

## Patrick Poissel: A general pushforward theorem for compactly supported Fourier multipliers

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To any sufficiently regular distribution  $m$  on a locally compact group is associated, by the mean of the Fourier transform, some sort of « differential operator with symbol  $m$  » on the dual of this group which in general is merely a quantum group. In 1970, M. Jodeit Jr. has shown that if a compactly supported distribution on  $\mathbf{R}^d$  is the symbol of a continuous linear operator from  $L^p(\mathbf{R}^d)$  to  $L^q(\mathbf{R}^d)$ , then its pushforward by the canonical homomorphism from  $\mathbf{R}^d$  to  $\mathbf{T}^d$  is the symbol of a continuous linear operator from  $\ell^p(\mathbf{Z}^d)$  to  $\ell^q(\mathbf{Z}^d)$ . We propose a generalisation of this result by characterising the continuous homomorphisms of locally compact groups by which, for all exponents  $p$  and  $q$ , the pushforward of a compactly supported distribution symbol of a continuous linear operator from  $L^p$  to  $L^q$  is again the symbol of a continuous linear operator from  $L^p$  to  $L^q$  as being those which are open.