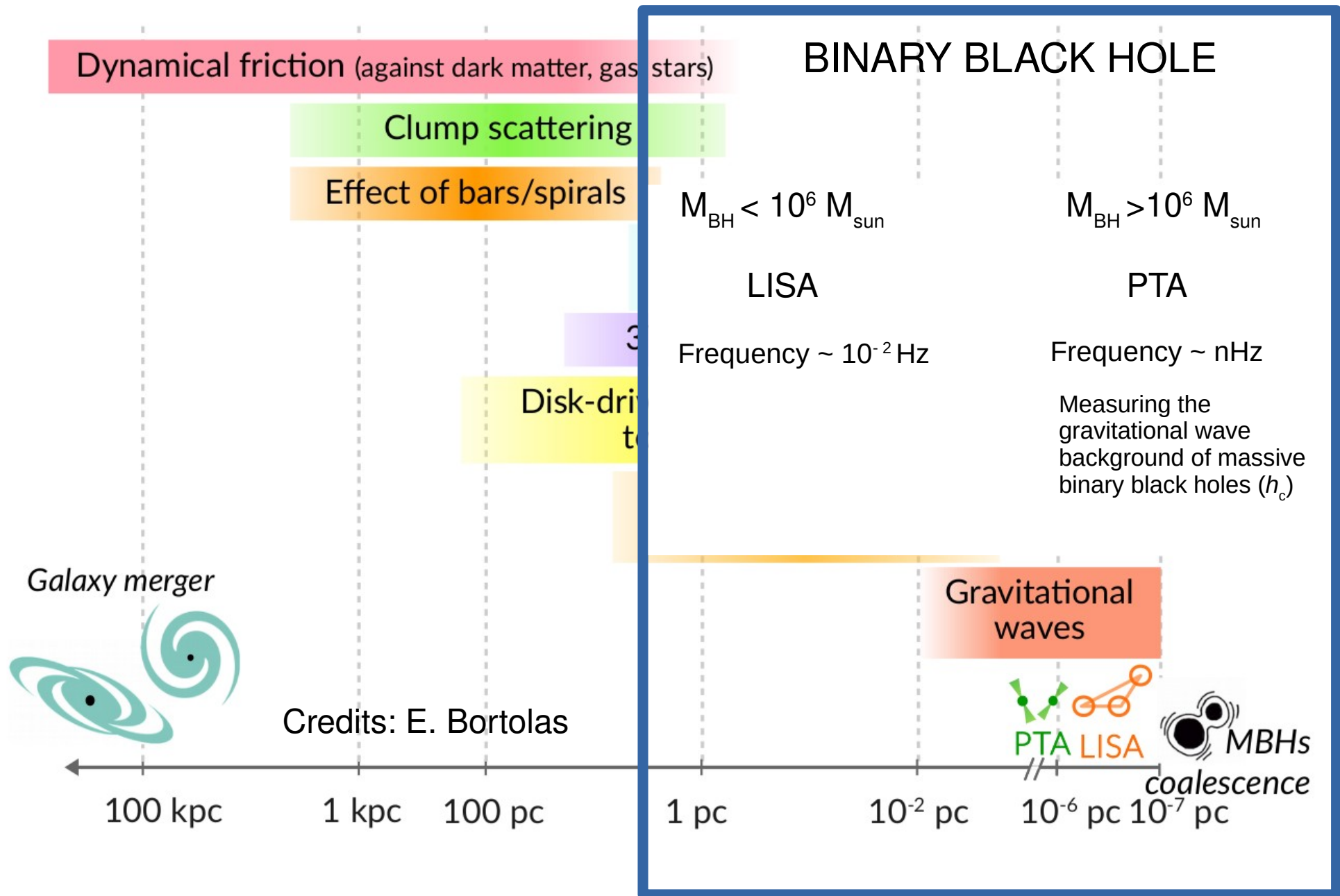
# INTRODUCTION

Many works have tackled this problem...

