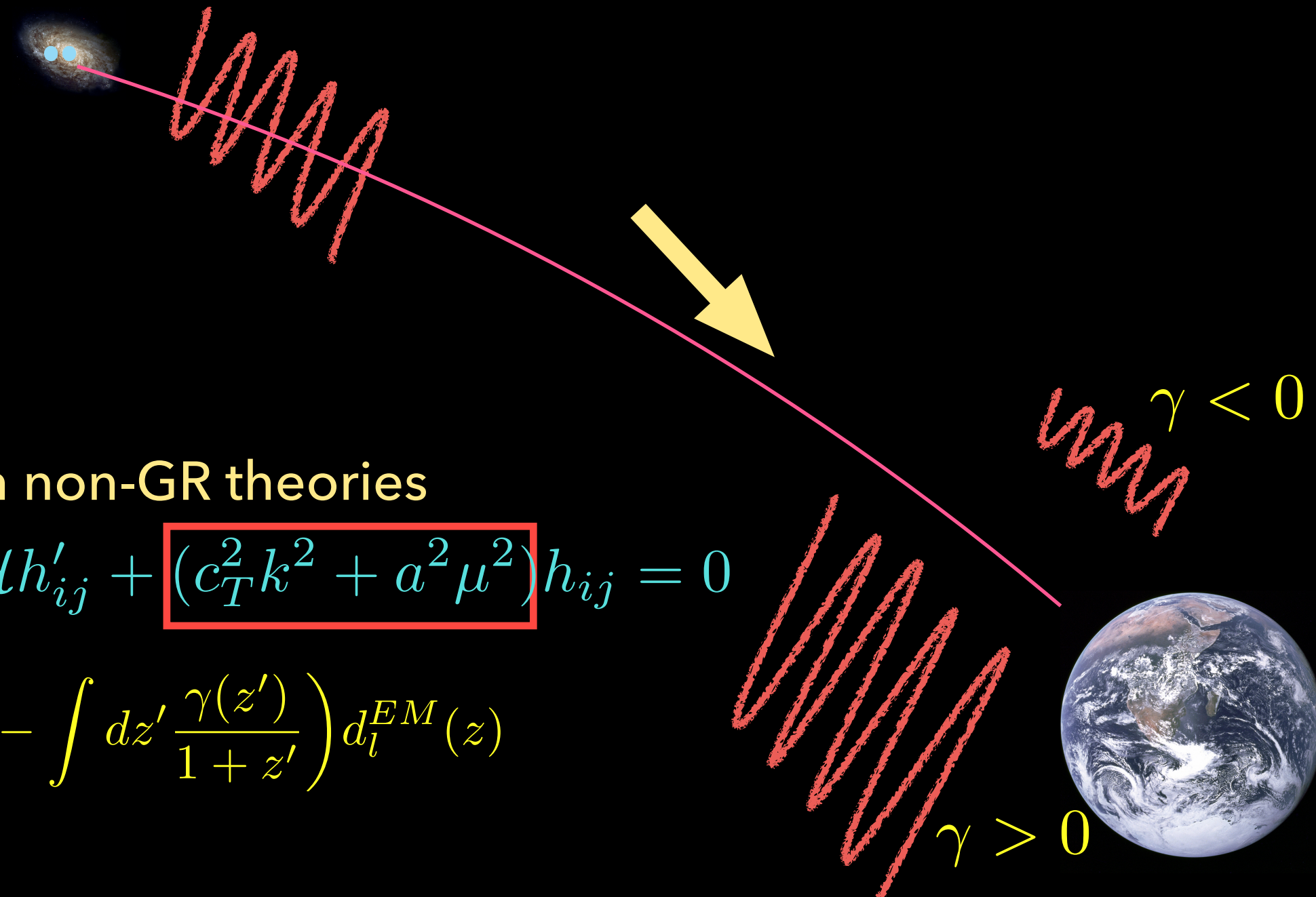


SUVODIP MUKHERJEE

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# COSMOLOGY WITH DARK GRAVITATIONAL WAVE SOURCES

# GW PROPAGATION THROUGH SPACE-TIME IS A PROBE TO COSMIC EXPANSION HISTORY AND FUNDAMENTAL PHYSICS



GW propagation in non-GR theories

$$h''_{ij} + 2(1 - \gamma(z))\mathcal{H}h'_{ij} + (c_T^2 k^2 + a^2 \mu^2)h_{ij} = 0$$

$$d_l^{GW}(z) = \exp\left(-\int dz' \frac{\gamma(z')}{1+z'}\right) d_l^{EM}(z)$$

$\gamma < 0$

$\gamma > 0$



# EM-GW PROBES TO MEASURE THE PROPAGATION OF GW

$$\boxed{d_l^{GW}(z)} = \exp \left( - \int dz' \frac{\boxed{\gamma(z')}}{1+z'} \right) \boxed{d_l^{EM}(z)}$$

From GW data

Unknown

Unknown

COSMOLOGY DEPENDENT

For dark sirens:  $z$  is unknown

From sources with EM counterparts: we can only probe **low** redshift with LVK detector network

From sources without EM counterparts: we can probe **high** redshift with LVK detector network

# GETTING AN INDEPENDENT MEASURE OF THE EM LUMINOSITY DISTANCE

Sound horizon at the drag epoch

$$\theta_{BAO}(z) = \frac{r_s}{(1+z)d_A(z)}$$

Angular diameter distance

$$d_A(z) = d_l^{EM}(z)/(1+z)^2$$

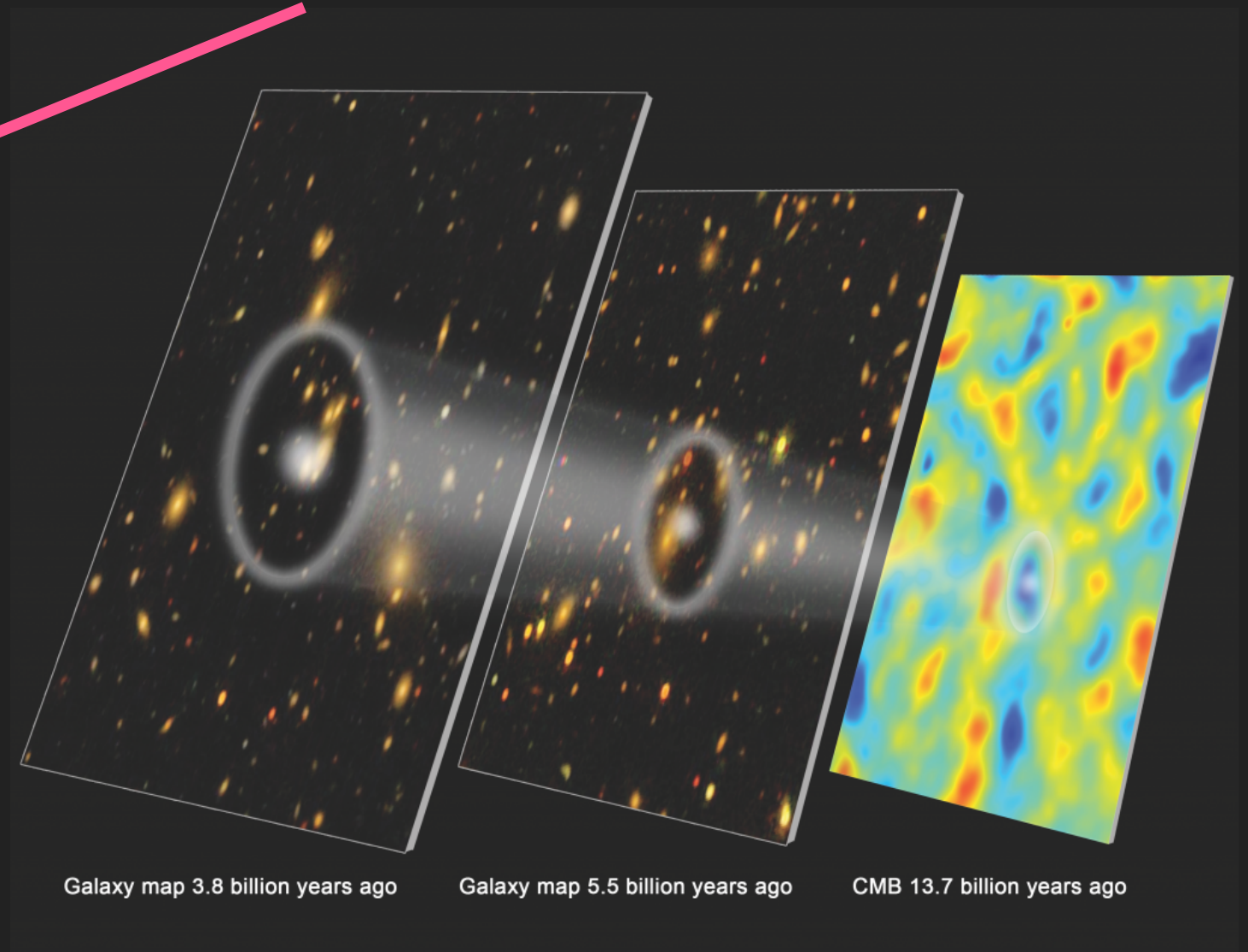


Image credit: ESA



# DATA DRIVEN TEST OF GENERAL RELATIVITY BY COMPARING THREE SCALES

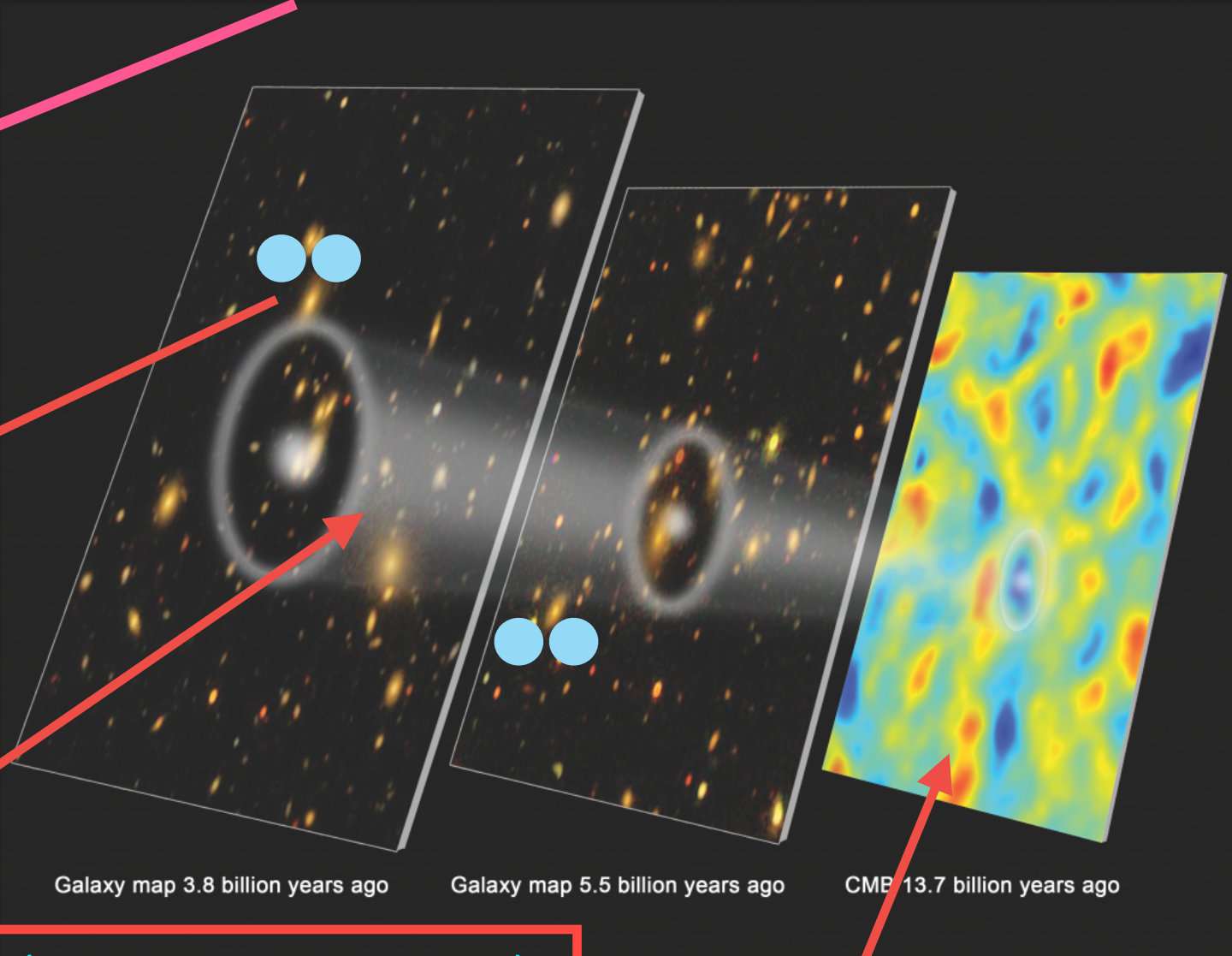
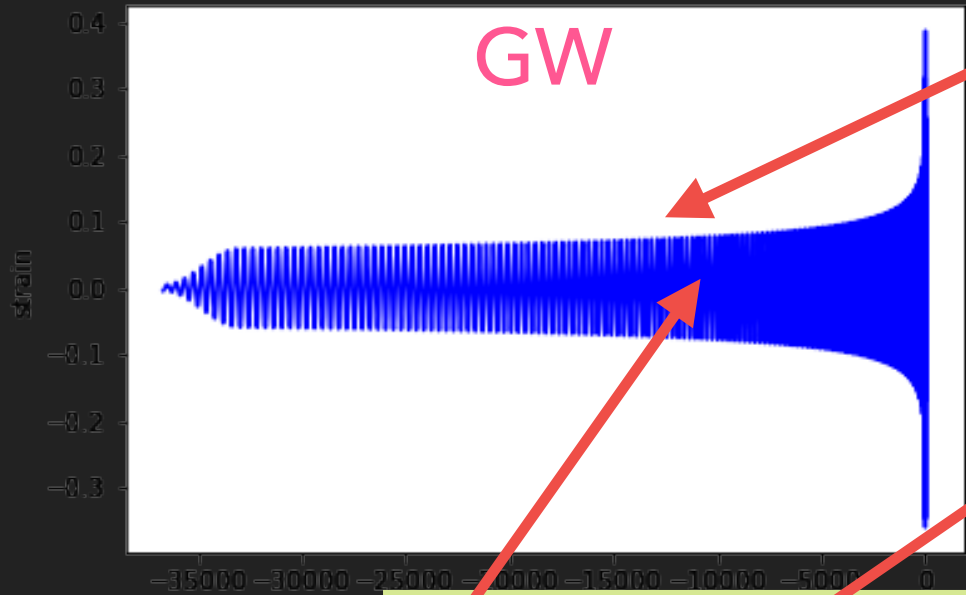
Sound horizon at the drag epoch

