

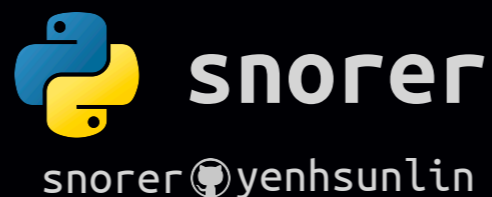
NDM 2025, Institut Henri Poincaré, Paris, May 5 - 23, 2025

SHIMMERING DARKNESS

Mapping the distribution of SNIa BDM across the sky

Yen-Hsun Lin
Academia Sinica

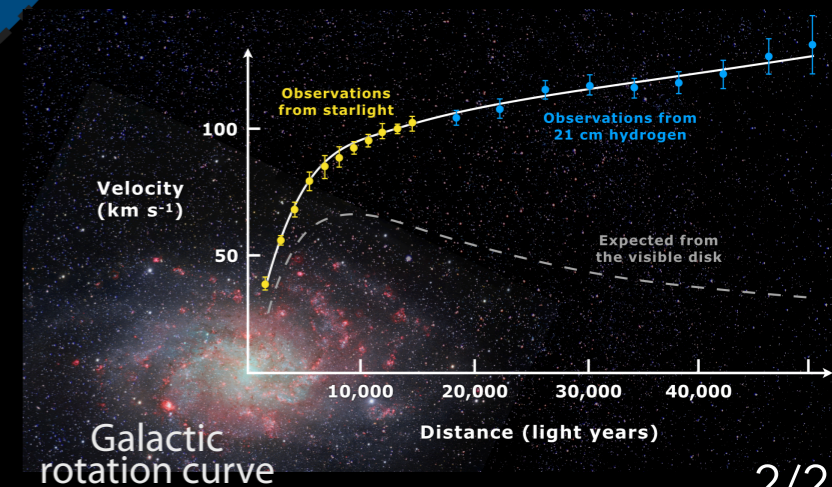
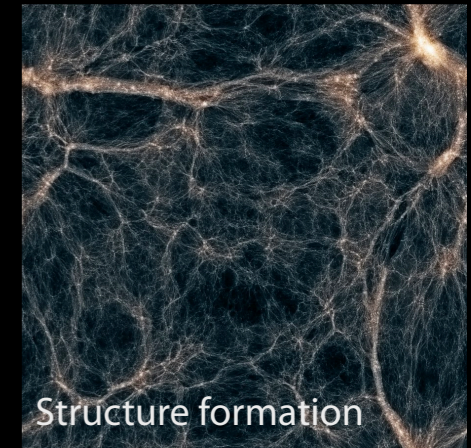
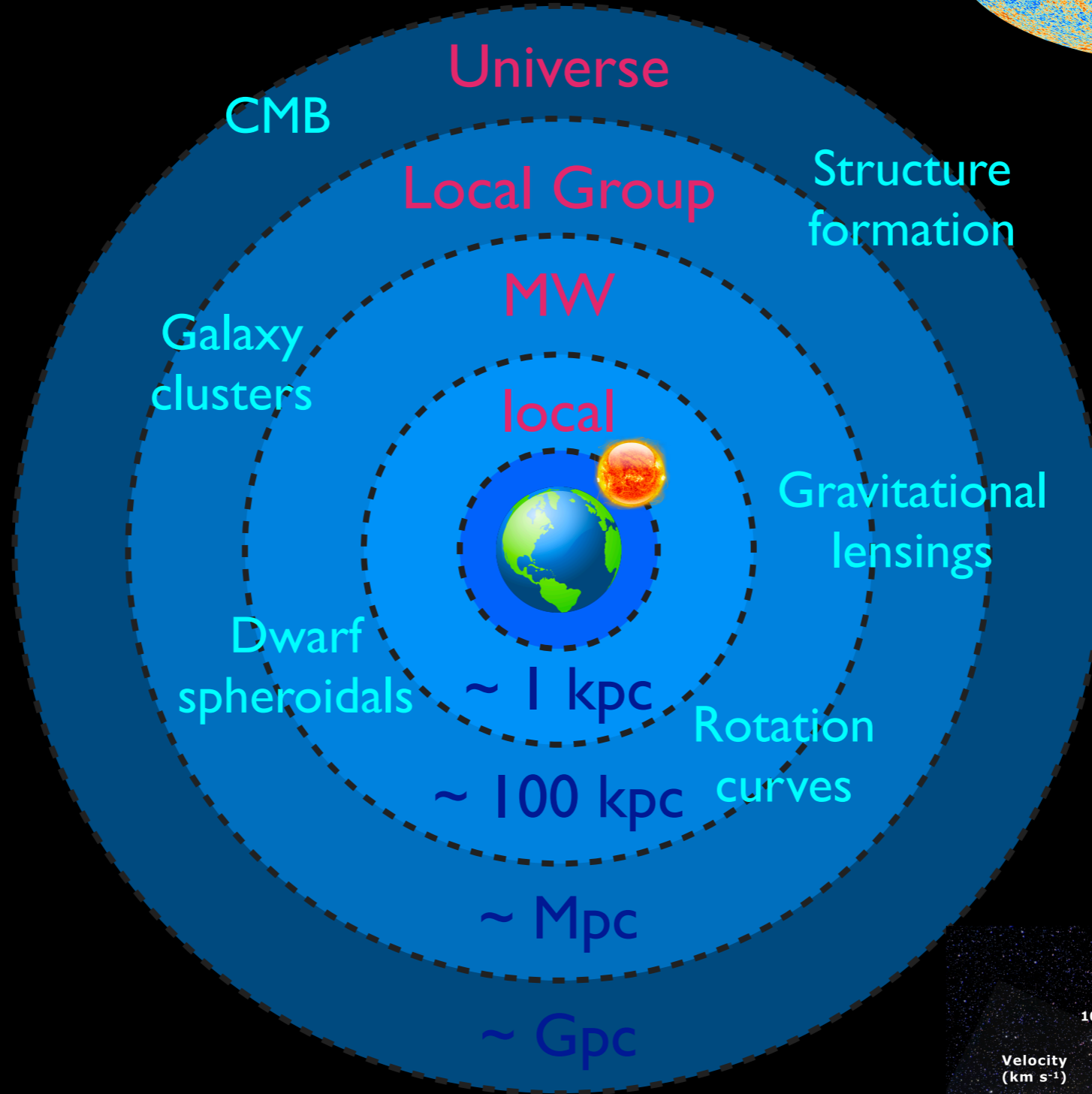
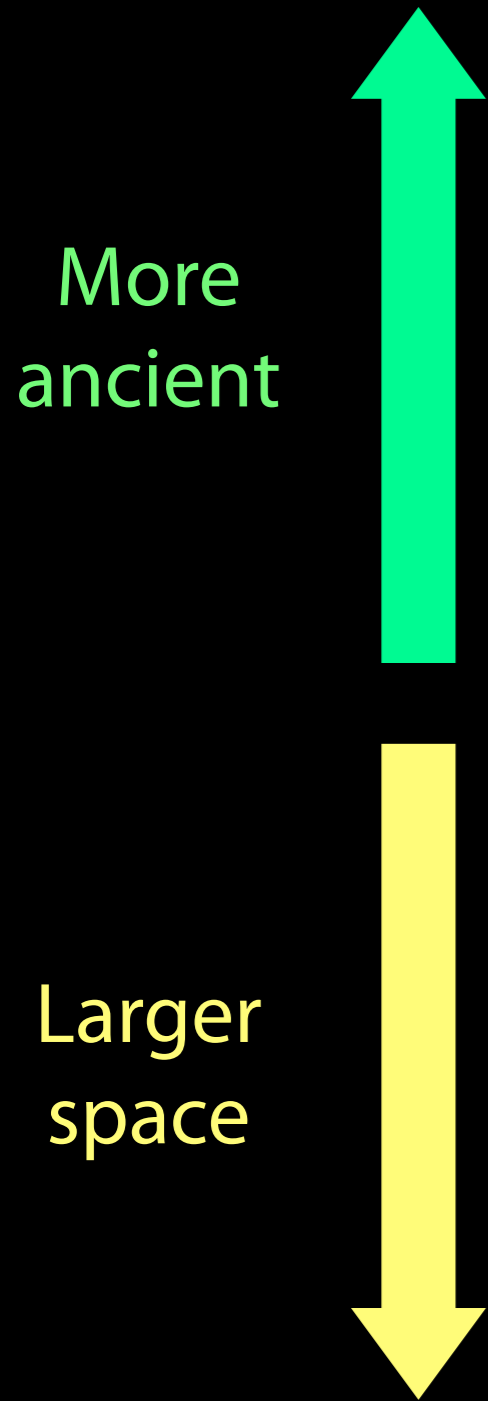
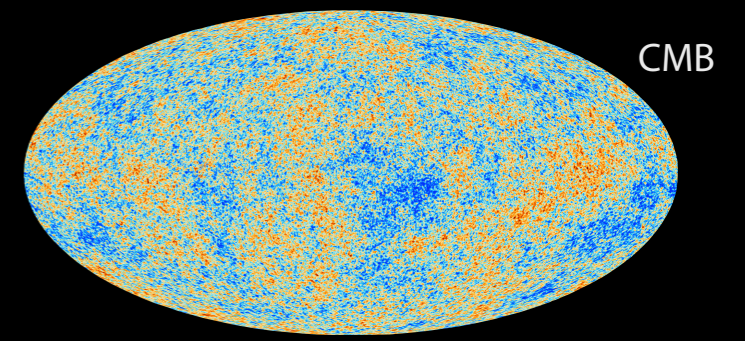
✉ yensun@phys.ncku.edu.tw



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Dark matter is *ubiquitous* in the Universe!