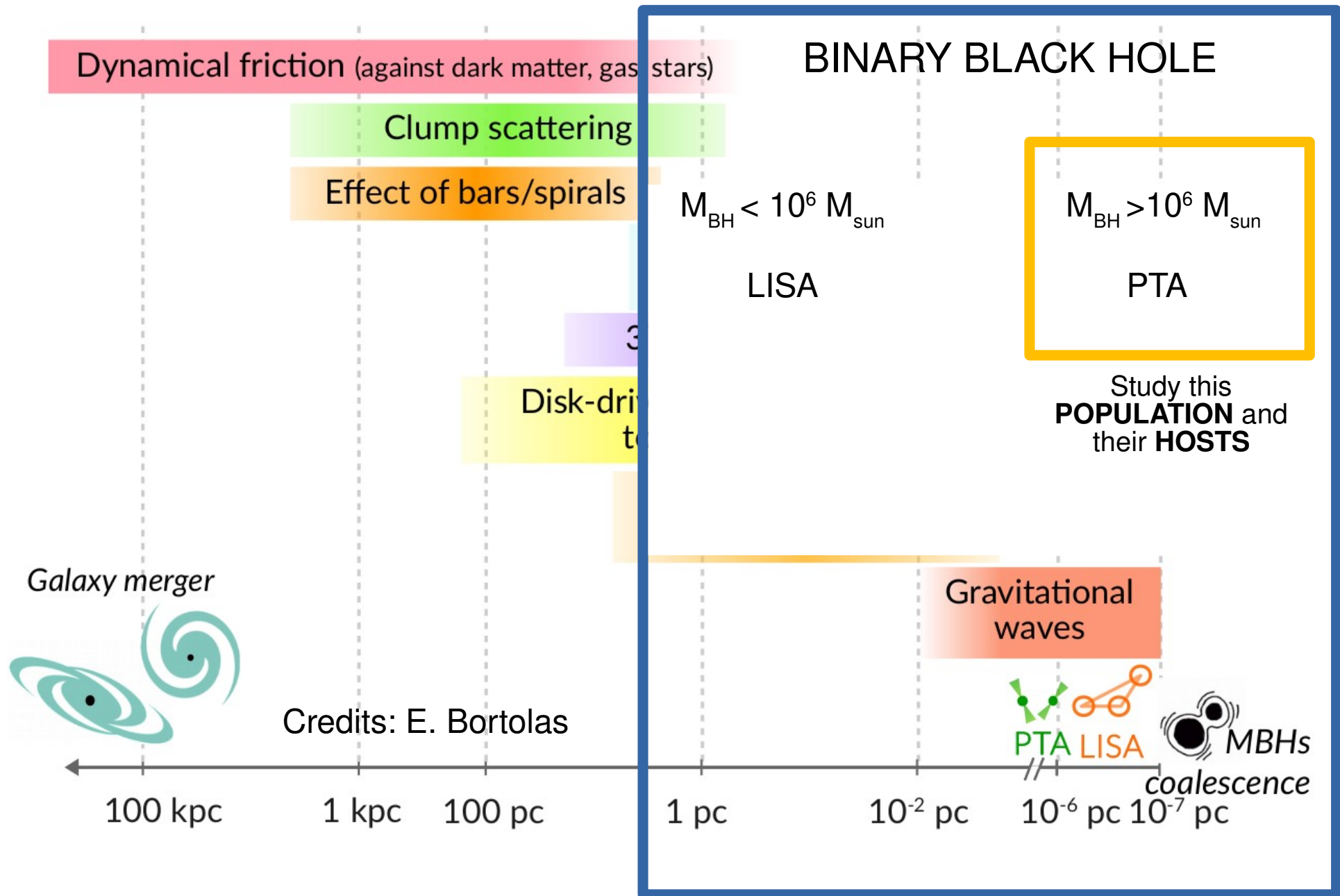




# INTRODUCTION



# INTRODUCTION



# THE MODEL

In order to study the population and hosts of massive binary black holes ( $>10^6 M_{\text{sun}}$ ) we need several ingredients

RELIABLE GALAXY POPULATION

RELIABLE BLACK HOLE POPULATION

MODEL FOR THE BINARY POPULATION



# THE MODEL

In order to study the population and hosts of massive binary black holes ( $>10^6 M_{\text{sun}}$ ) we need several ingredients

