

# Positivity properties for the lowest summand of the asymptotic Hecke algebra

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Affine Hecke algebras play a prominent role in the representation theory of a  $p$ -adic group  $G$ , with the principal Bernstein block being equivalent to modules over the Iwahori-Hecke algebra. Braverman-Kazhdan proposed Lusztig's asymptotic Hecke algebra  $J$  as means to an algebraic version of tempered representations for the principal block. In particular, elements of  $J$  are certain rapidly-decaying functions on  $G(F)$ .

I will explain positivity properties, as conjectured by Braverman-Kazhdan, for two bases of the best understood part of the ring  $J$ , in terms of K-theory of the flag variety of  $\hat{G}$  and spherical Kazhdan-Lusztig polynomials for  $G$ , and report on joint work

in progress with Bezrukavnikov to give an asymptotic characterization of these functions in terms of the wonderful compactification of  $G$ . Time permitting, I will explain partial results on positivity properties for two-sided cells corresponding to Levi subgroups of the general linear group with one block size.

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