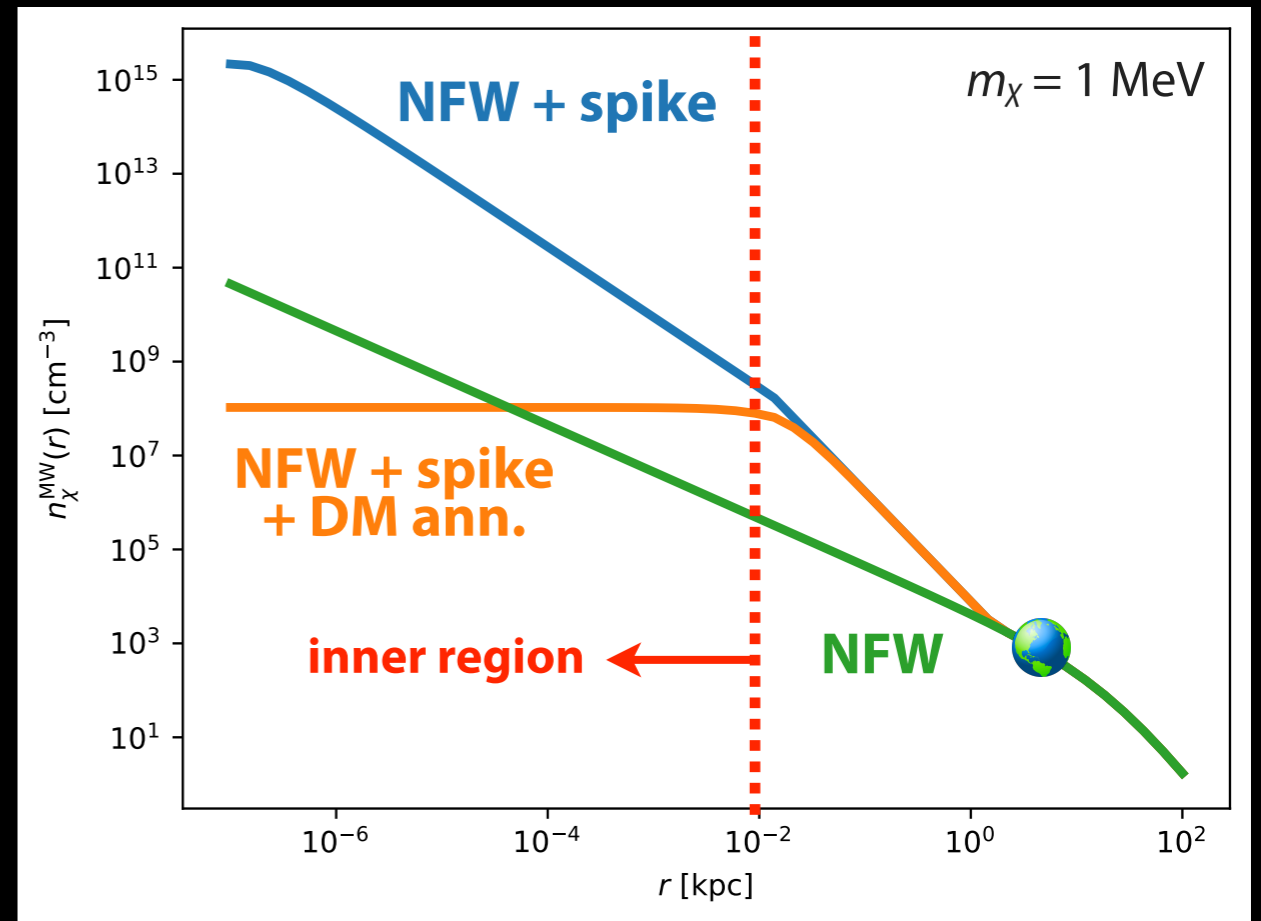
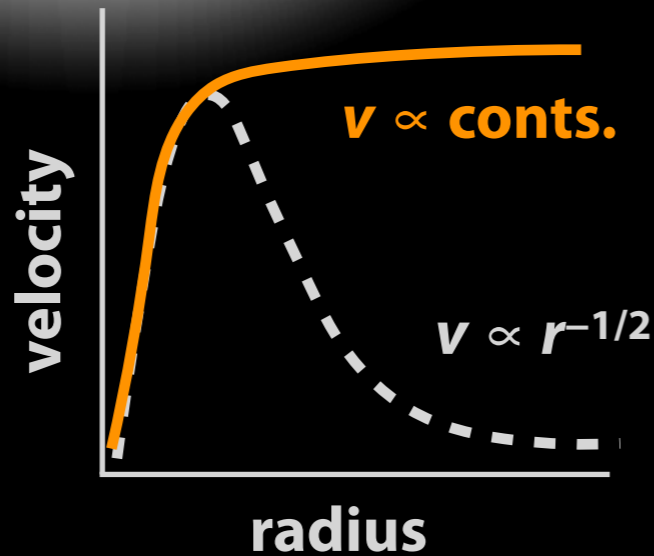
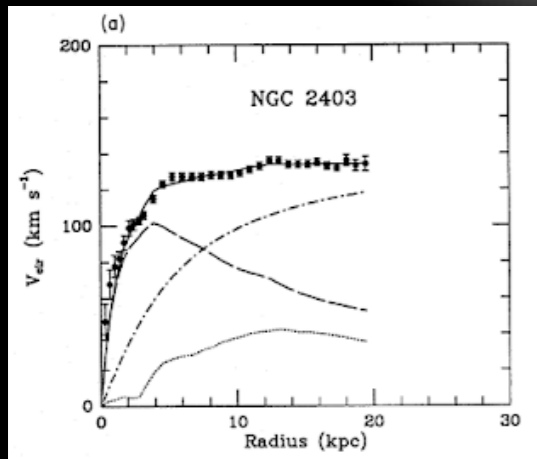
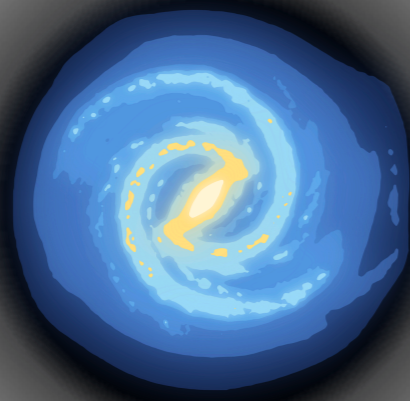


Dark matter halo

- Dark matter density in our Milky Way is characterized by **Navarro-Frenk-White (NFW) profile**

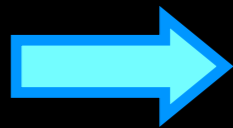
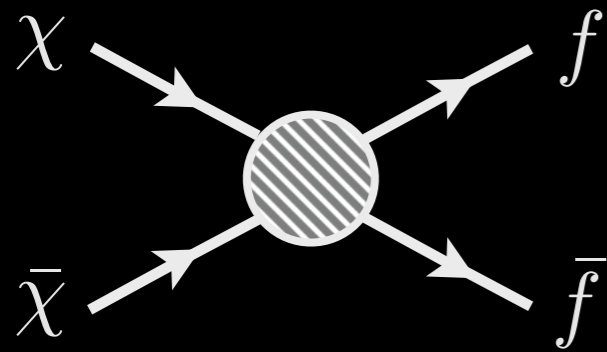
$$\rho_\chi(r) = \frac{\rho_s}{\frac{r}{r_s} \left(1 + \frac{r}{r_s}\right)^2}$$

with $\rho_s = 184 \text{ MeV cm}^{-3}$ and $r_s = 24.4 \text{ kpc}$



Modern approaches for probing DM

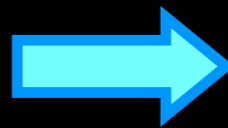
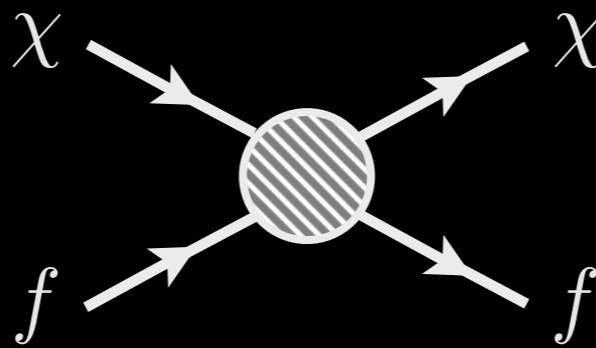
MAKE



Annihilation signals in deep space

$$\langle \sigma v \rangle$$

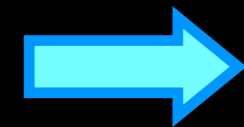
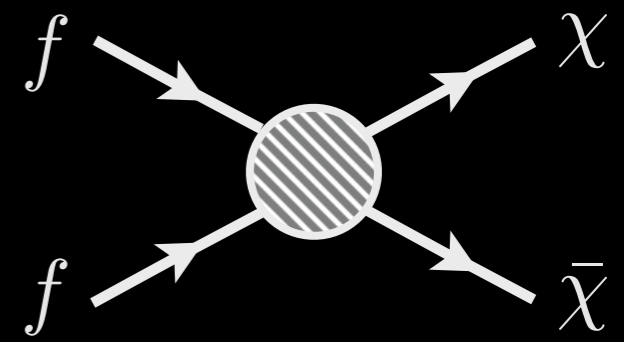
SHAKE