RELIABLE GALAXY POPULATION

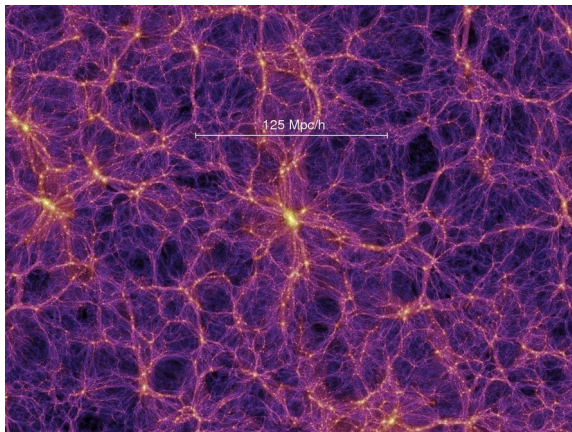
RELIABLE BLACK HOLE POPULATION

MODEL FOR THE BINARY POPULATION

## 1) MILLENNIUM SIMULATION Springel et al. 2005

$$L_{\text{box}} = 500 \text{ Mpc} / h$$

$$M_{\text{halo}} \sim 1.7 \times 10^{10} M_{\text{sun}}$$



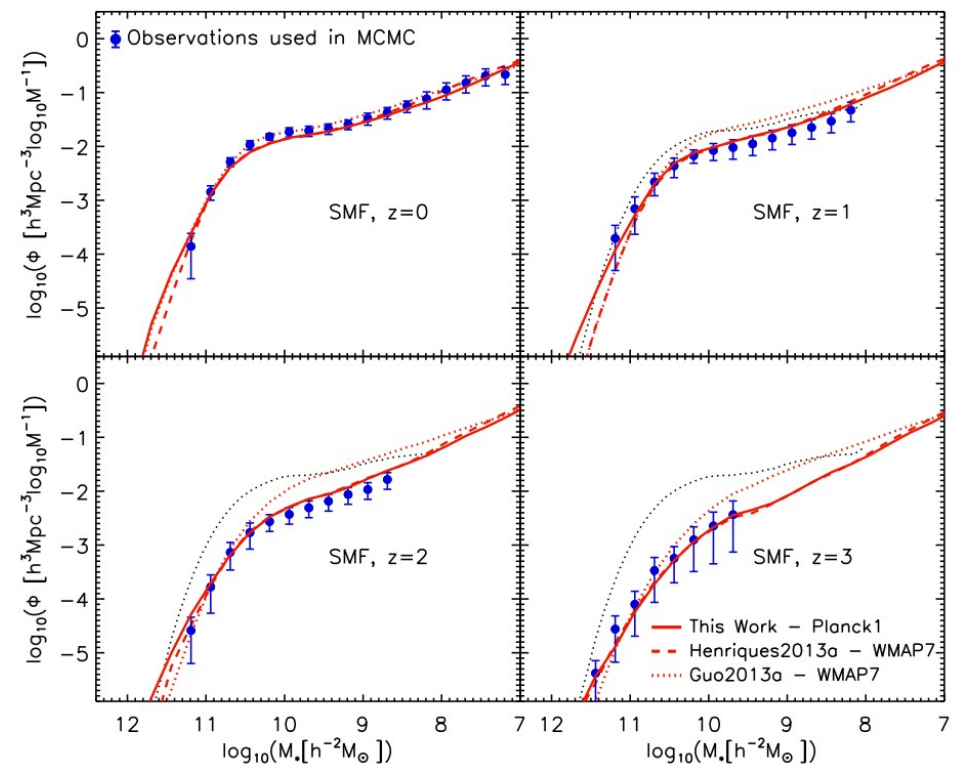
Proof of concept

## 2) SEMI-ANALYTICAL MODEL

L-Galaxies, Munich Galaxy Formation Model

Guo et al. 2011, Henriques et al. 2015

## Evolution of the STELLAR MASS FUNCTION



Henriques et al. 2015

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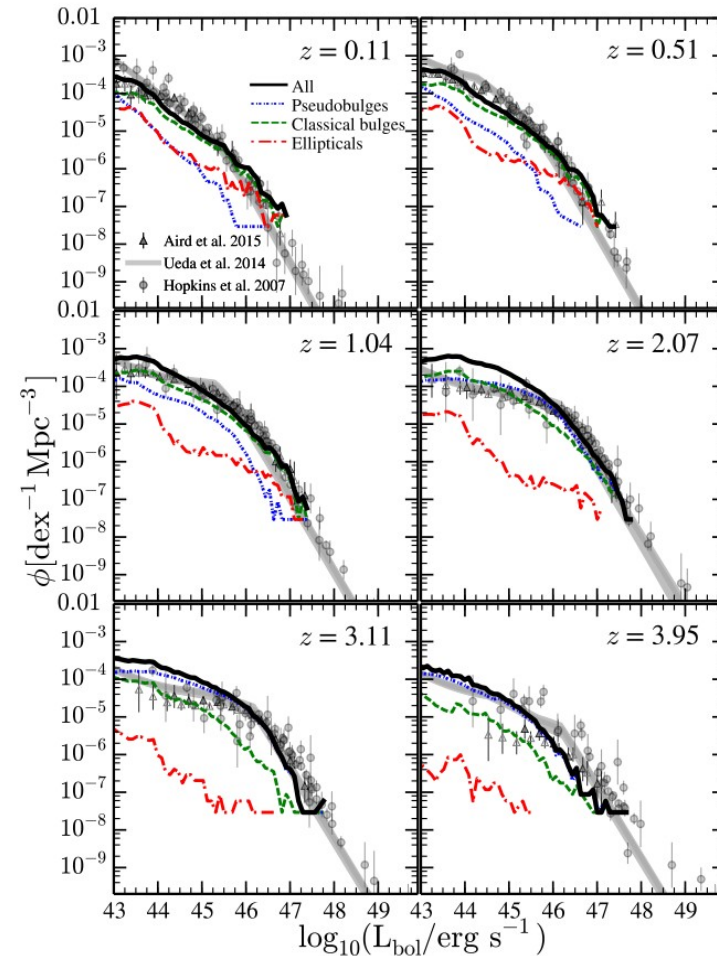
## 1) MILLENNIUM SIMULATION

## 2) SEMI-ANALYTICAL MODEL

- Growth  $\rightarrow$  Mergers & Disk instabilities
- Spin evolution  $\rightarrow$  Link with the bulge formation and evolution
- Recoil velocities
- Wandering black holes

