

Lagrange Duality Gap of Decomposed Dynamic Programming: The Case of Bandits

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This study explores **multi-armed bandit** problems under the premise that the decision-maker possesses prior knowledge of the arms' distributions and knows the finite time horizon. These conditions render the problems suitable for **stochastic multistage optimization decomposition techniques**. On the one hand, multi-armed bandit algorithms are integral to reinforcement learning and are supported by extensive theoretical analysis, particularly regarding regret minimization. Meanwhile, stochastic multistage optimization emphasizes examining the **performance gap between** a given policy and the optimal, adapted policy, which can be estimated numerically through dual methods. Within this framework, decomposition strategies have been demonstrated to efficiently tackle large-scale stochastic multistage optimization challenges. A fact in **dire need of better theoretical understanding**. On the empirical side, our experiments corroborate **the approach's efficacy on multi-armed bandit**. On the theoretical side, **we reinterpret the duality gap by relating it to quantities defined along the trajectory of the decision-making process**: the Lagrangian multiplier, the instantaneous reward and the value of information. This lays the groundwork for subsequent investigations into the performance of decomposition methods.

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