Recoil signals from DM scattering off nucleus and leptons

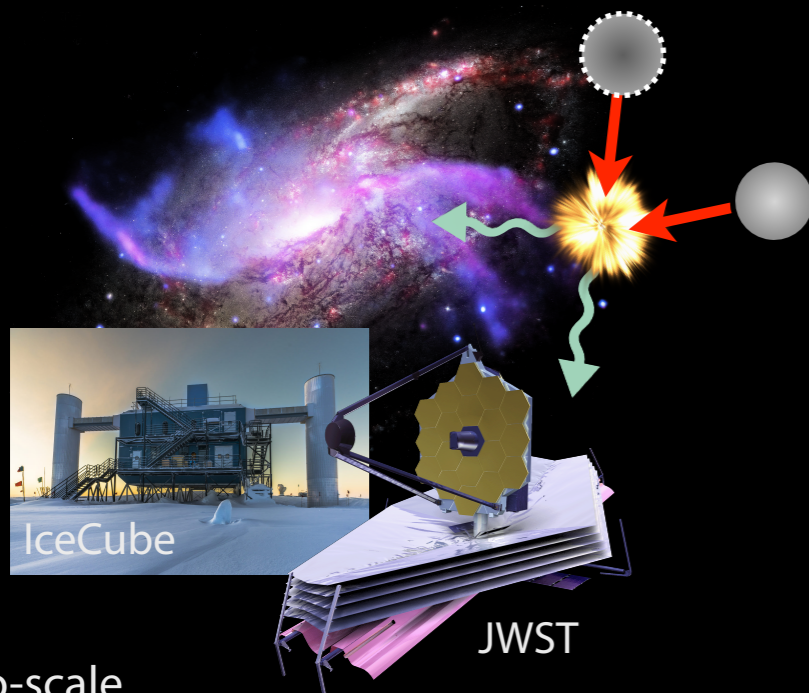
$$\sigma_{\chi f}$$

BREAK



Missing momentum

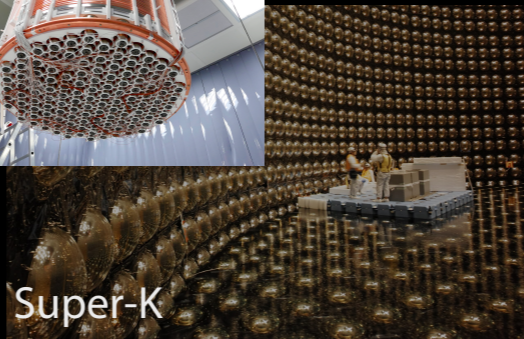
$$\Lambda$$



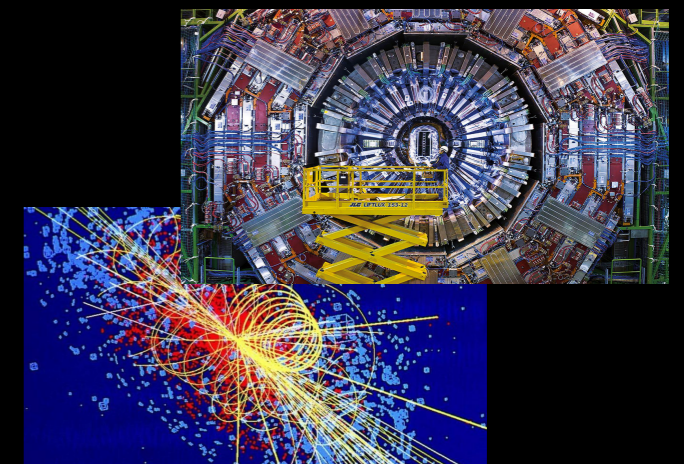
XENON



Super-K

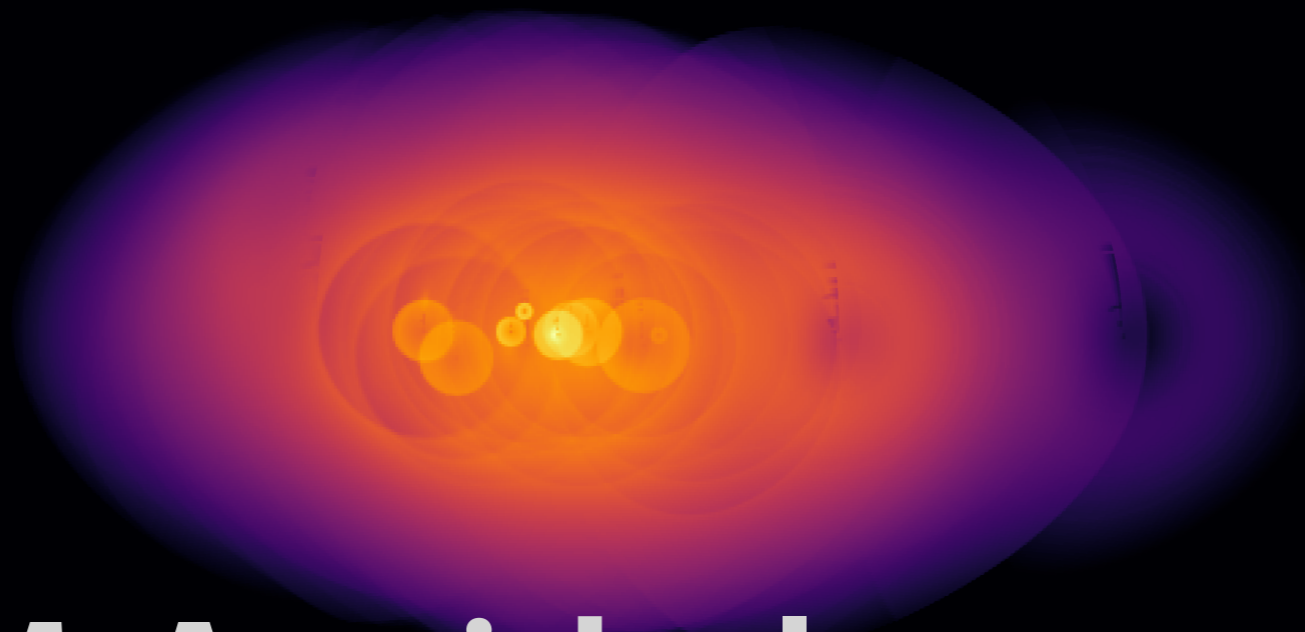


LHC



Outline

- **Supernova-neutrino-boosted dark matter (SN ν BDM)**
 - ▶ Concept introduction
 - ▶ Time-dependent flux and direct DM mass measurement
- **BDM flux from SNe in the past**
 - ▶ In our Milky Way (distribution in both spatial and temporal dimensions)
 - ▶ From all galaxies in the Universe
- **Summary**



$SN\nu$ BDM: A quick glance

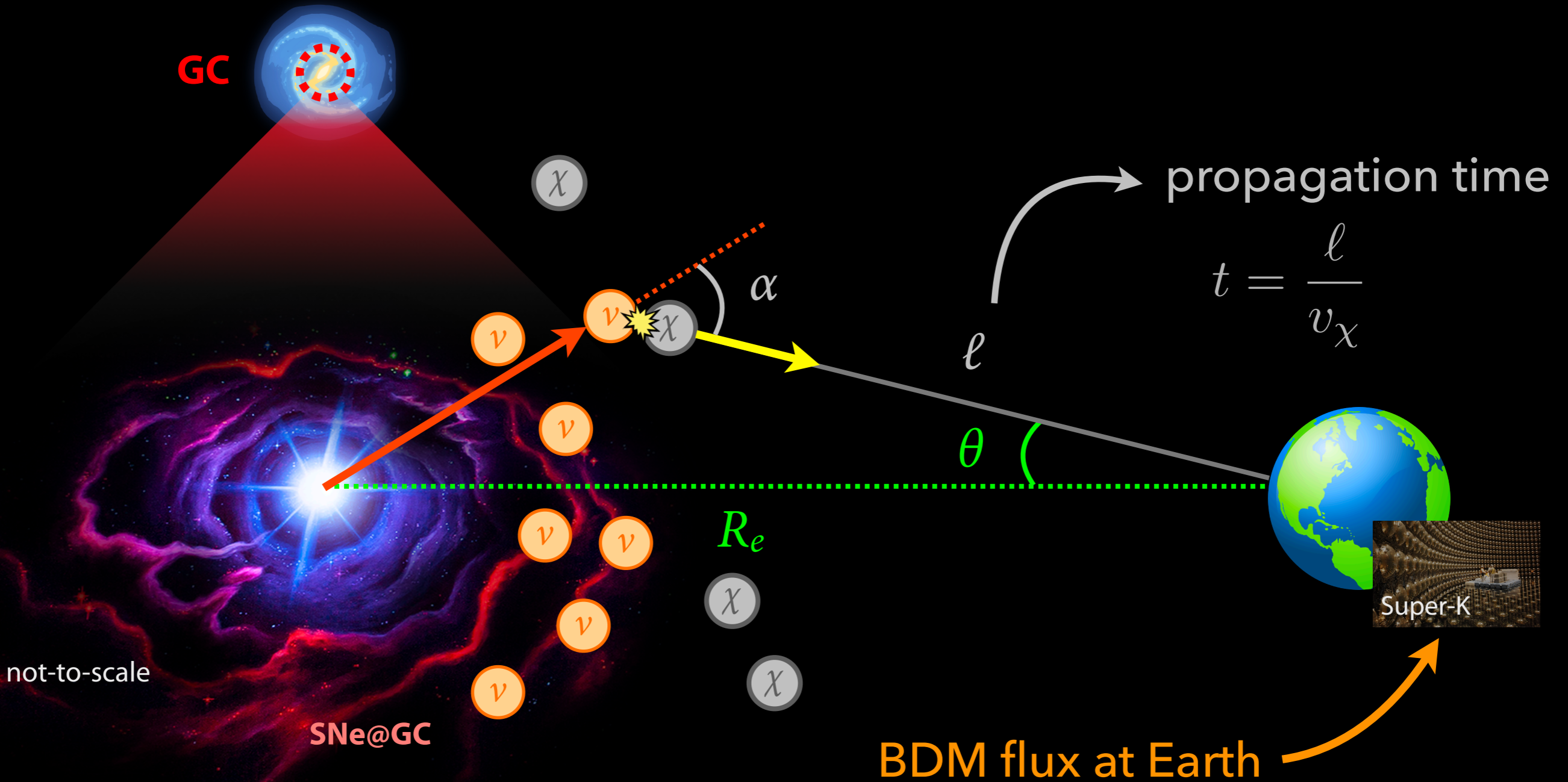
A direct measurement of dark matter mass through time-of-flight signature

YHL+, *PRL* **130**, 111002 (2023) [2206.06864]

YHL+, *PRD* **108**, 083013 (2023) [2307.03522]