Izquierdo-Villalba et al. 2020

Evolution of the *QUASAR BOLOMETRIC LUMINOSITY FUNCTION*



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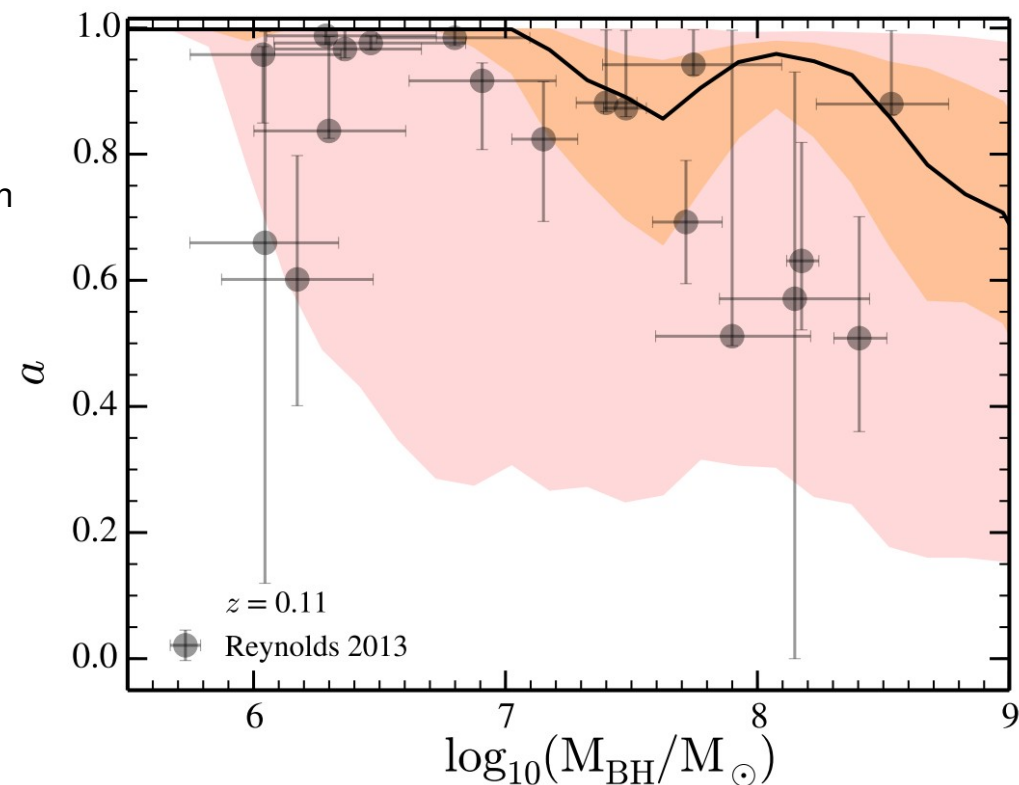
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[Izquierdo-Villalba et al. 2020](#)

SPIN PARAMETER AT  $z = 0$



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- 
- Dynamical friction phase
  - Hardening phase

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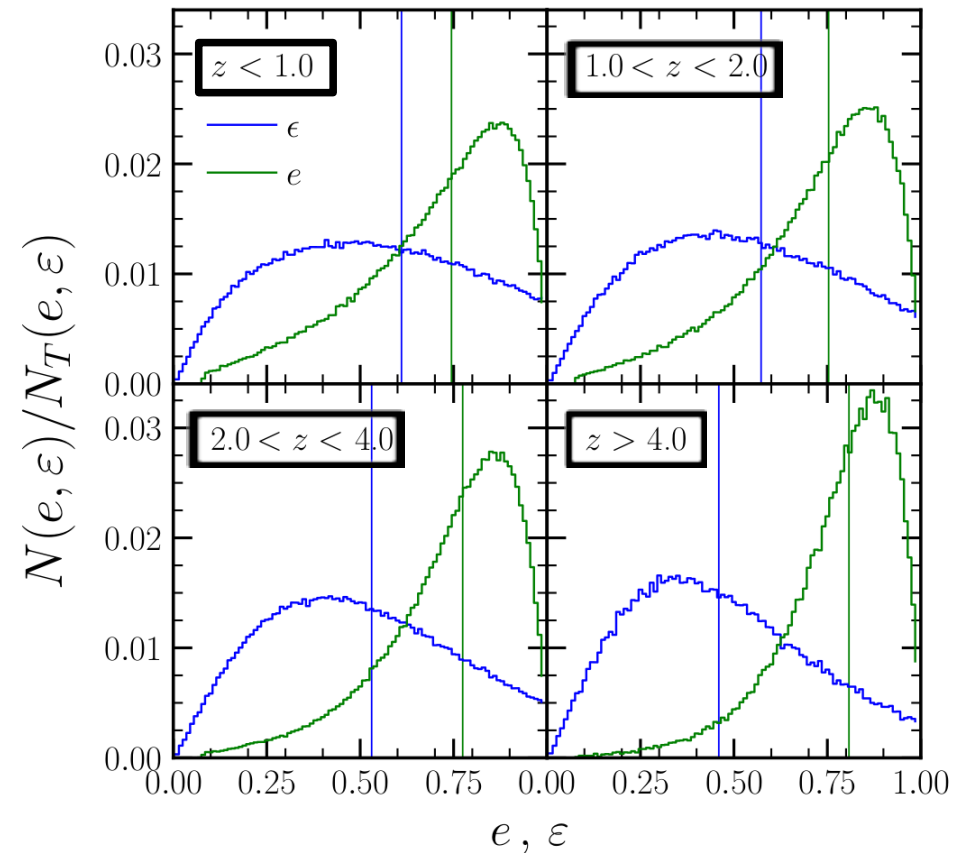
MODEL FOR THE BINARY POPULATION

- Dynamical friction phase

$$t_{\text{dyn}}^{\text{BH}} = 19 f(\epsilon) \left( \frac{r_0}{4 \text{ kpc}} \right)^2 \left( \frac{\sigma}{200 \text{ km/s}} \right) \left( \frac{10^8 M_{\odot}}{M_{\text{BH}}} \right) \frac{1}{\Lambda} [\text{Gyr}]$$

▼ **CIRCULARITY** of the black hole orbit → Computed from the  
 circularity of the **GALAXY ORBIT**