Mukherjee, Wandelt, Silk (*MNRAS*, 502,1136, 2021)

Angular diameter distance

$$\theta_{BAO}(z) = \frac{r_s}{(1+z)d_A(z)}$$

$$d_A(z) = d_l^{EM}(z)/(1+z)^2$$



$$d_l^{GW}(z)\theta_{BAO}(z) = \left( \Xi_0 + \frac{1 - \Xi_0}{(1+z)^n} \right) (1+z)r_s$$

# HOW TO MEASURE THE REDSHIFT OF GW SOURCES

- ▶ **\*Only\*** GW signal cannot provide the redshift to the source in the absence of a known mass scale.

48 Binary Black holes  
( $< 1000 M_{\text{sun}}$ ) **Unlikely\***

? Black hole- Neutron  
stars **Likely**

- ▶ Every GW sources will not have electromagnetic counterpart. So, redshift cannot be estimated independently.

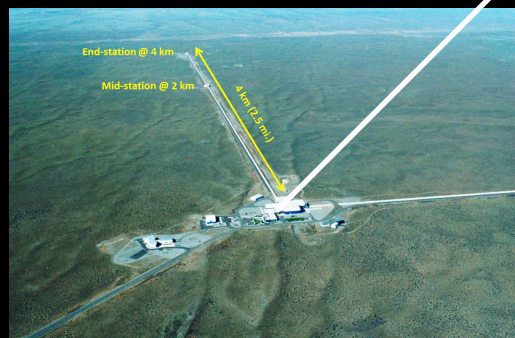
1 Binary Neutron stars **Likely**

Super Massive Binary  
Black holes **Likely**

\* Unless there are presence of baryons in the BBH surroundings

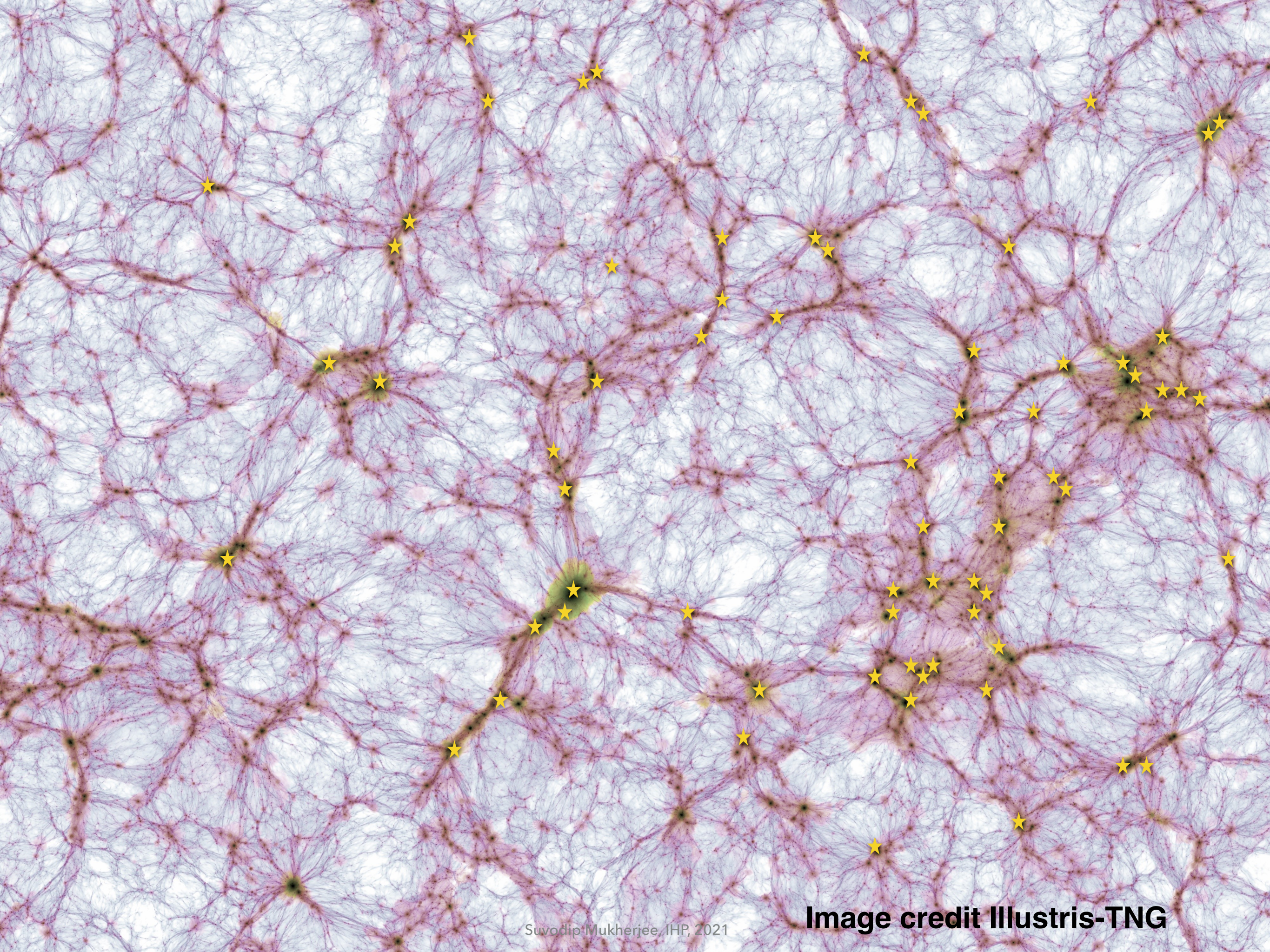
# HOW BLACK HOLES ARE GOING TO BE DISTRIBUTED ?

Luminosity  
Distance



GW binaries (dark sirens)

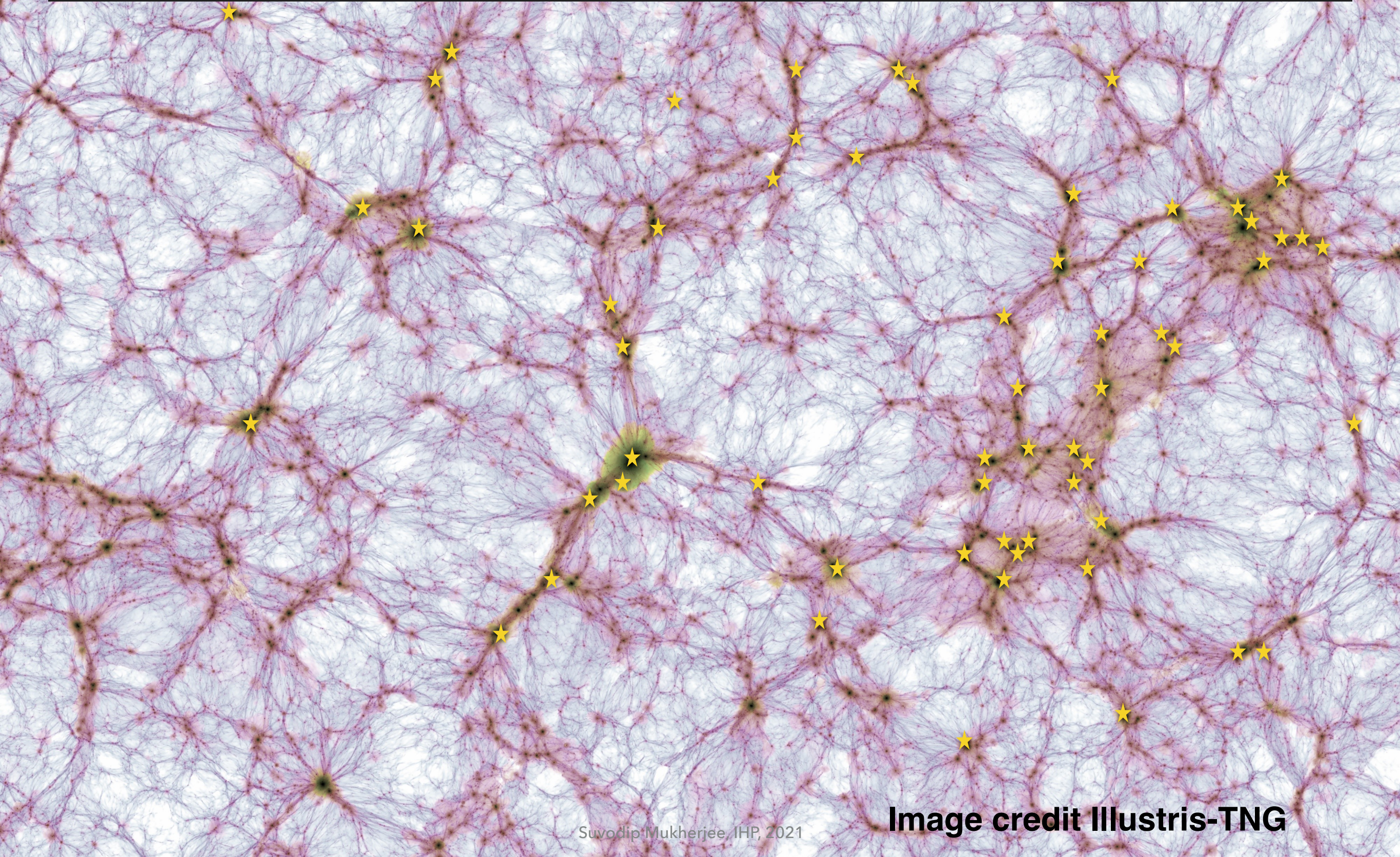






# How GW sources trace the Dark Matter distribution

$$b(z) = b_{GW}(1+z)^{\alpha}$$





A visualization of the cosmic web, showing a dense network of dark red filaments and nodes against a dark blue background. Numerous yellow stars are scattered throughout the network, representing galaxies. A small inset image in the upper right corner shows a zoomed-in view of a galaxy cluster.