Milky Way

GC



Duration: ~ 10 s

$$N_\nu \approx 10^{58}$$

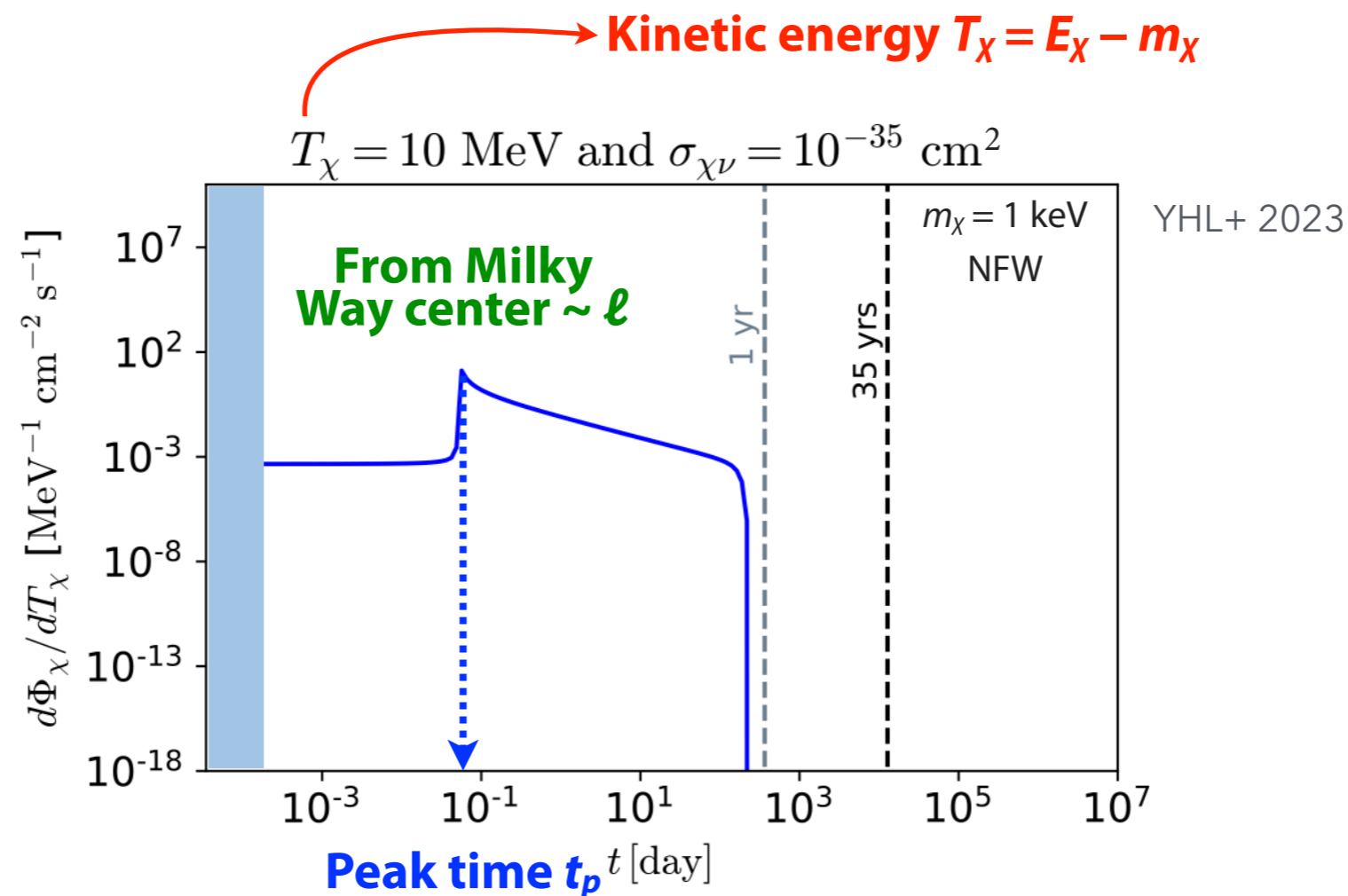
$$\bar{E}_\nu \approx 10 - 15 \text{ MeV}$$

$$\frac{d\phi_\nu}{dE_\nu} = \sum_i \frac{L_\nu}{4\pi r^2 \langle E_{\nu_i} \rangle} E_\nu^2 f_{\nu_i}(E_\nu)$$

Duan+ 2006

$$\frac{d\Phi_\chi(T_\chi, t)}{dT_\chi} = 2\pi r \int_0^1 d\cos\theta \mathcal{J} j_\chi(r, T_\chi, \alpha) \Big|_{t' = \frac{r}{c} + \frac{\ell}{v_\chi}}$$

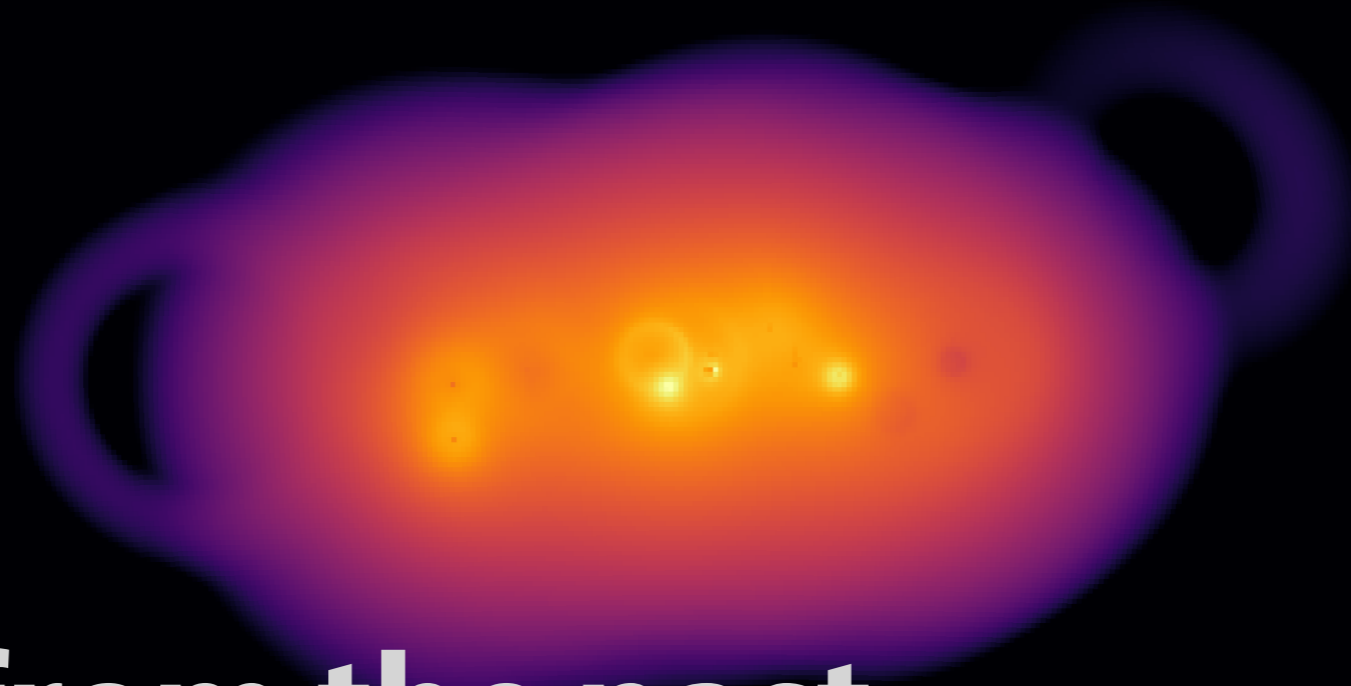
Time-dependent flux and DM mass



- Three measurable quantities t_p , ℓ and v_χ uniquely determine m_χ

$$t_p \sim \frac{\ell}{v_\chi(T_\chi, m_\chi)} \rightarrow m_\chi \simeq 9.7 \text{ keV} \times \left(\frac{t_p}{10 \text{ days}} \right)^{1/2} \left(\frac{T_\chi}{10 \text{ MeV}} \right)$$

- Precise flux measurement in large underground detectors can be a good complementary probe to the DM direct search