- Hardening phase



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- Dynamical friction phase

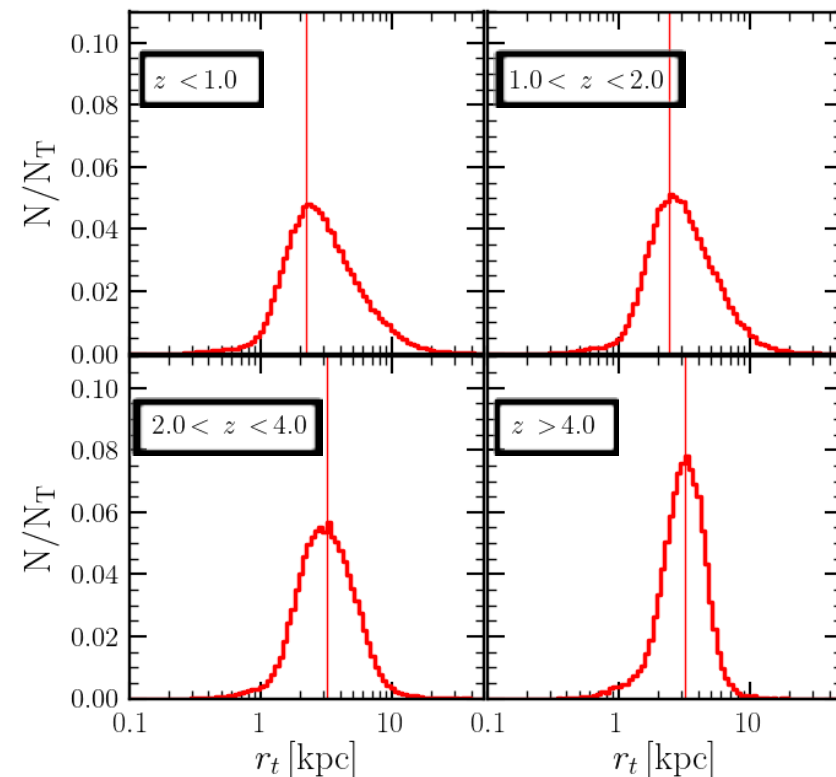
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INITIAL POSITION of the black hole

Computed according to  
the galaxy  
**TIDAL RADIUS**

- Hardening phase

$$r_t = \left( \frac{G M_{\text{sat}}}{\omega^2 - d^2 \Phi / dr^2} \right)^{1/3}$$





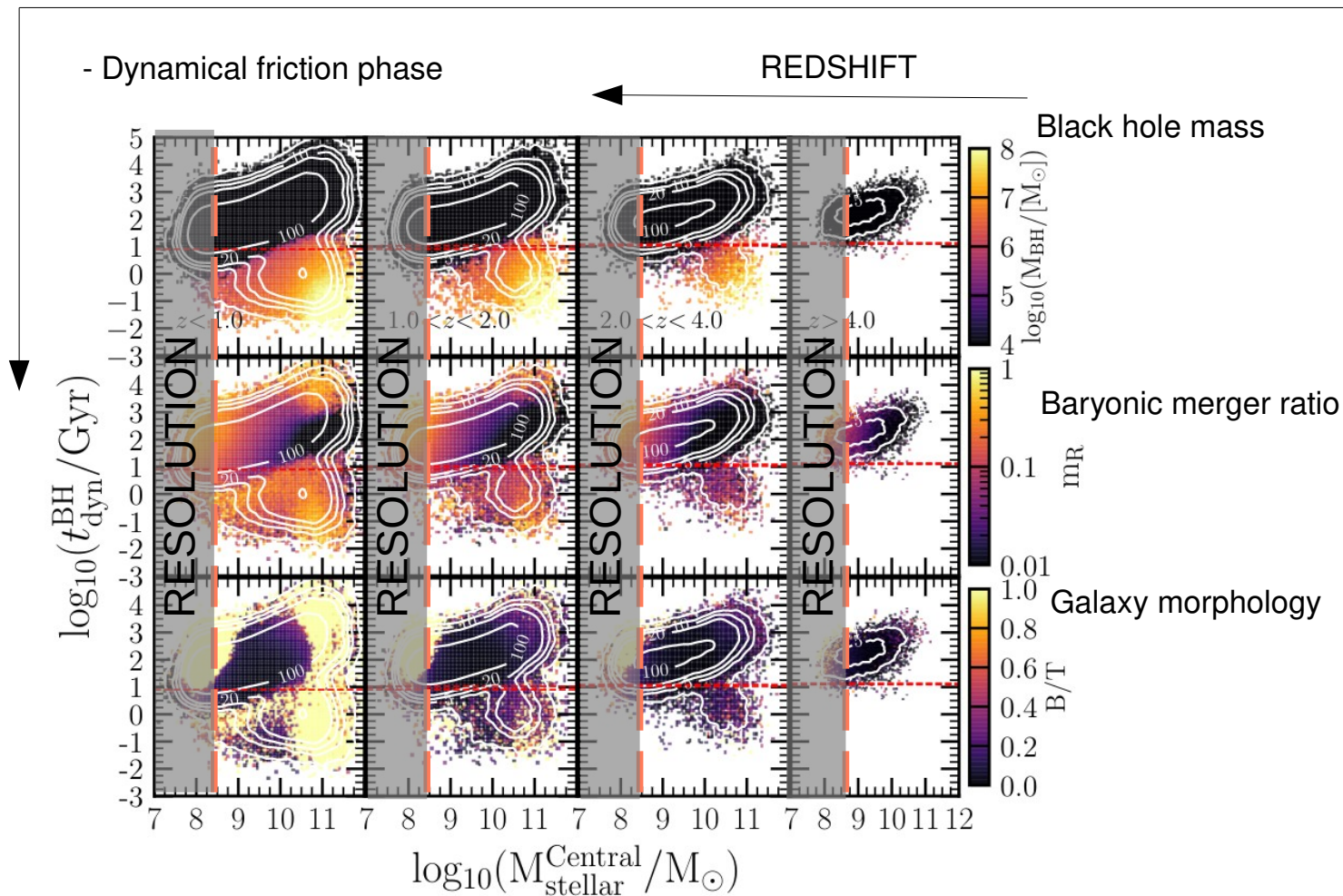
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$t_{\text{dyn}}^{\text{BH}} < t_{\text{H}}$  when:

- Massive black holes ( $>10^6 M_{\text{sun}}$ )
- Large merger ratios
- Typically in elliptical galaxies

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MODEL FOR THE BINARY POPULATION

- Dynamical friction phase

- Hardening phase: We have assumed a **Sérsic model profile**

$$\rho_B(r) = \rho_0 \left( \frac{r}{R_e} \right)^{-p} e^{-b \left( \frac{r}{R_e} \right)^{1/n}}$$

Biava et al. 2019

1) **Gas rich mergers** : Disk torques driven the binary merge

$$t_{\text{delay}} = R_c \frac{G(M_{\text{BH},1} + M_{\text{BH},2})}{\sigma_{\text{inf}}^2}$$

2) **Gas poor mergers** : The stellar background drives the binary merge [Sesana & Khan 2015](#)

$$\frac{da_{\text{BH}}}{dt} = \left( \frac{da_{\text{BH}}}{dt} \right)_{\text{Hard}} + \left( \frac{da_{\text{BH}}}{dt} \right)_{\text{GW}} = - \frac{GH\rho_{\text{inf}}}{\sigma_{\text{inf}}} a_{\text{BH}}^2 - \frac{64G^3(M_{\text{BH},1} + M_{\text{BH},2})^3 F(e)}{5c^5(1+q)^2 a_{\text{BH}}^3}$$

$$\frac{de}{dt} = a_{\text{BH}} \frac{G\rho_{\text{inf}}HK}{\sigma_{\text{inf}}} - \frac{304}{15} \frac{G^3 q (M_{\text{BH},1} + M_{\text{BH},2})^3}{c^5(1+q)^2 a_{\text{BH}}^4 (1-e^2)^{5/2}} \left( e + \frac{121}{304} e^3 \right)$$

a) The initial eccentricity is assumed to be random between [0,1]

b) The initial separation is computed as  $\tilde{M}_{\text{Bulge}}(<a_0) = 2M_{\text{BH},2}$

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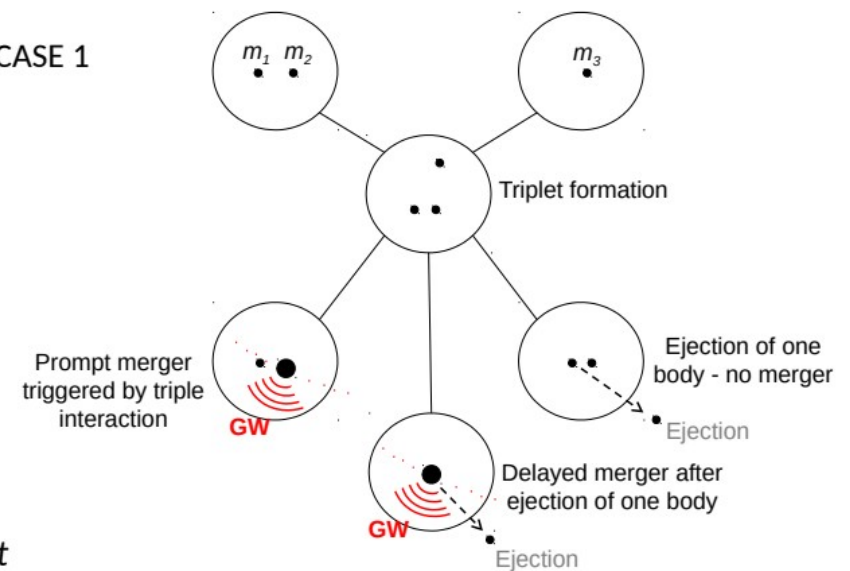
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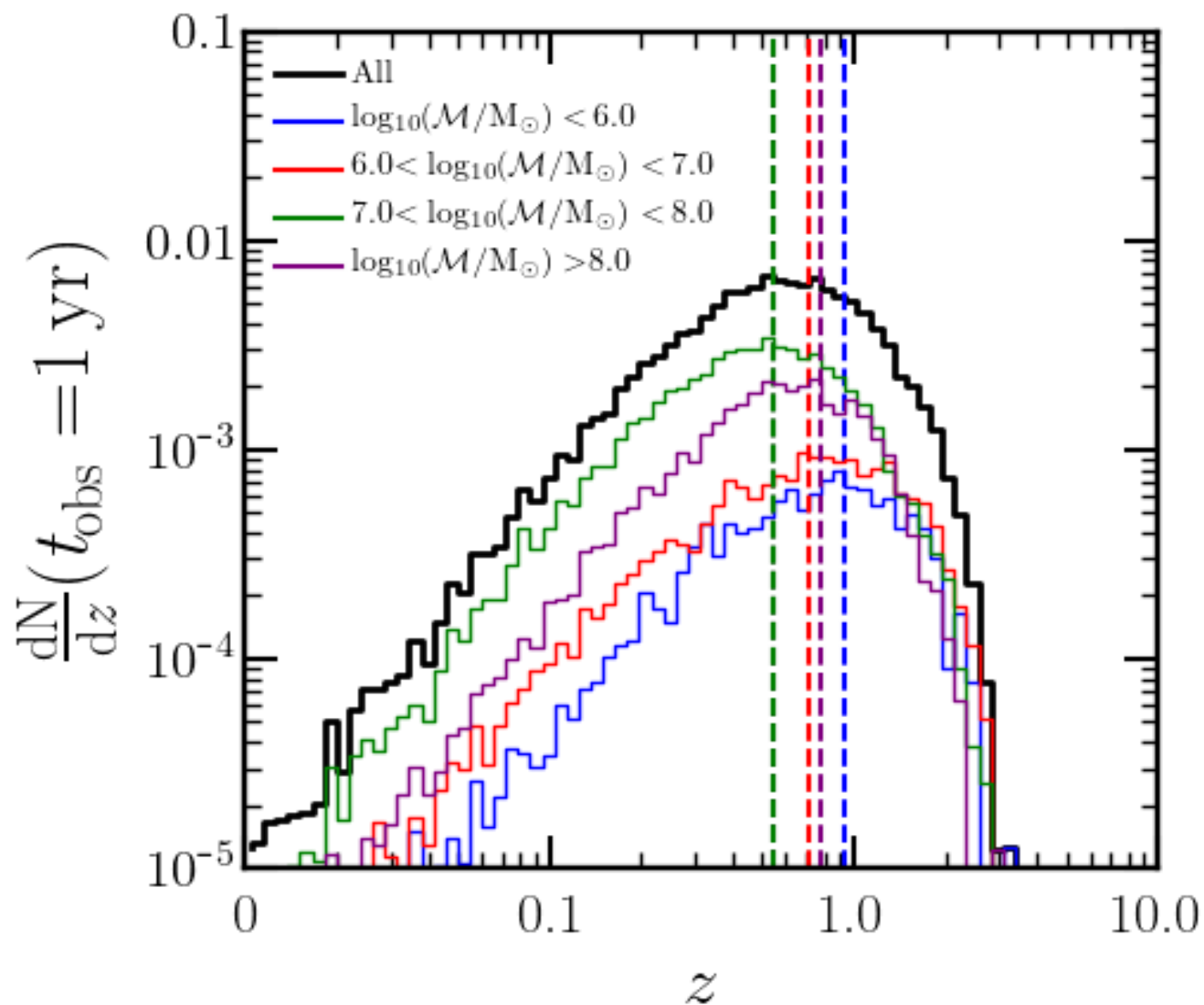
- Dynamical friction phase
- Hardening phase
- Merger caused by intruder massive black hole ([Bonetti et al. 2018](#))

