

Patrick Poissel: A general pushforward theorem for compactly supported Fourier multipliers

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To any sufficiently regular distribution m on a locally compact group is associated, by the mean of the Fourier transform, some sort of « differential operator with symbol m » on the dual of this group which in general is merely a quantum group. In 1970, M. Jodeit Jr. has shown that if a compactly supported distribution on \mathbf{R}^d is the symbol of a continuous linear operator from $L^p(\mathbf{R}^d)$ to $L^q(\mathbf{R}^d)$, then its pushforward by the canonical homomorphism from \mathbf{R}^d to \mathbf{T}^d is the symbol of a continuous linear operator from $\ell^p(\mathbf{Z}^d)$ to $\ell^q(\mathbf{Z}^d)$. We propose a generalisation of this result by characterising the continuous homomorphisms of locally compact groups by which, for all exponents p and q , the pushforward of a compactly supported distribution symbol of a continuous linear operator from L^p to L^q is again the symbol of a continuous linear operator from L^p to L^q as being those which are open.