Echoes from the past

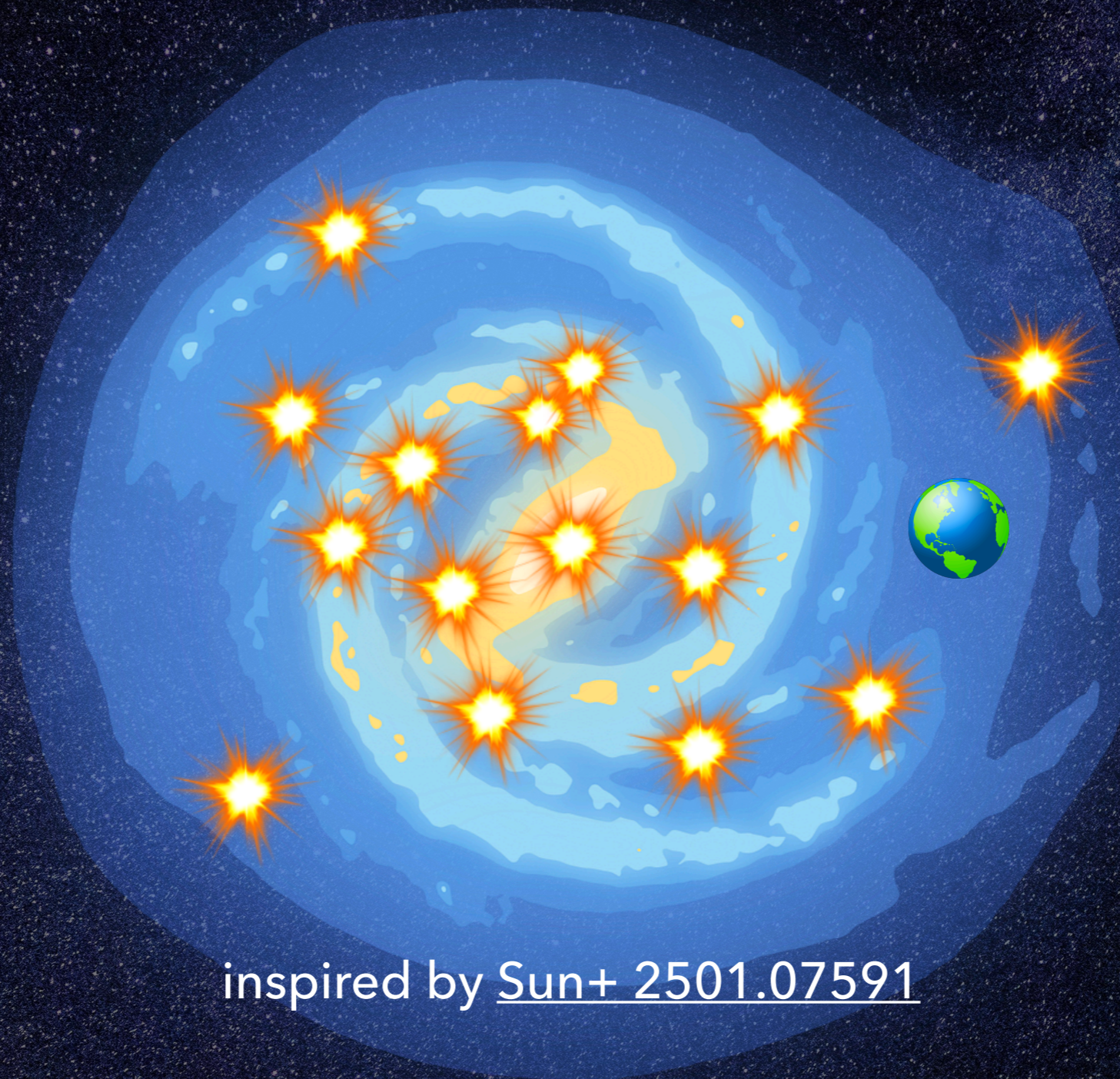
SN *v* BDM from the past SNe in our Milky Way and all galaxies in the Universe

YHL & MRW, *PRL* **133**, 111004 (2024) [2404.08528]

25xx.xxxxx, *in preparation*

Where to look?

Diffusive?

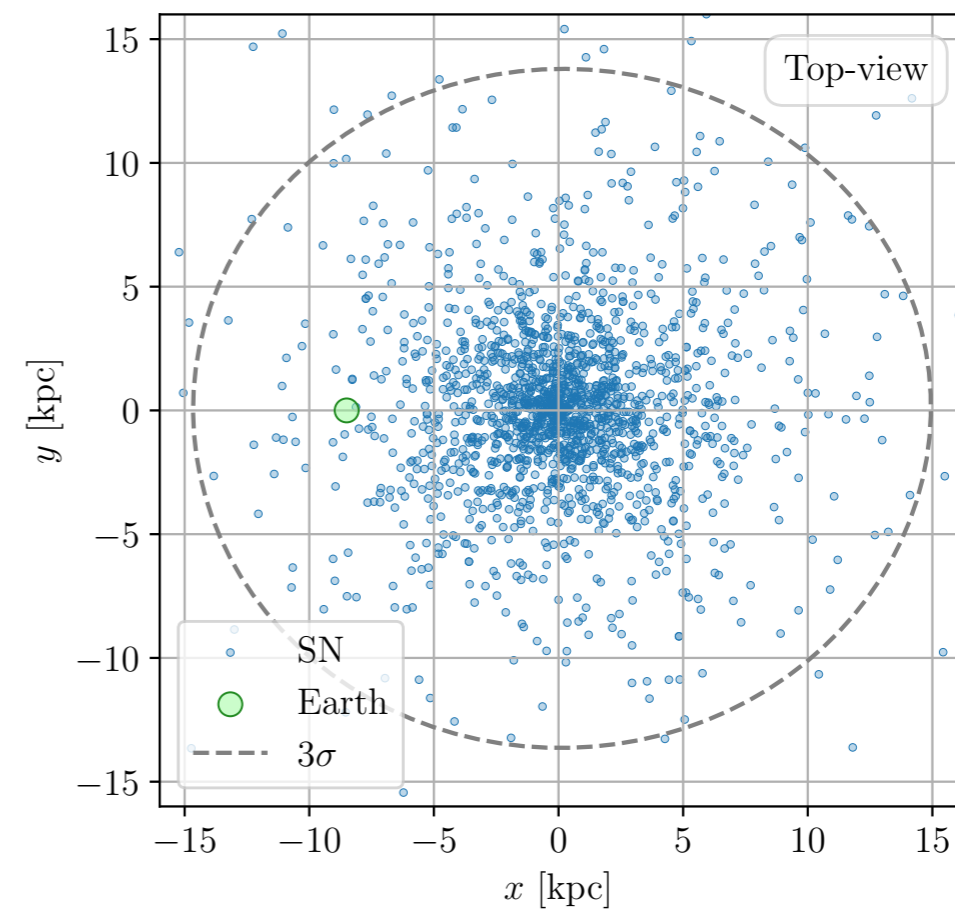
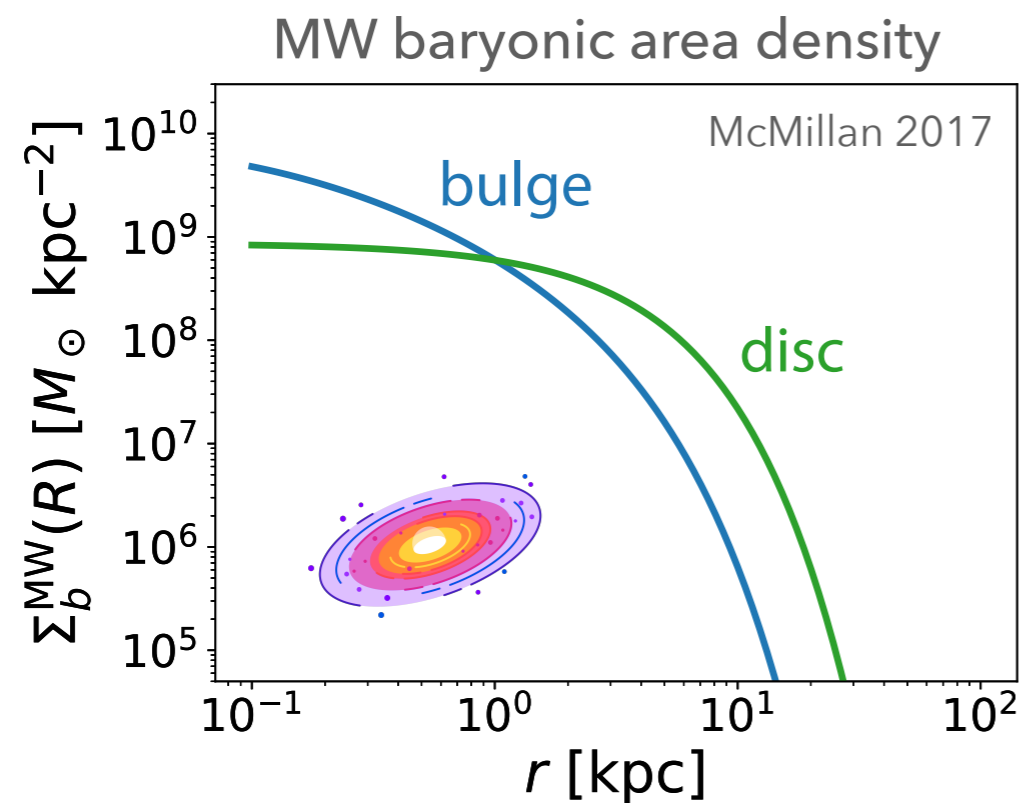


Transient?