Let us concentrate on a single dark siren★

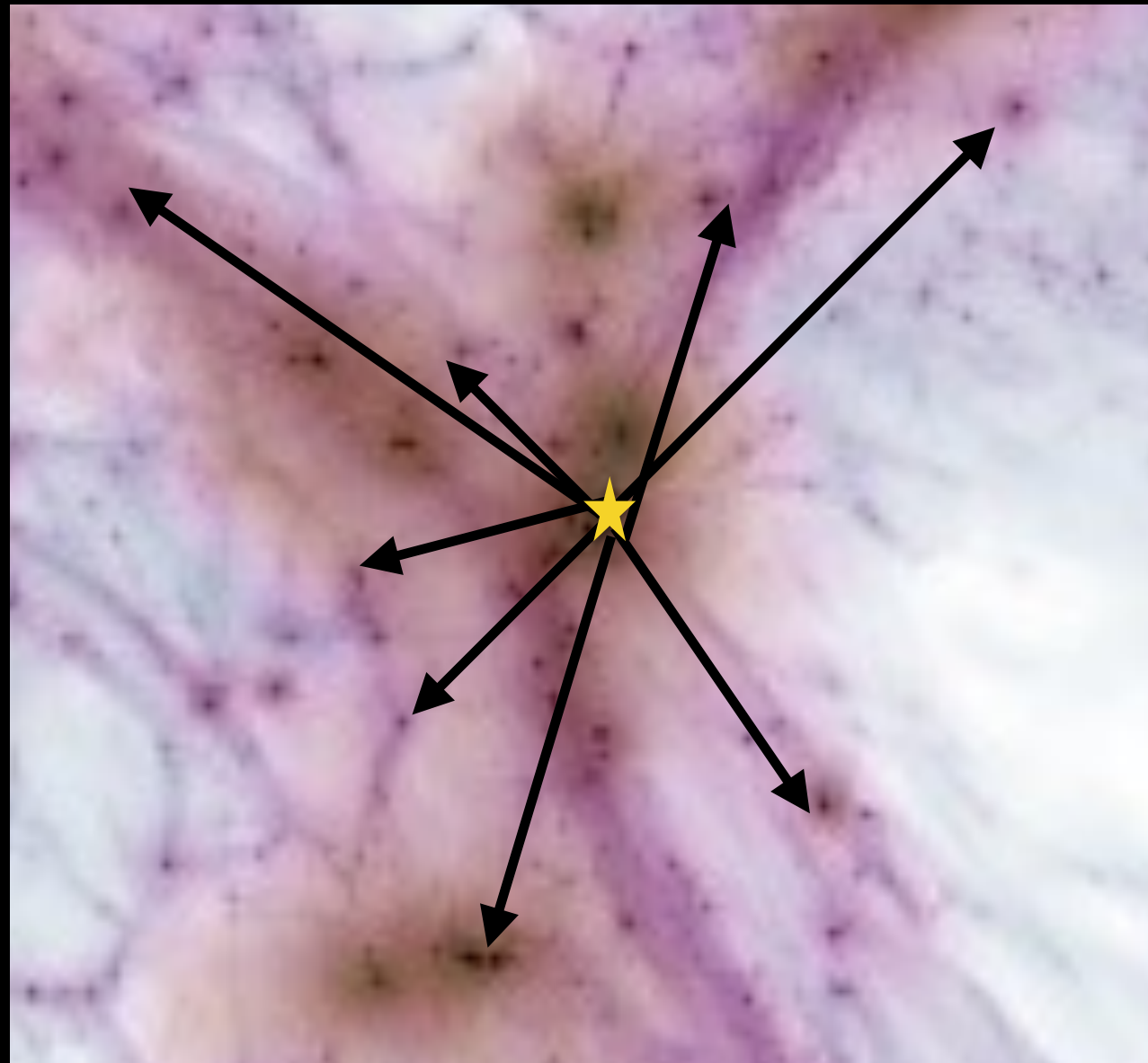


# Three-dimensional spatial clustering with galaxies can be used to measure the redshift of the GW source

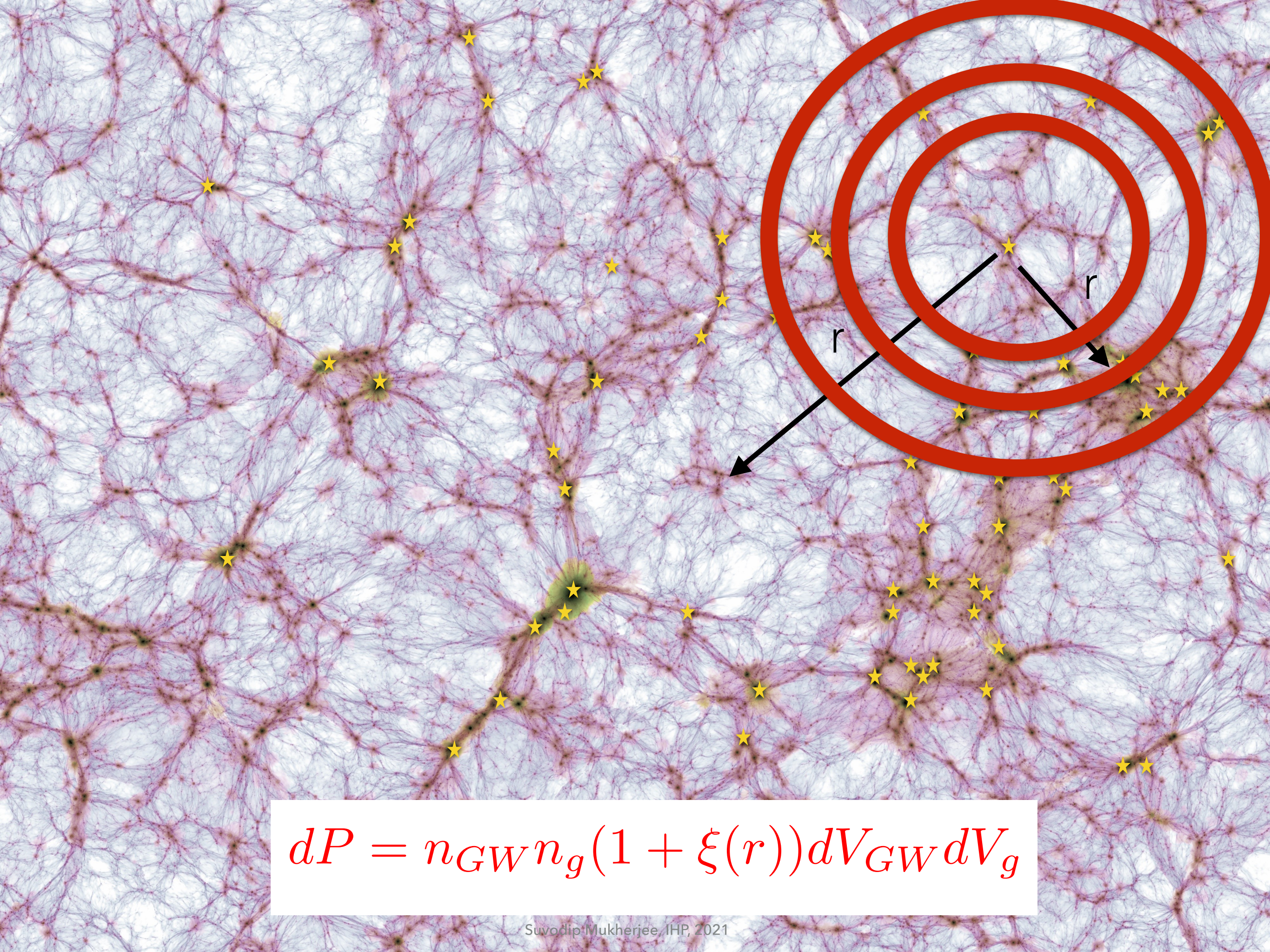
Mukherjee, Wandelt (2018)

Mukherjee, Wandelt, Silk (2020)

Mukherjee, Wandelt, Nissanke, Silvestri (2021)







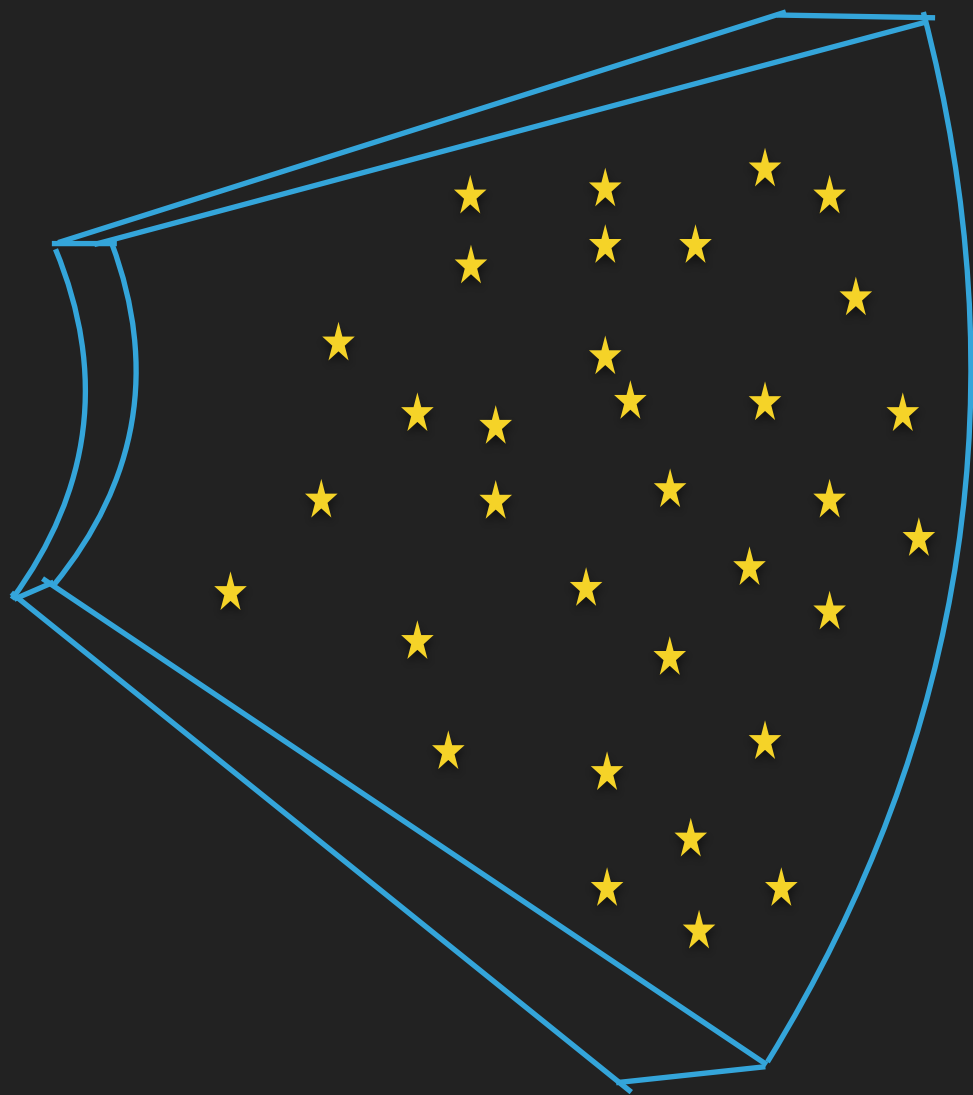
$$dP = n_{GW} n_g (1 + \xi(r)) dV_{GW} dV_g$$



