

# Formal transversality of the infinitesimal generator along the fixed point set

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Given a tangent to the identity germ of holomorphic diffeomorphism  $\phi$ , we consider the map  $P \mapsto \phi_P$  that associates to any fixed point  $P$  of  $\phi$  near the origin the germ  $\phi_P$  of  $\phi$  at  $P$ . Such germs are not in general tangent to the identity. Given the infinitesimal generator  $X$  of  $\phi$ , a formal vector field, it is natural to ask whether we can define “infinitesimal generators”  $X_P$  of  $\phi_P$  for  $P \in \text{Fix}(\phi)$  and if the dependence of  $X_P$  on  $P \in \text{Fix}(\phi)$  is analytic. In other words, we are asking whether  $X$  is formally transversal along  $\text{Fix}(\phi)$ .

We introduce a weak and a strong concept of formal transversality for  $X$ . On the one hand, we will see that  $X$  is always formally transversal along  $\text{Fix}(\phi)$  in the weak sense. On the other hand, there are examples where  $X$  is not formally transversal along  $\text{Fix}(\phi)$  in the strong sense. We will discuss the gap between the weak and the strong concepts and provide a characterization of strong formal transversality. This is a joint work with Rudy Rosas.

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