inspired by Sun+ 2501.07591

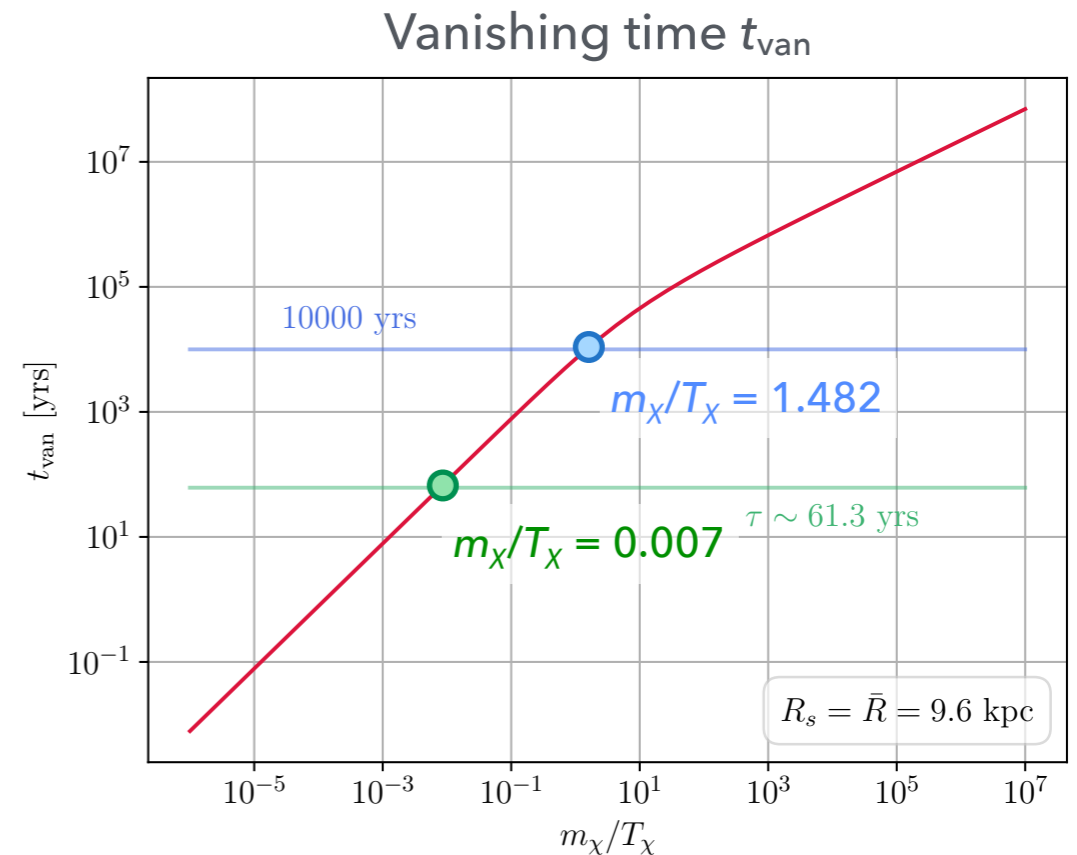
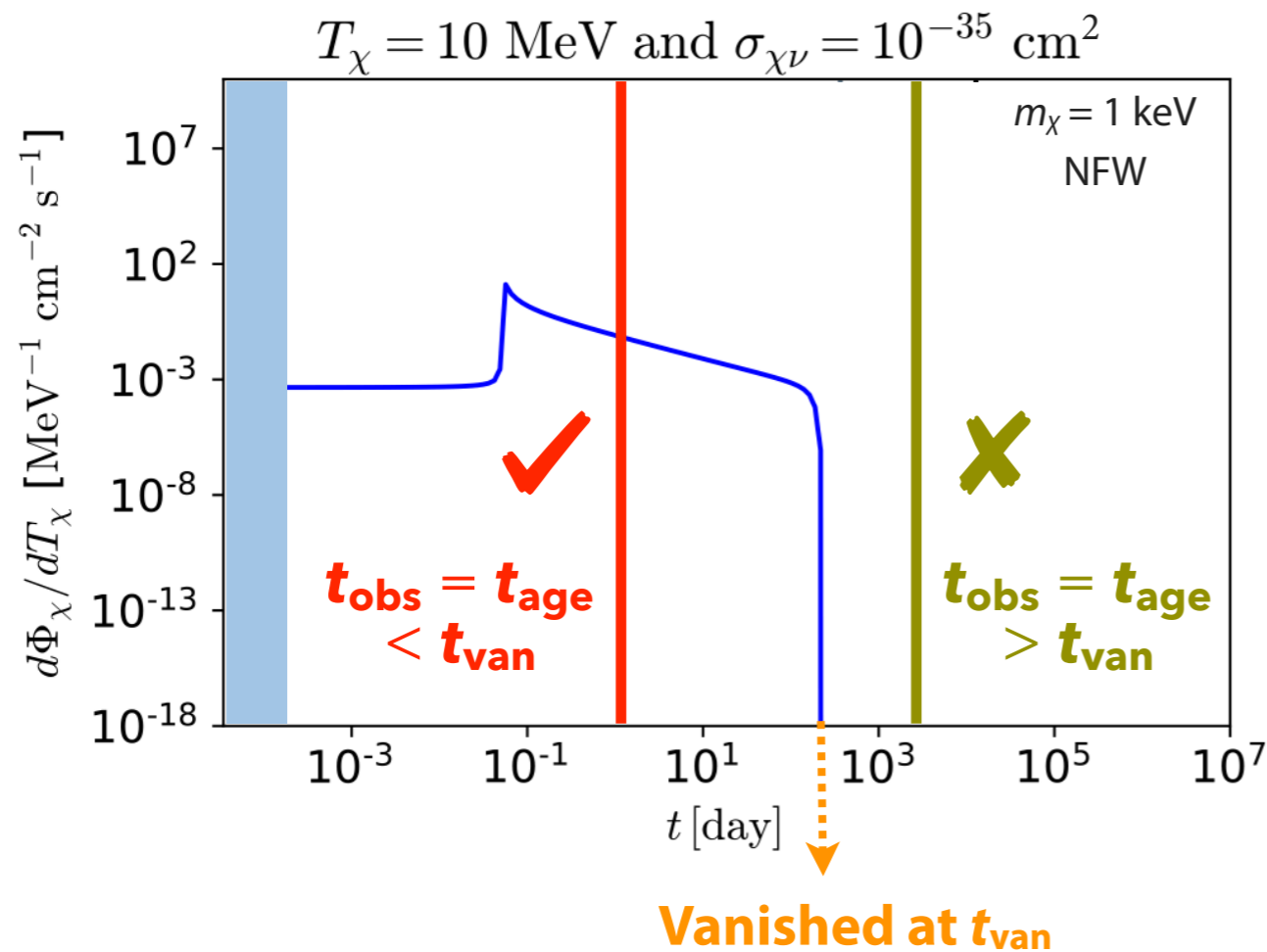
When to look?

- Core-collapse SN rate $1/\tau \sim 1.63/\text{century}$ ($\tau \sim 61$ yrs) \rightarrow Mean 1,630 SNe in **100,000 years**
Rozwadowska+ 2021
- The SNe spatial distribution over the Milky Way



- The SN occurrence follows uniform distribution within **100,000 years**

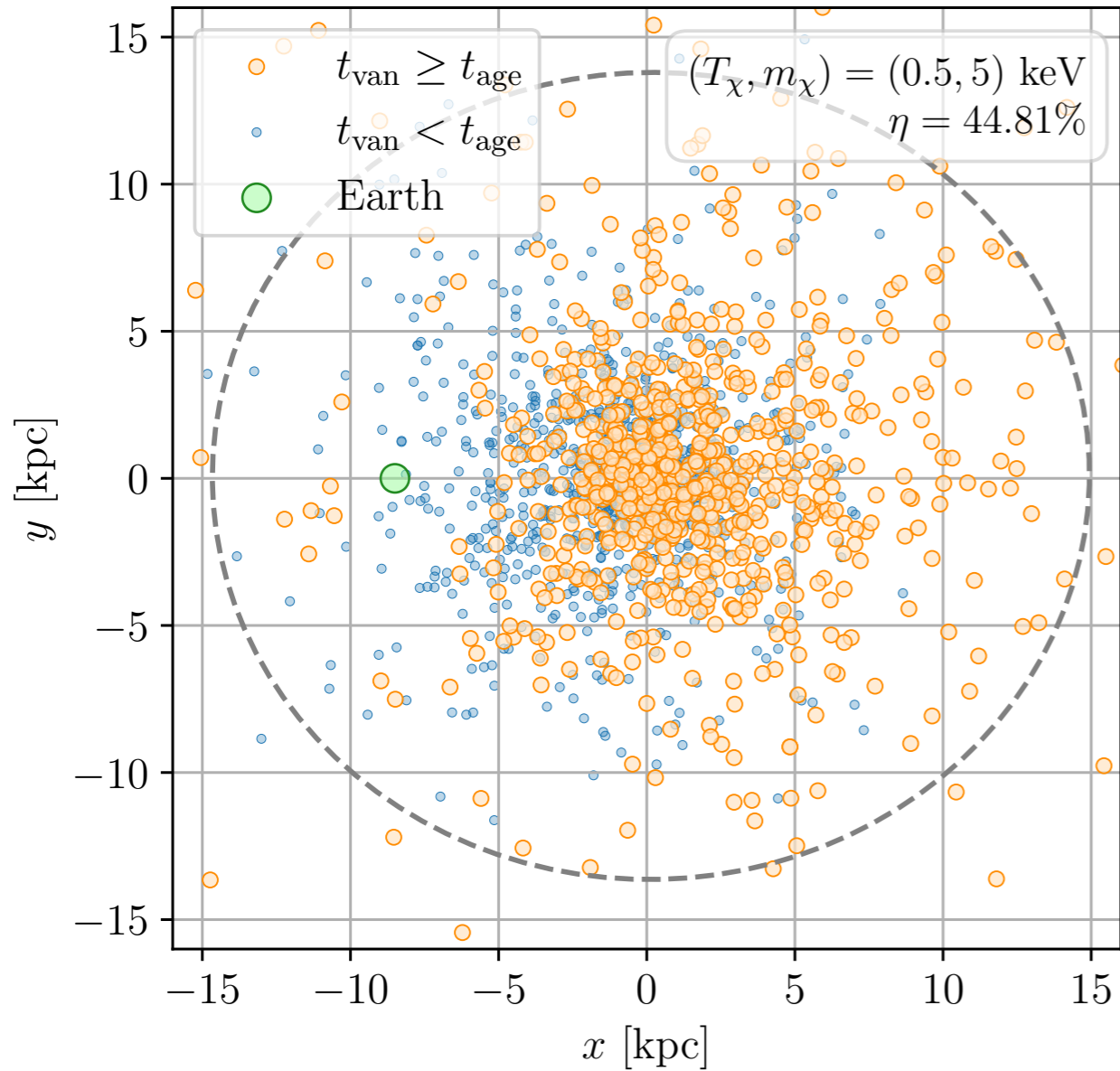
The vanishing of the flux



- Non-zero BDM contribution at Earth happens when $t_{\text{van}} > t_{\text{age}}$
- Larger m_χ/T_χ yields longer t_{van}

$$t_{\text{van}} \sim \begin{cases} \frac{R_s}{c} \sqrt{\frac{m_\chi}{2T_\chi}} \approx 6.2 \times 10^5 \text{ yrs} \left(\frac{R_s}{8.5 \text{ kpc}} \right) \left(\frac{m_\chi/T_\chi}{1000} \right)^{1/2}, & \frac{m_\chi}{T_\chi} \gg 1 \text{ (non-rel.)} \\ \frac{R_s}{c} \frac{m_\chi}{4T_\chi} \approx 6.9 \text{ yrs} \left(\frac{R_s}{8.5 \text{ kpc}} \right) \left(\frac{m_\chi/T_\chi}{0.001} \right), & \frac{m_\chi}{T_\chi} \ll 1 \text{ (ultra-rel.)} \end{cases}$$