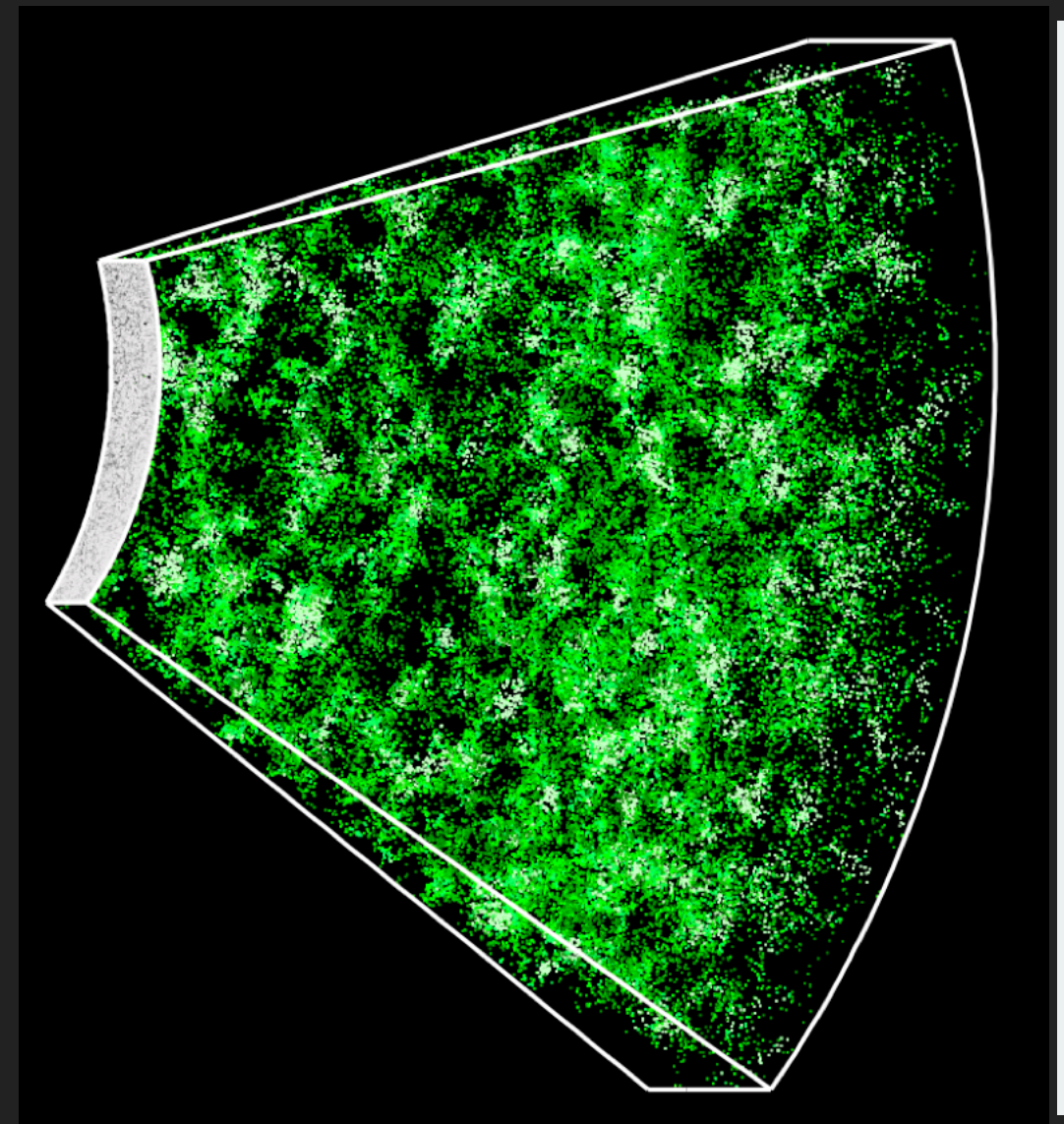
# CROSS-CORRELATION OF GW SOURCES WITH GALAXIES

Mukherjee et al. (2007.02943)

$$dP = n_{GW} n_g (1 + \xi(r)) dV_{GW} dV_g$$



Dark sirens observed in luminosity distance space



Galaxy samples observed in redshift space

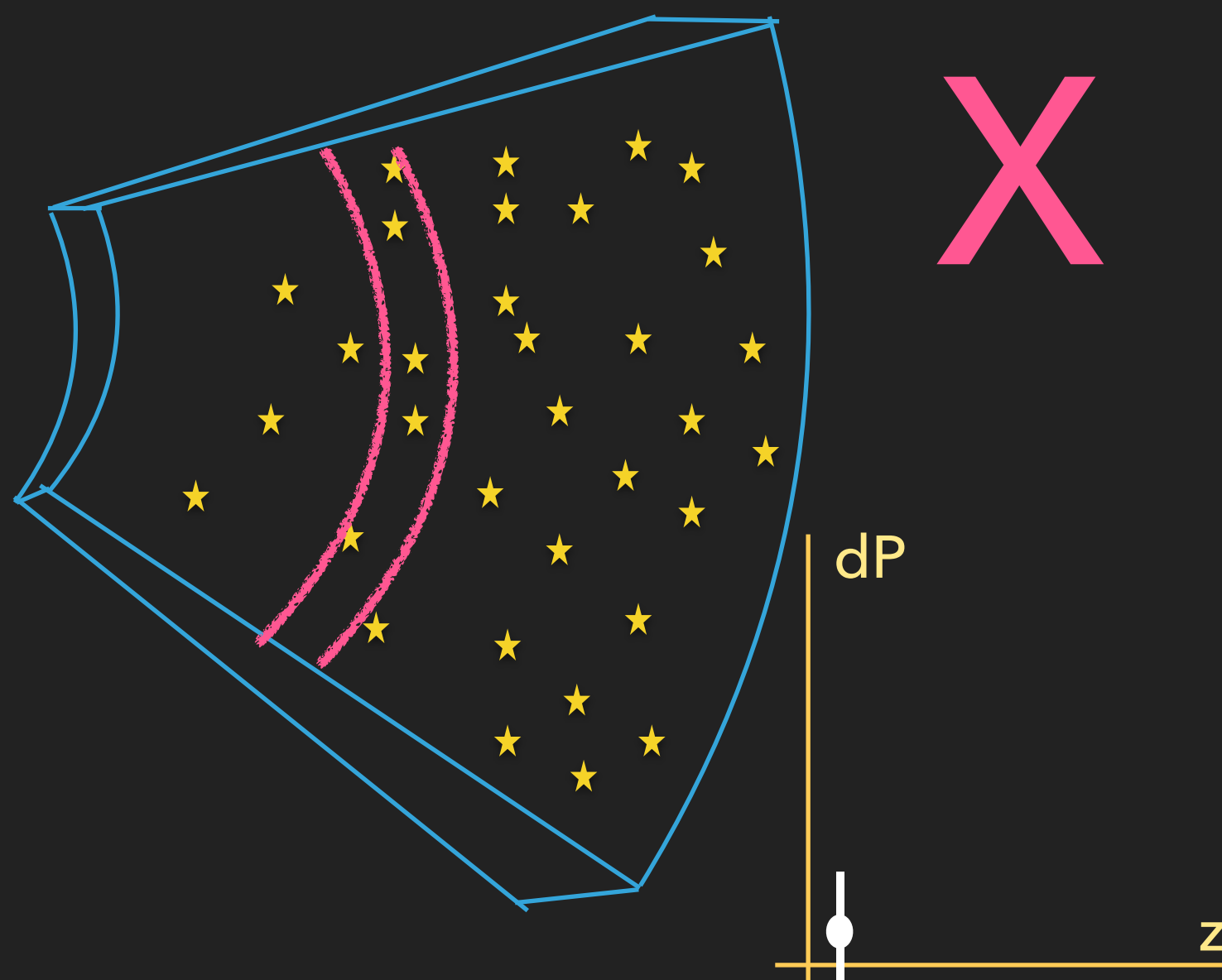
Image credit: Jeremy Tinker and the SDSS-III collaboration



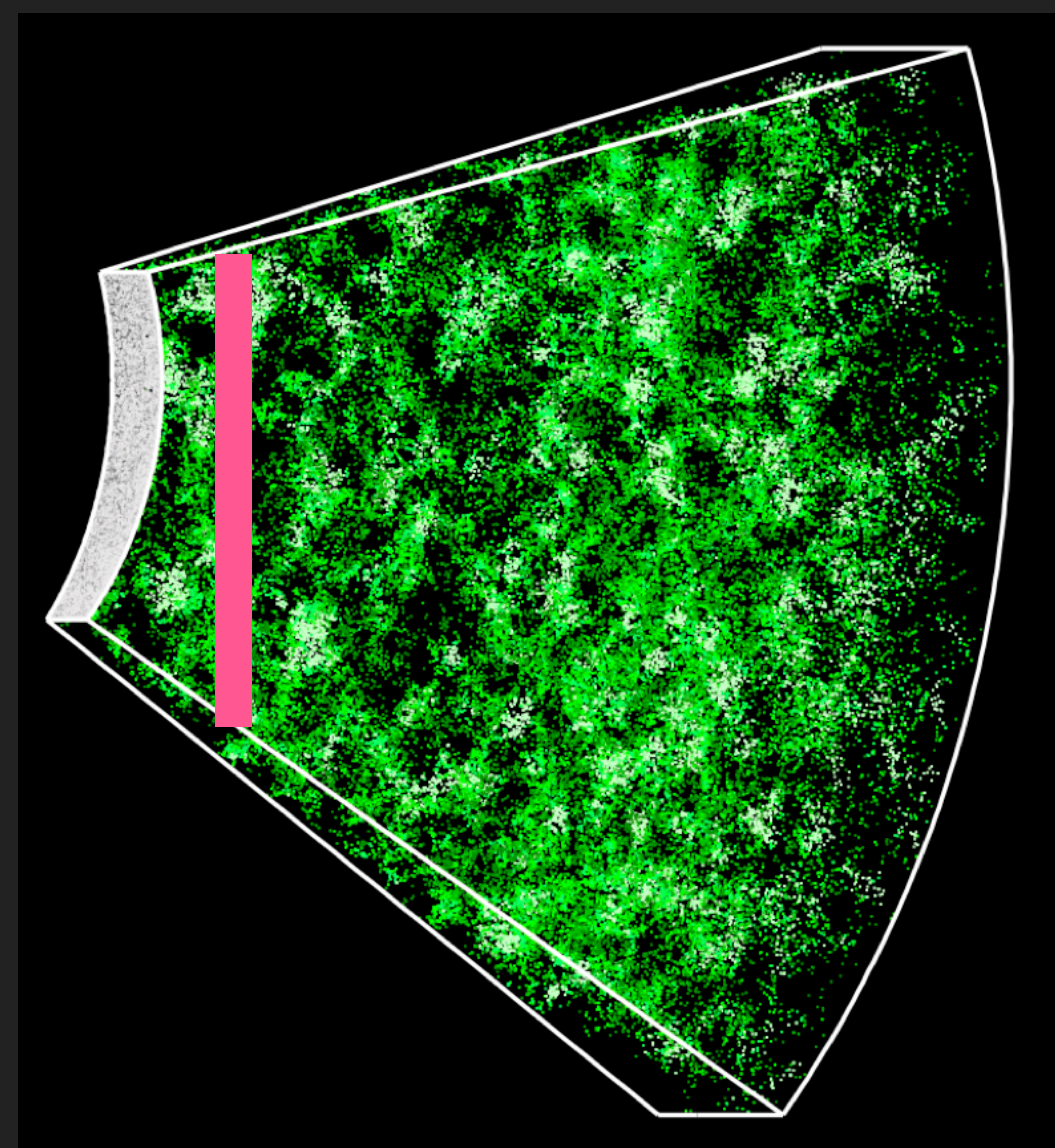
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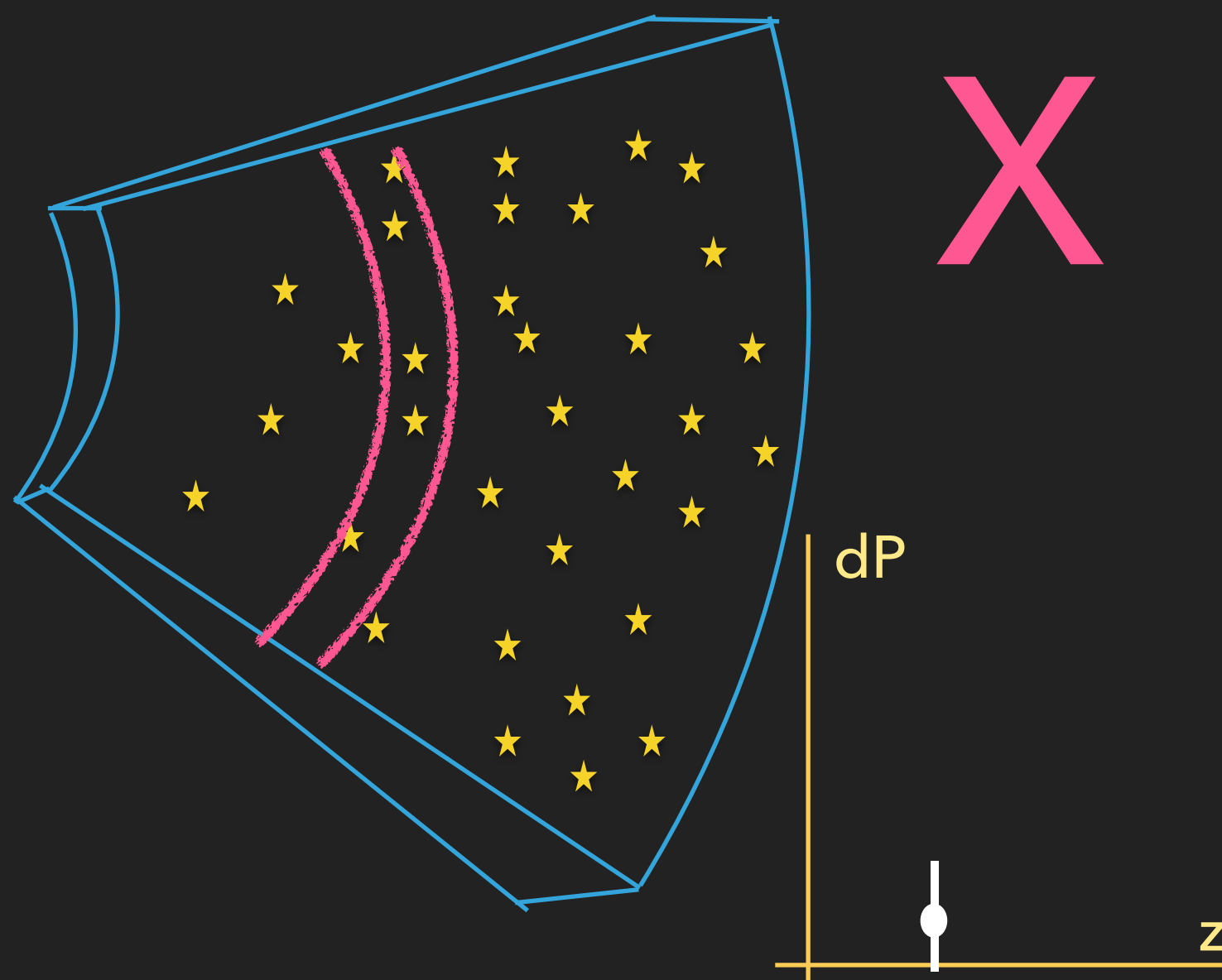
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X