CASE 1



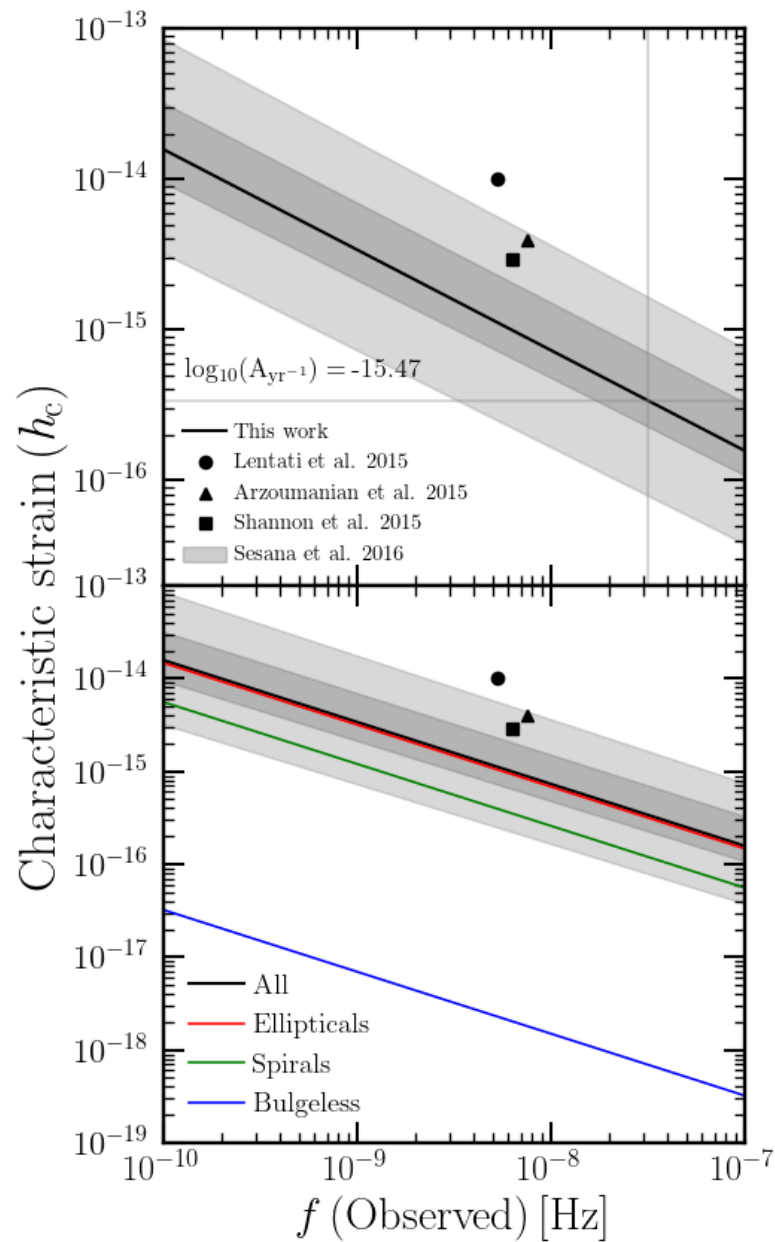
# RESULTS

## MERGER RATE



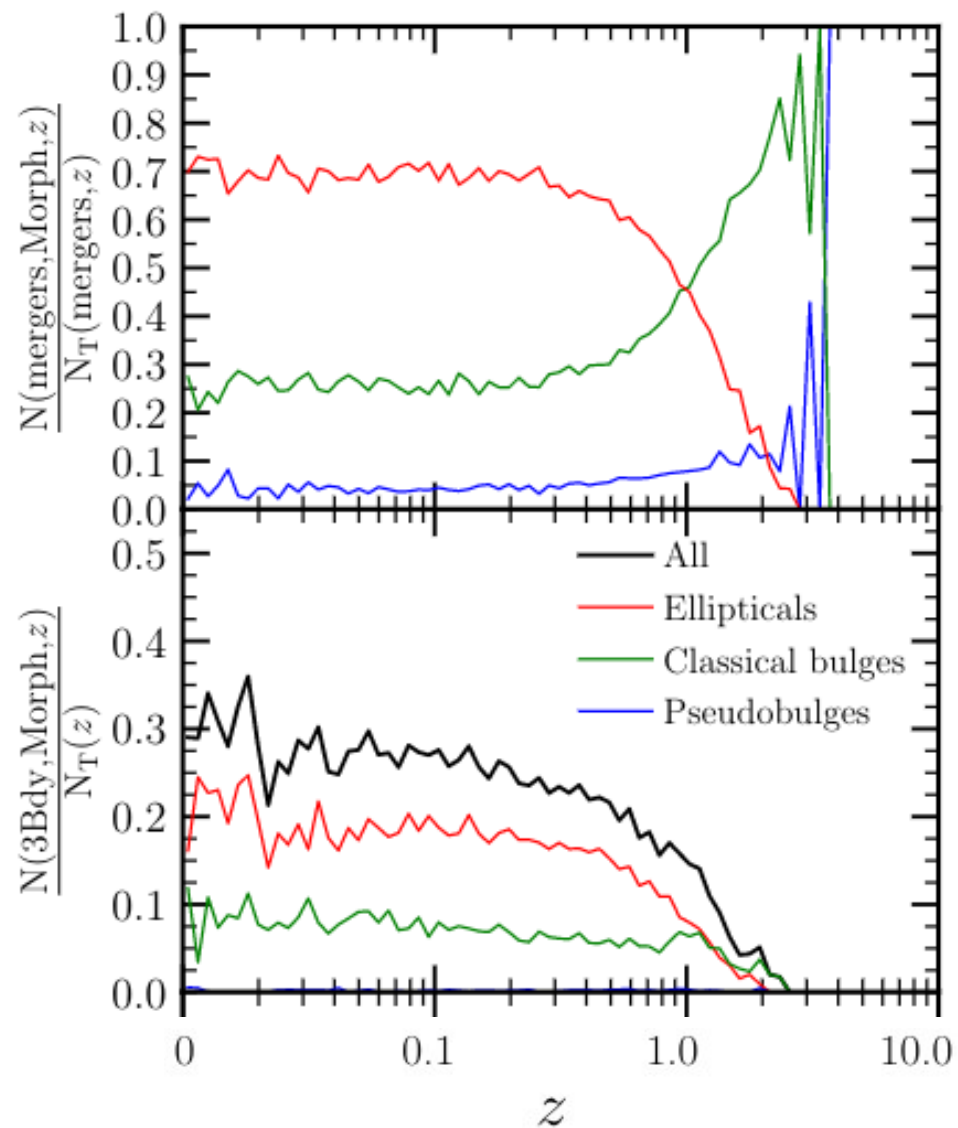
# RESULTS

## AMPLITUDE OF THE GRAVITATIONAL WAVE BACKGROUND IN THE PTA BAND



# RESULTS

## PROPERTIES OF THE GALAXIES HOSTING MERGING MASSIVE BLACK HOLES





# CONCLUSIONS

- \* We have tackled the formation and evolution of massive black hole binaries ( $>10^6 M_{\text{sun}}$ ) in the PTA band
  - Dark matter merger trees from N-body simulations
  - Semi-analytical model
  - Proper treatment of the growth and spin evolution
  
- \* For galaxies  $M_{\text{stellar}} > 10^9 M_{\text{sun}}$  only black holes  $>10^6 M_{\text{sun}}$  can reach the nucleus of its central galaxy
  - After baryonic merger with merger ratios  $> 0.1$
  - Seems to have a correlation between the wandering time and the galaxy morphology
  
- \* The merger rate of binary black holes of  $>10^6 M_{\text{sun}}$  is quite low  $< 0.01$  event per year
  
- \* The amplitude of the gravitational wave background at nHz is consistent with the expectations AND most of the signal comes from binary black holes merging in elliptical galaxies
  
- \* The encounter with an intruder black hole lead to the final coalescence of the
  - ~30% of binary black holes in elliptical galaxies
  - ~10% of binary black holes in spiral galaxies hosting a classical bulge
  - ~0% of binary black holes in spiral galaxies hosting a pseudobulge

# THANKS

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