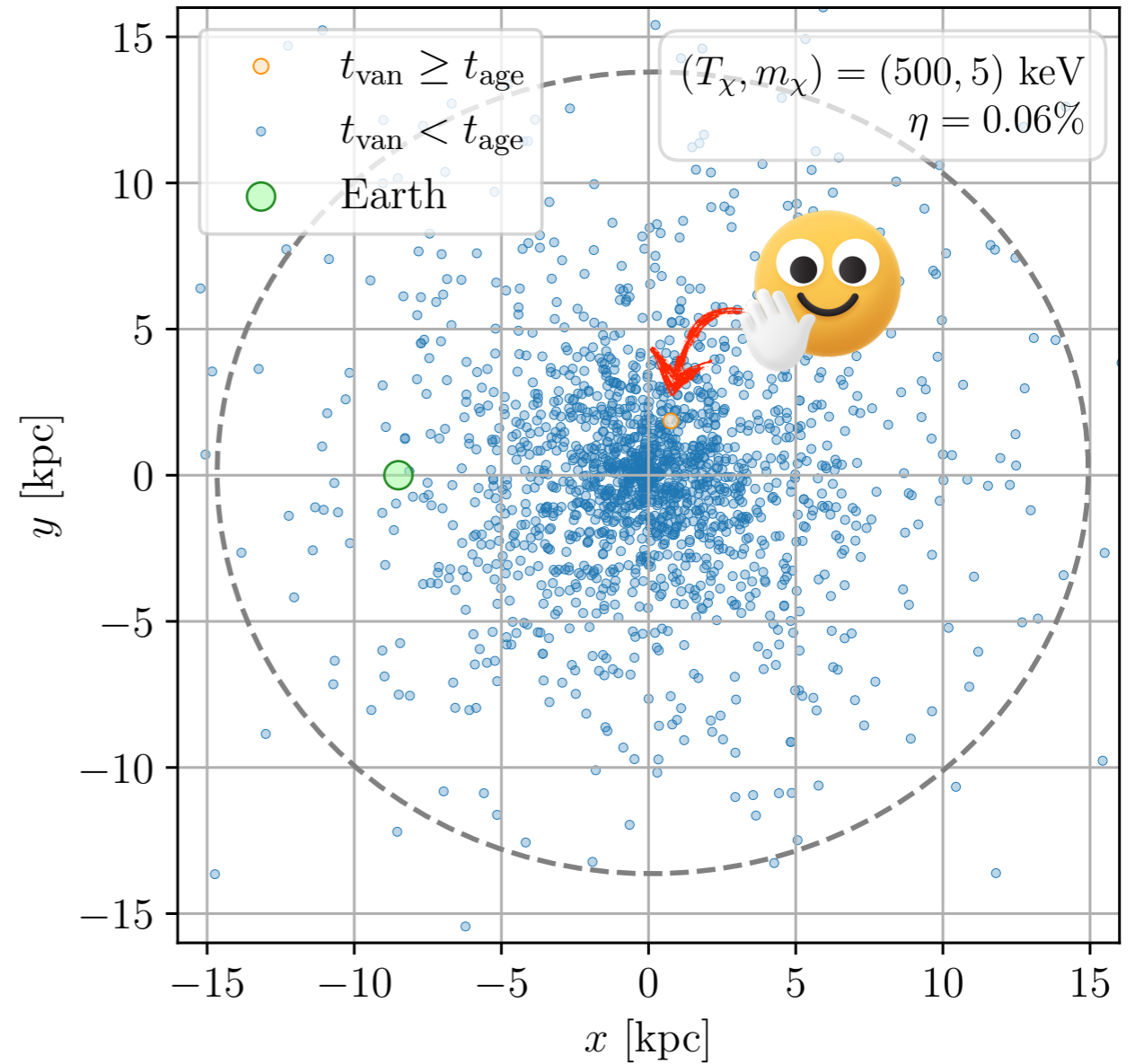
$m_\chi = 5 \text{ keV}$
 $t = 10^5 \text{ years, present day (AD 2025)}$