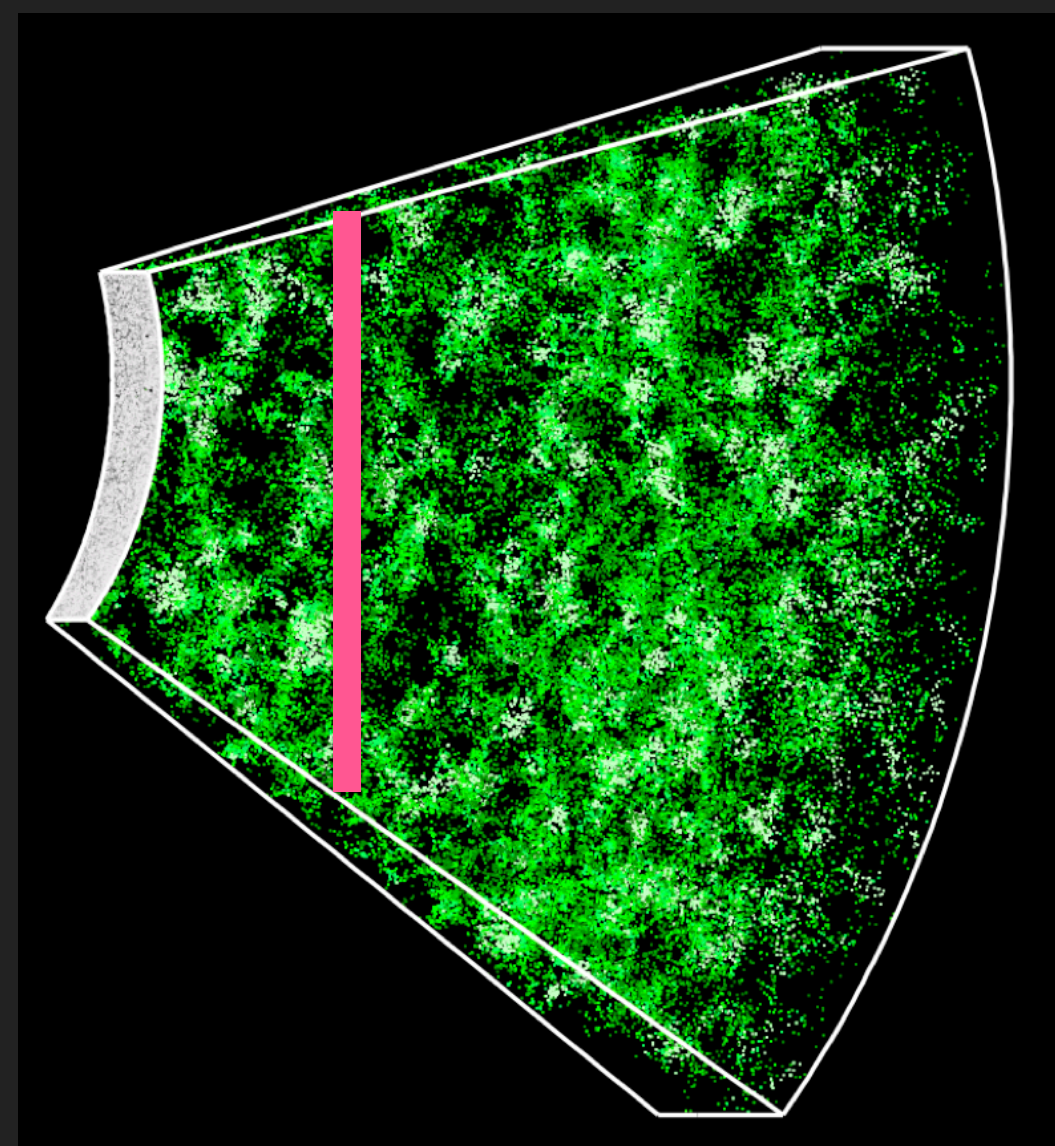


Image credit: Jeremy Tinker and the SDSS-III collaboration

Dark sirens observed in luminosity distance space

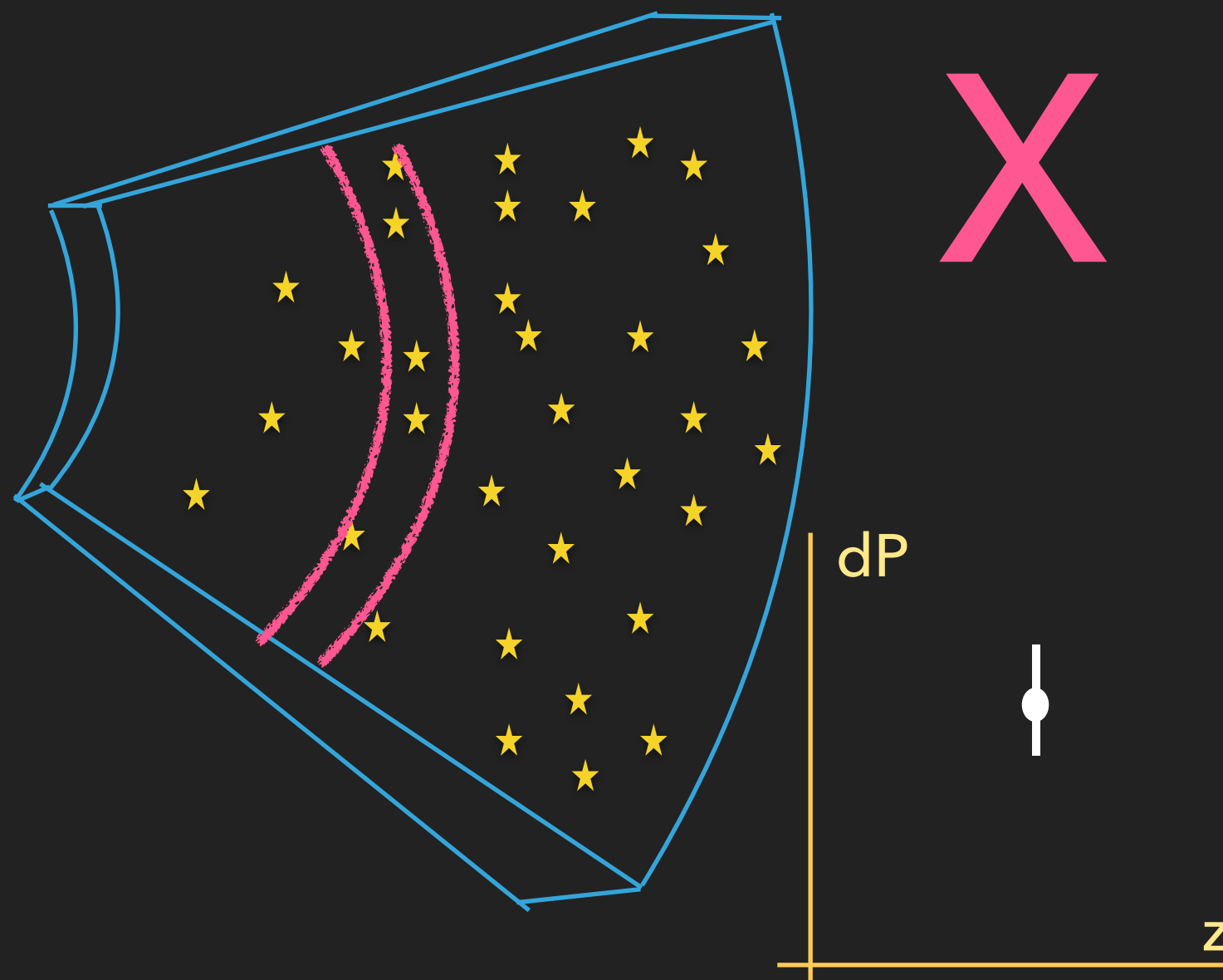
Galaxy samples observed in redshift space



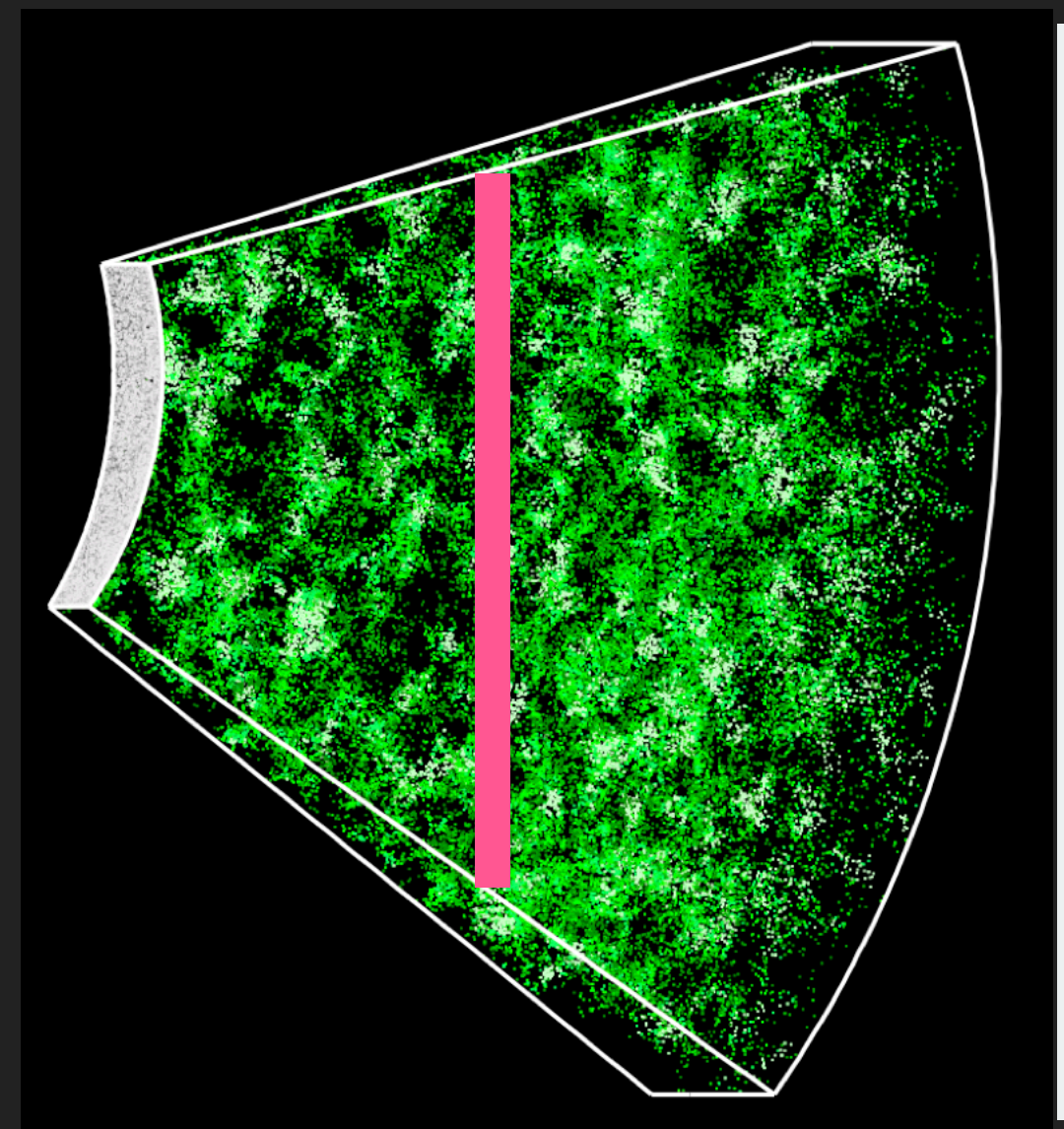
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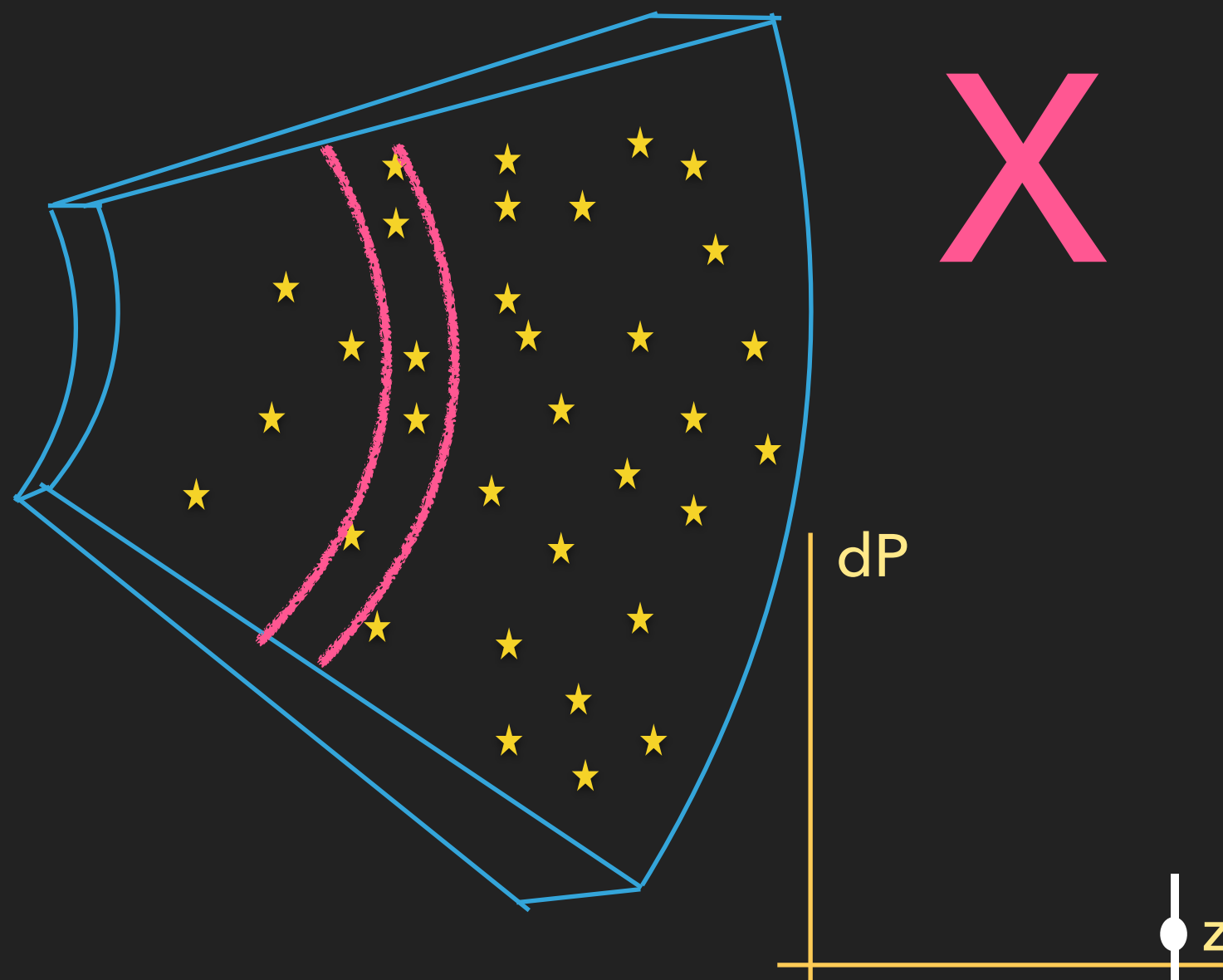
Image credit: Jeremy Tinker and the SDSS-III collaboration



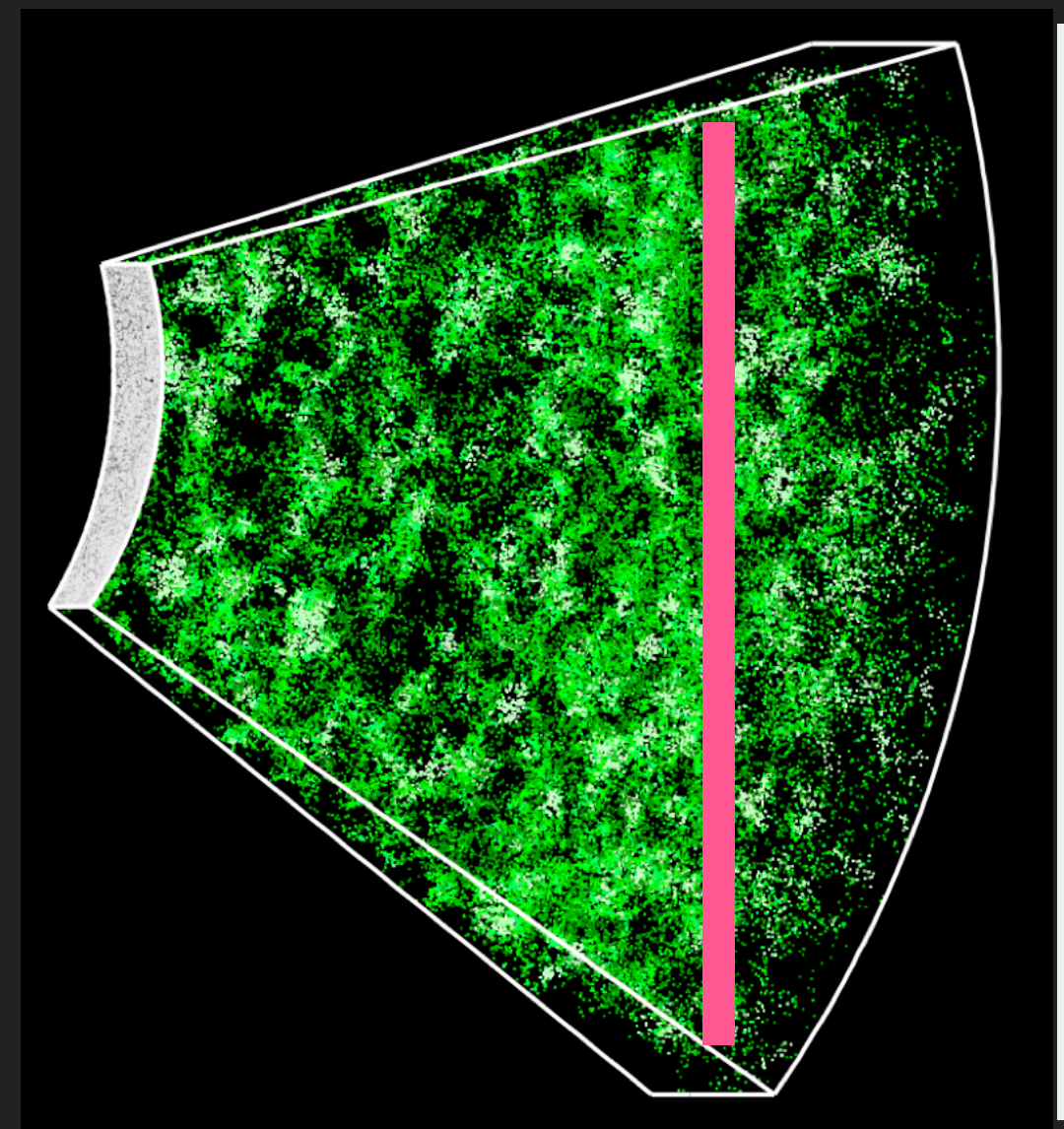
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Dark sirens observed in luminosity distance space



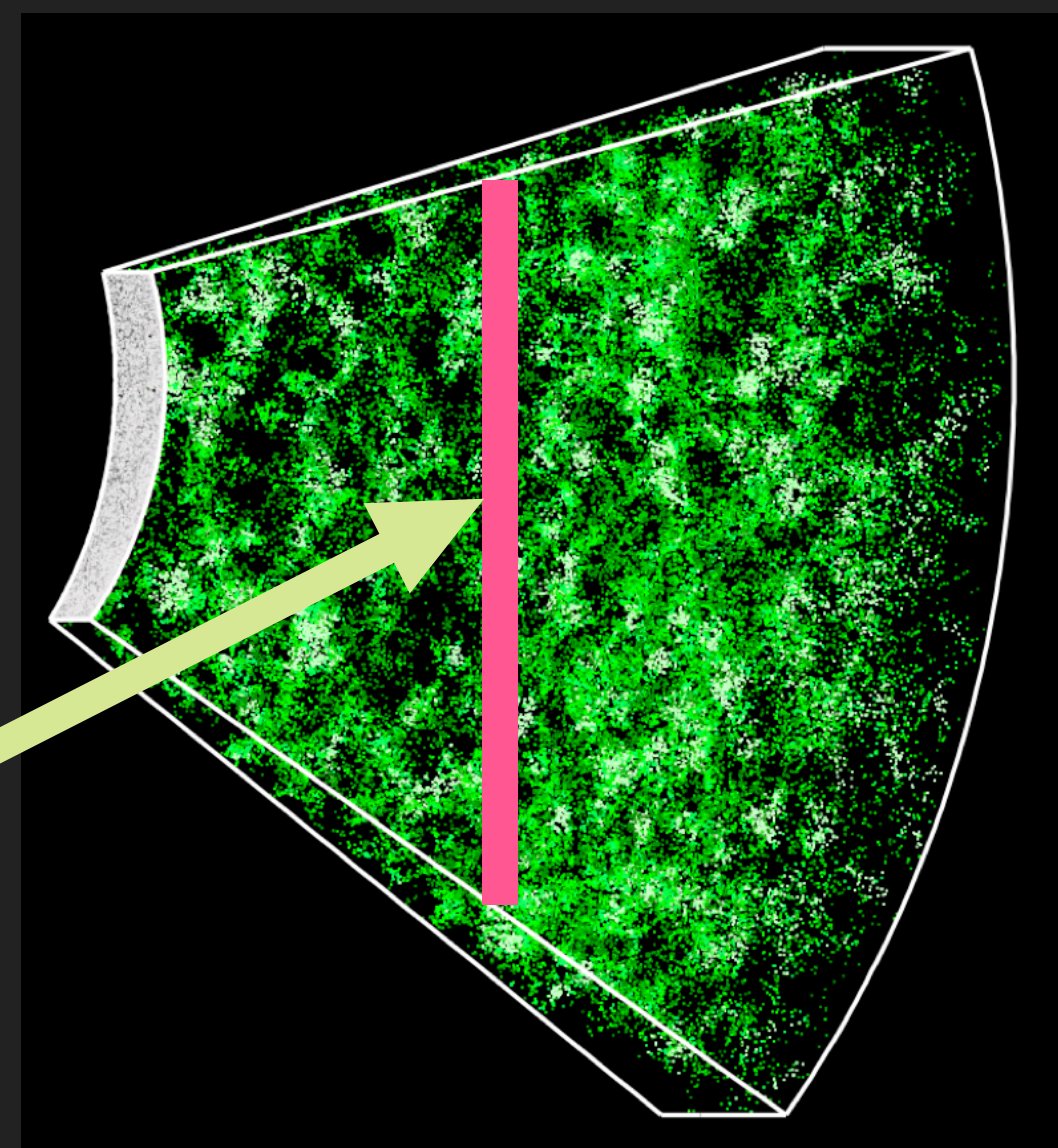
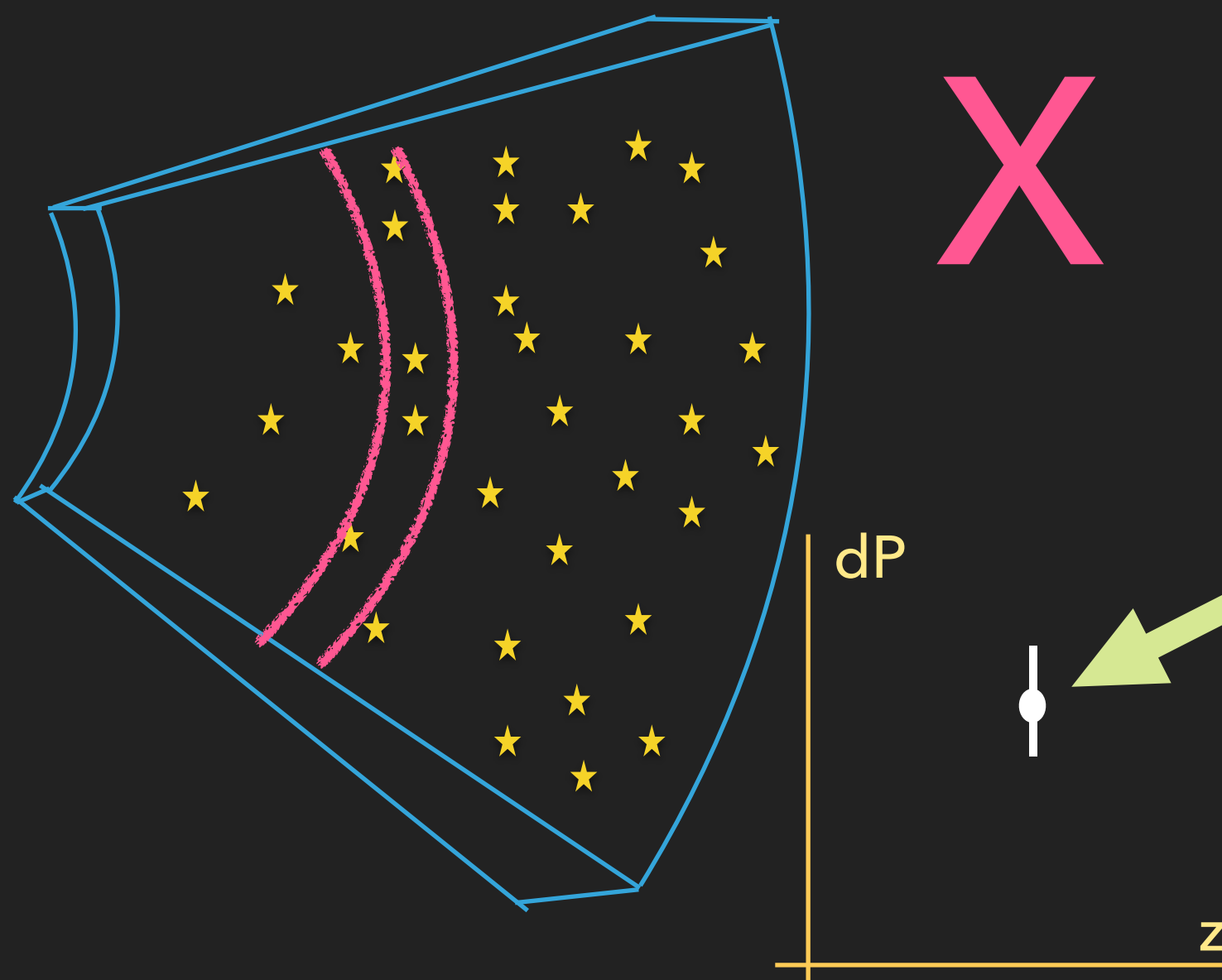
Galaxy samples observed in redshift space

Image credit: Jeremy Tinker and the SDSS-III collaboration

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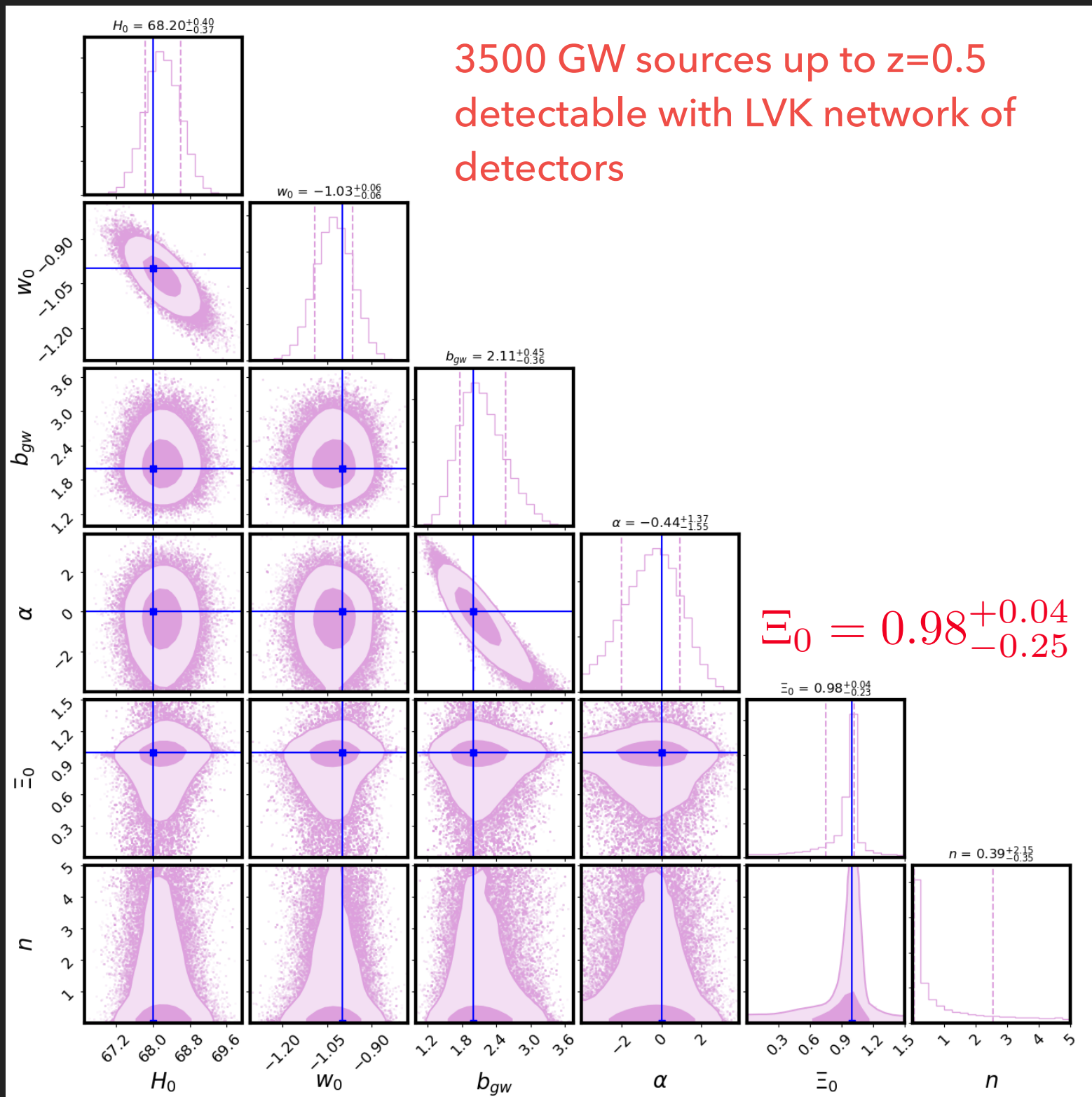


Dark sirens observed in luminosity distance space

Galaxy samples observed in redshift space

Image credit: Jeremy Tinker and the SDSS-III collaboration

## FORECAST TO MEASURE THE COSMOLOGICAL PARAMETERS FROM DARK SIRENS



Mukherjee, Wandelt, Silk  
(*MNRAS*, 502,1136, 2021)

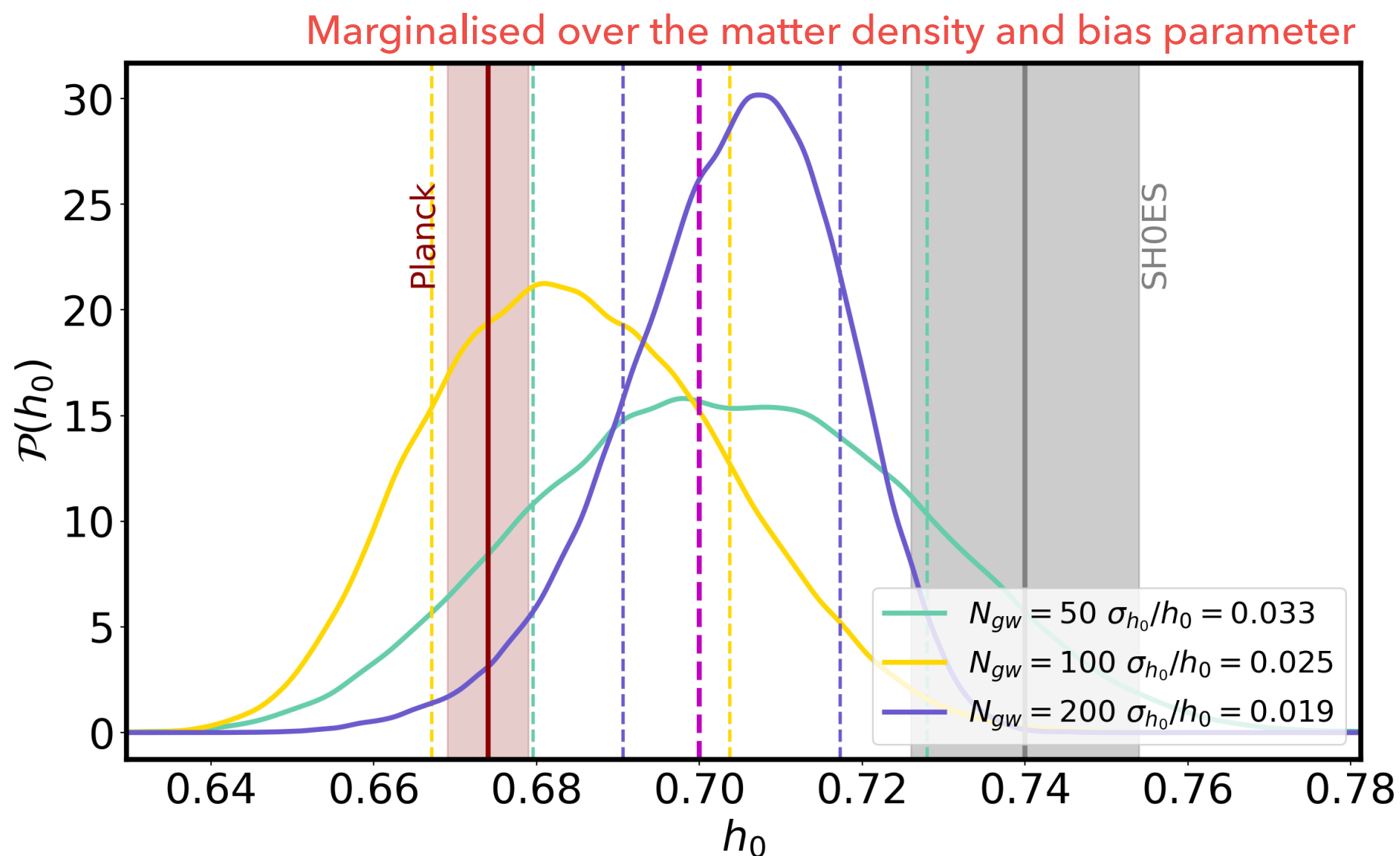
$$\frac{d_l^{GW}(z)}{d_l^{EM}(z)} = \Xi_0 + \frac{1 - \Xi_0}{(1+z)^n}$$

$$b(z) = b_{GW}(1+z)^\alpha$$



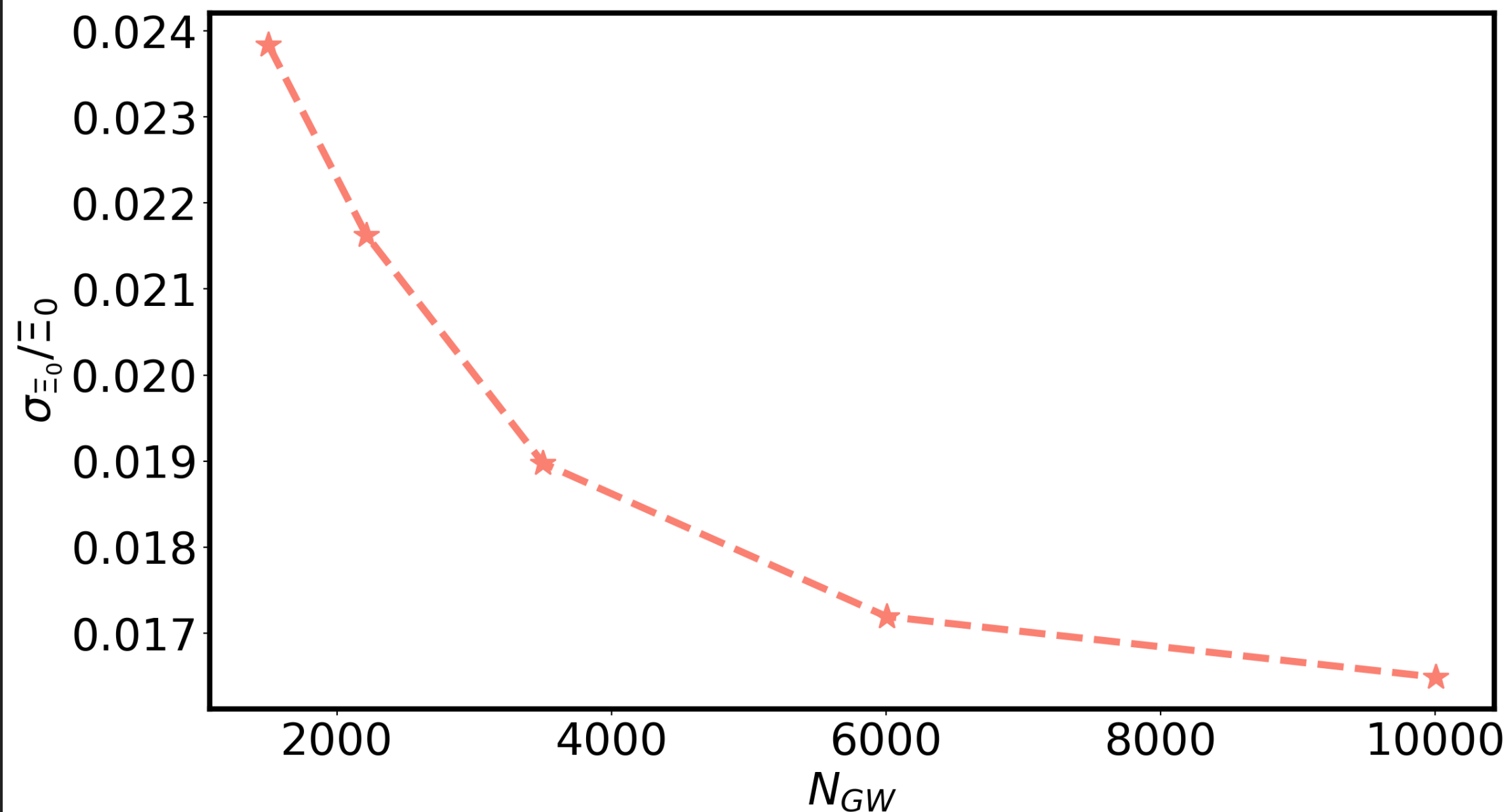
## FORECAST: HUBBLE CONSTANT FROM DARK SIRENS USING CROSS-CORRELATION WITH GALAXIES

Mukherjee, Wandelt, Nissanke, Silvestri (2021)



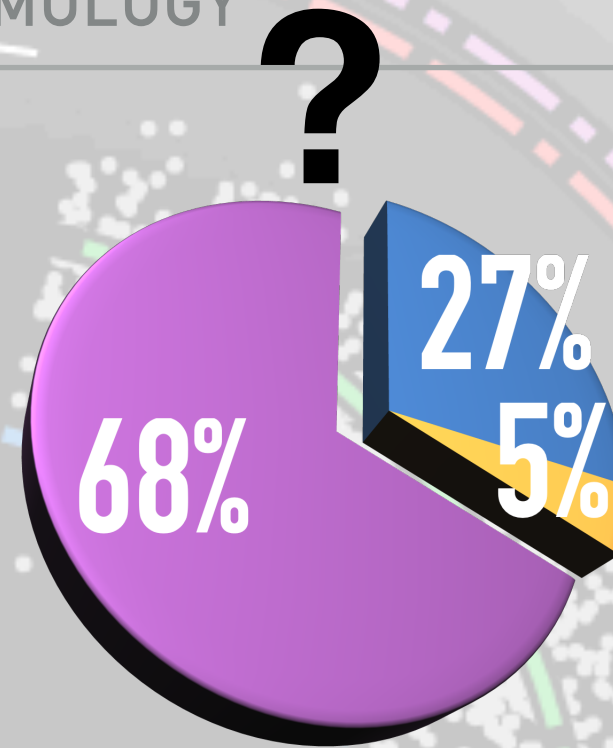
**FORECAST: FRICTIONAL TERM FROM DARK SIRENS USING CROSS-CORRELATION WITH GALAXIES**

Mukherjee, Wandelt, Silk (*MNRAS*, 502,1136, 2021)

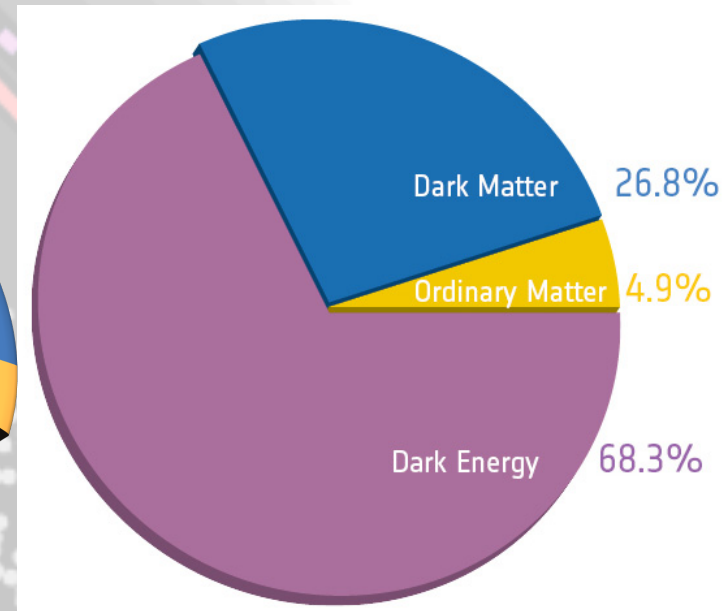


## TAKE HOME MESSAGES

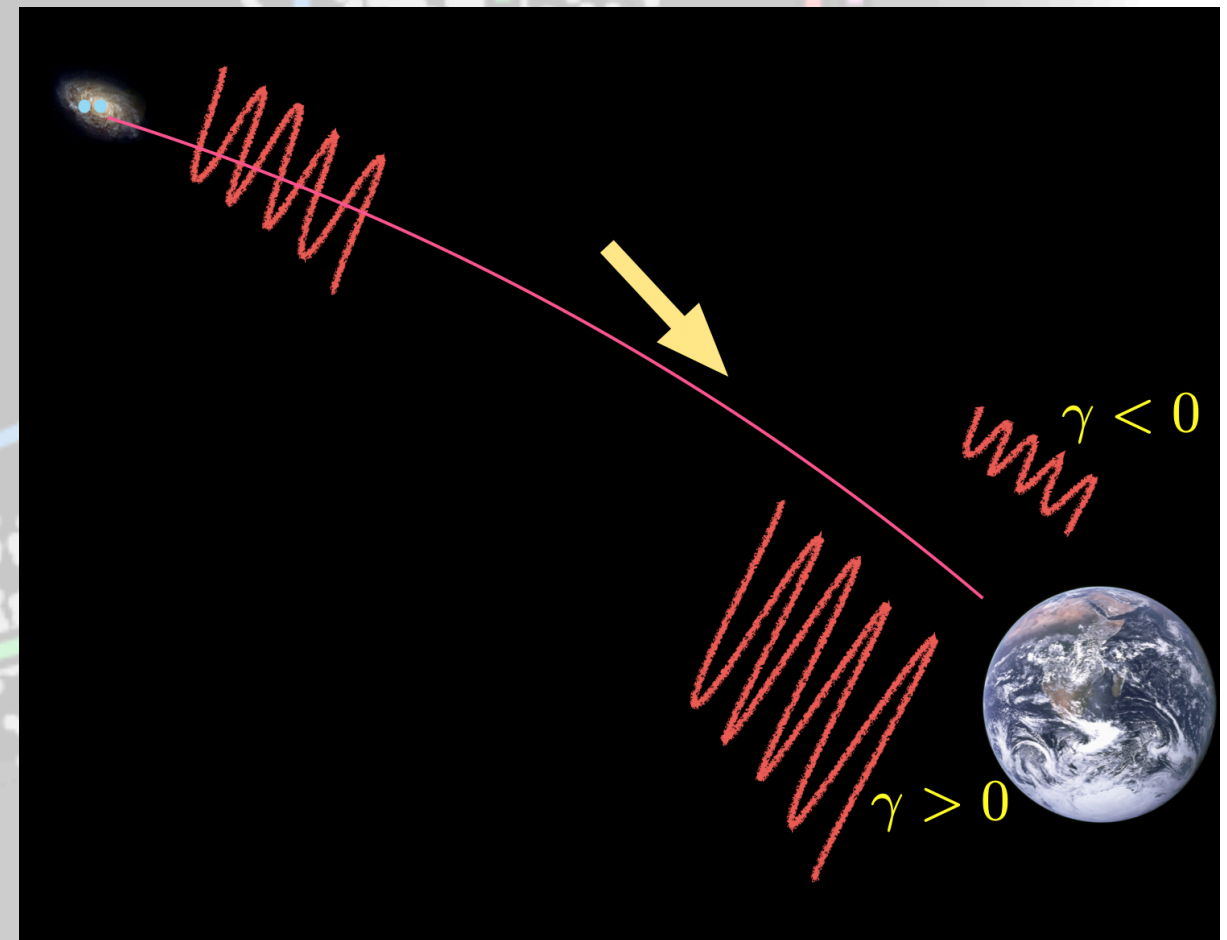
- ▶ Dark sirens will be able to provide an independent measurement of the cosmic pie chart.
- ▶ By combining the EM sector with the GW sector, we will test the theory of gravity at the cosmological scales.
- ▶ We will measure the GW bias and its redshift dependence.



From the GW sector  
(In future)



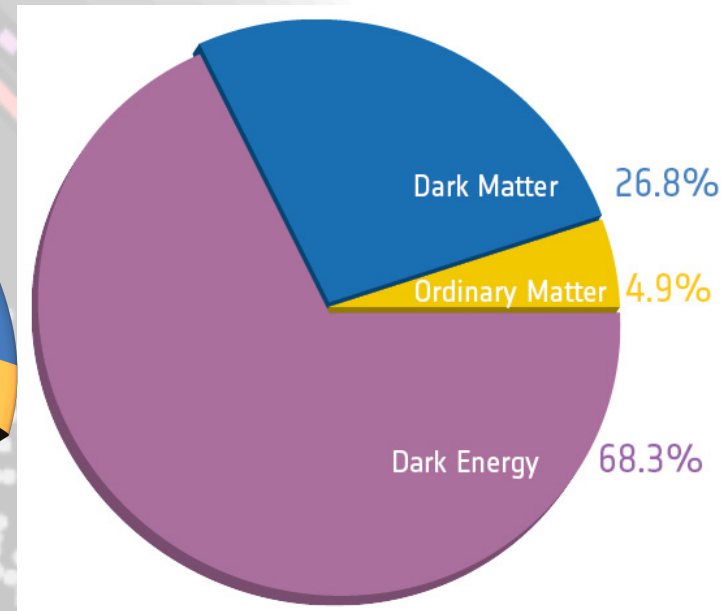
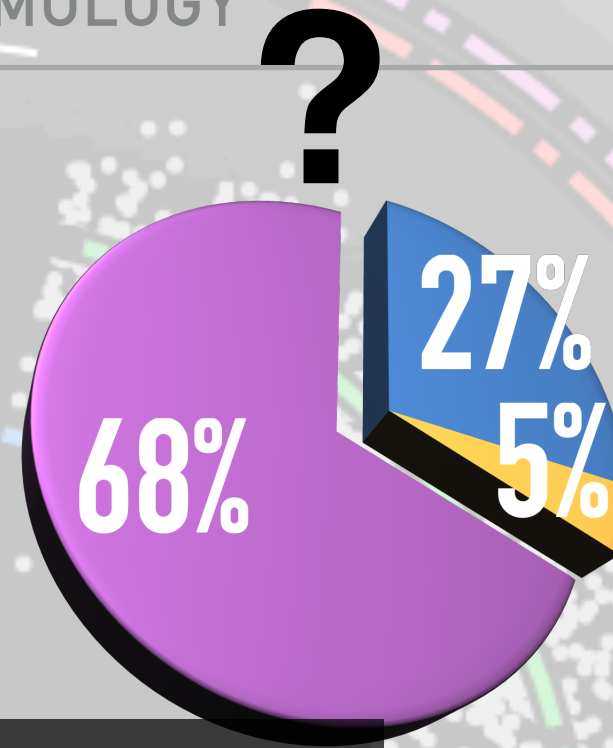
From the EM sector





## TAKE HOME MESSAGES

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From the GW sector  
(In future)

From the EM sector

Thank you