$T_\chi = 0.5 \text{ keV}$

$m_\chi/T_\chi = 10$

Contributed
SN rate:
44.81%



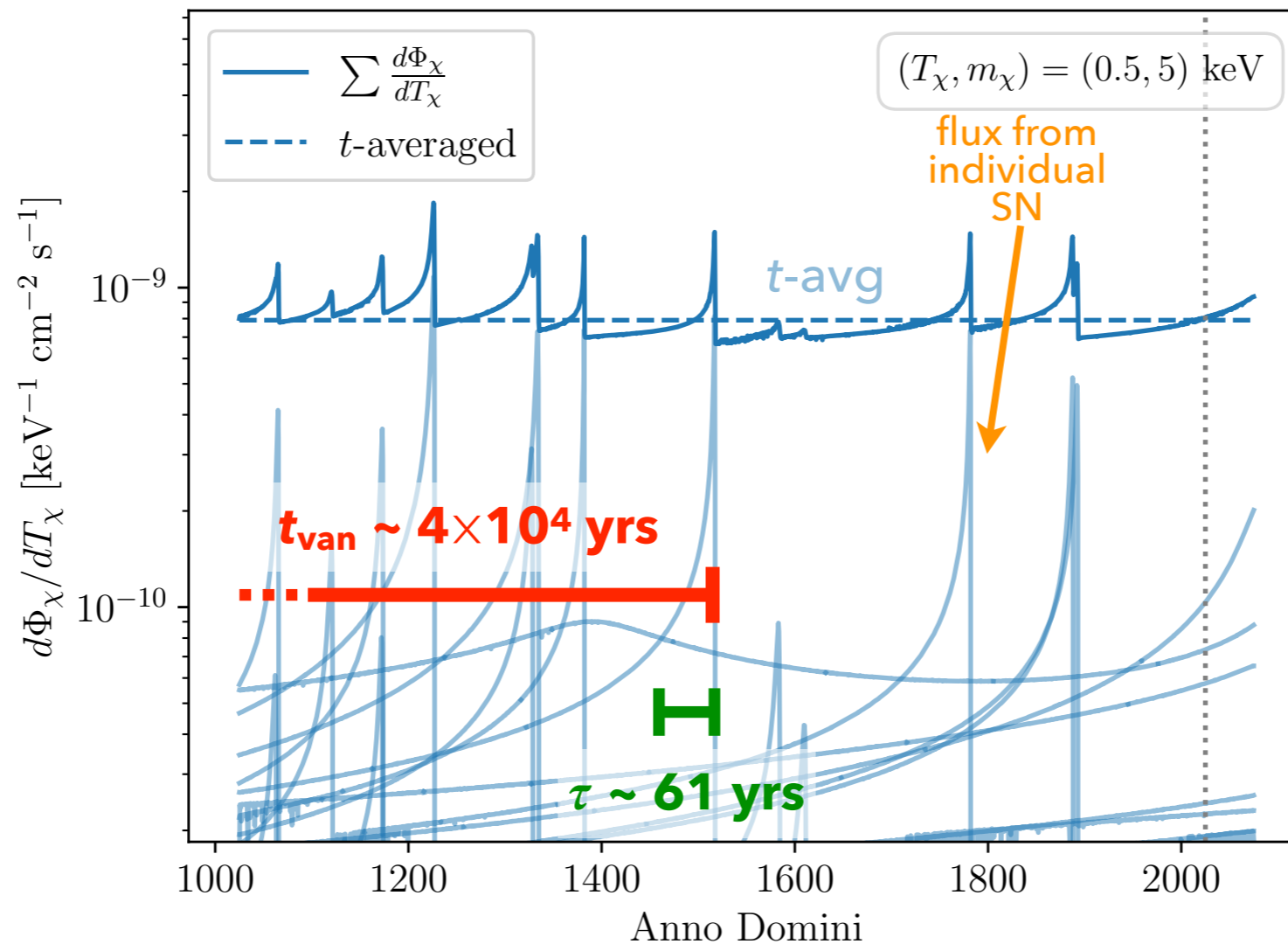
$T_\chi = 500 \text{ keV}$

$m_\chi/T_\chi = 0.01$

Contributed
SN rate:
0.06%

Total BDM flux vs. time

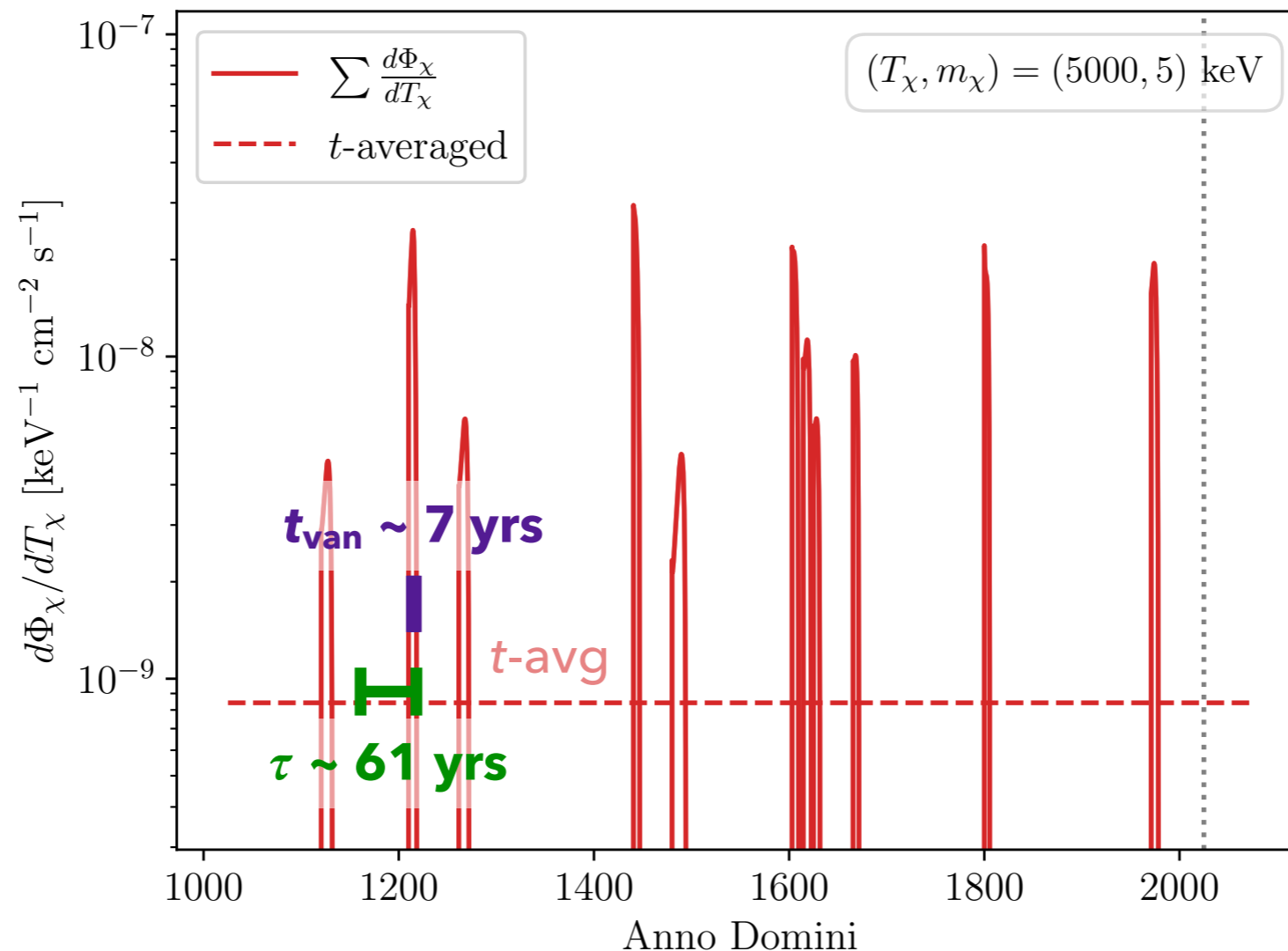
$$m_\chi/T_\chi = 10$$



- Fluxes **overlapped** \rightarrow Manifest **diffuse behavior**
- $t_{\text{van}} \gg \tau \rightarrow m_\chi/T_\chi \gg 0.1$ (non-relativistic) \rightarrow time-averaged approx. is valid

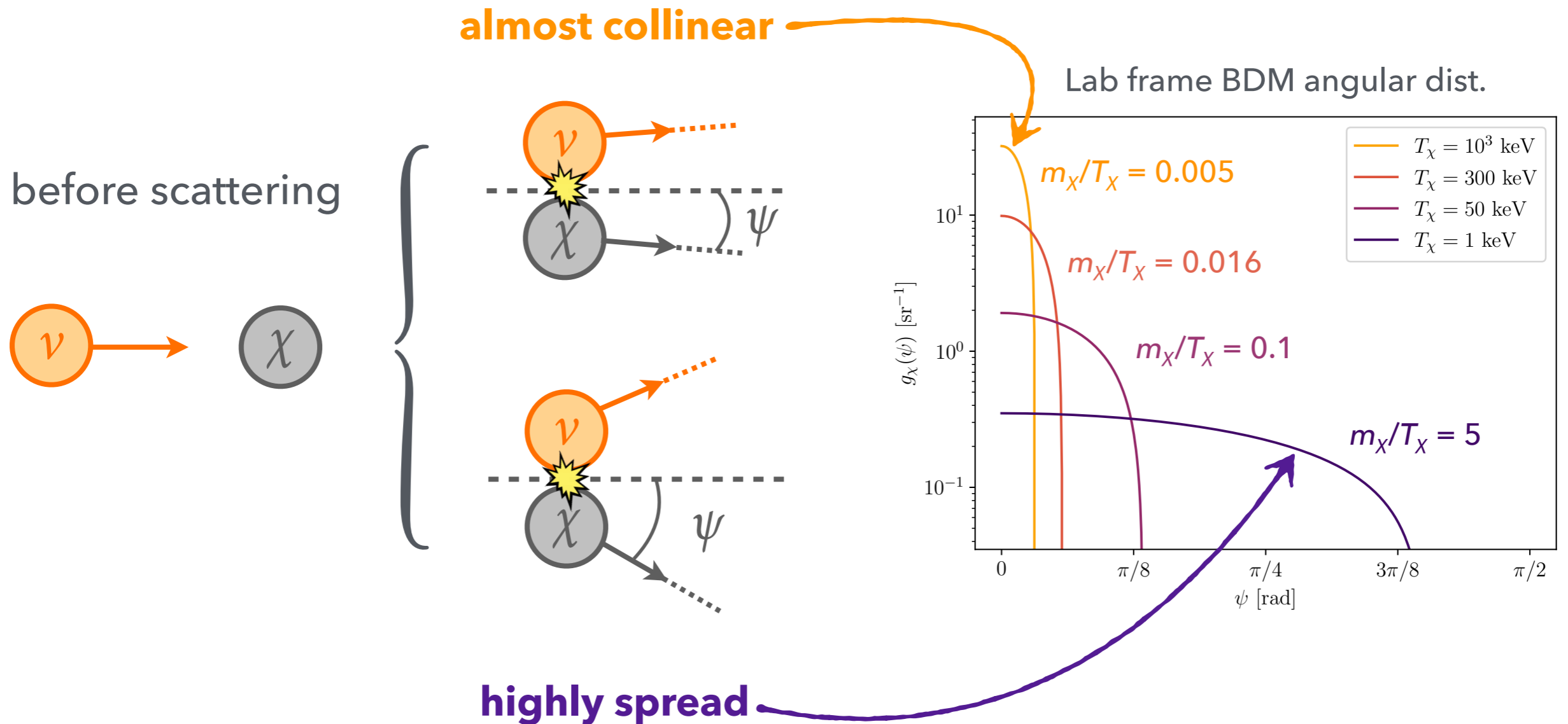
Total BDM flux vs. time

$$m_\chi/T_\chi = 0.001$$



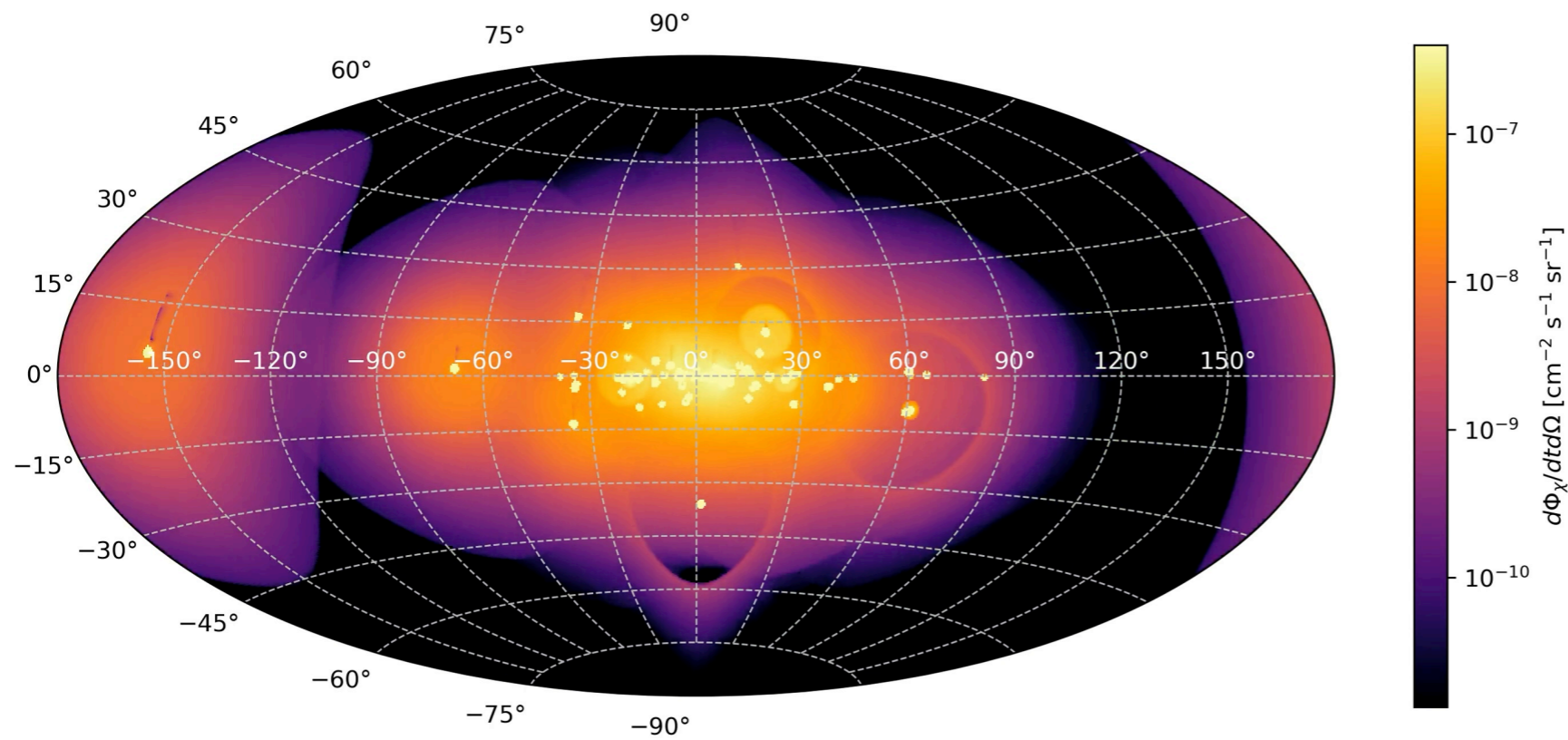
- Fluxes **did not overlap** → Manifest **transient behavior**
- $t_{\text{van}} \ll \tau \rightarrow m_\chi/T_\chi \ll 0.1$ (relativistic) → time-averaged approx. breaks down

The spatial distribution



- $m_\chi/T_\chi \ll 0.1$ BDM is highly collinear with the incoming neutrino
- $m_\chi/T_\chi \gtrsim 0.1$ BDM would be much spread in the space after scattering

Year 54089

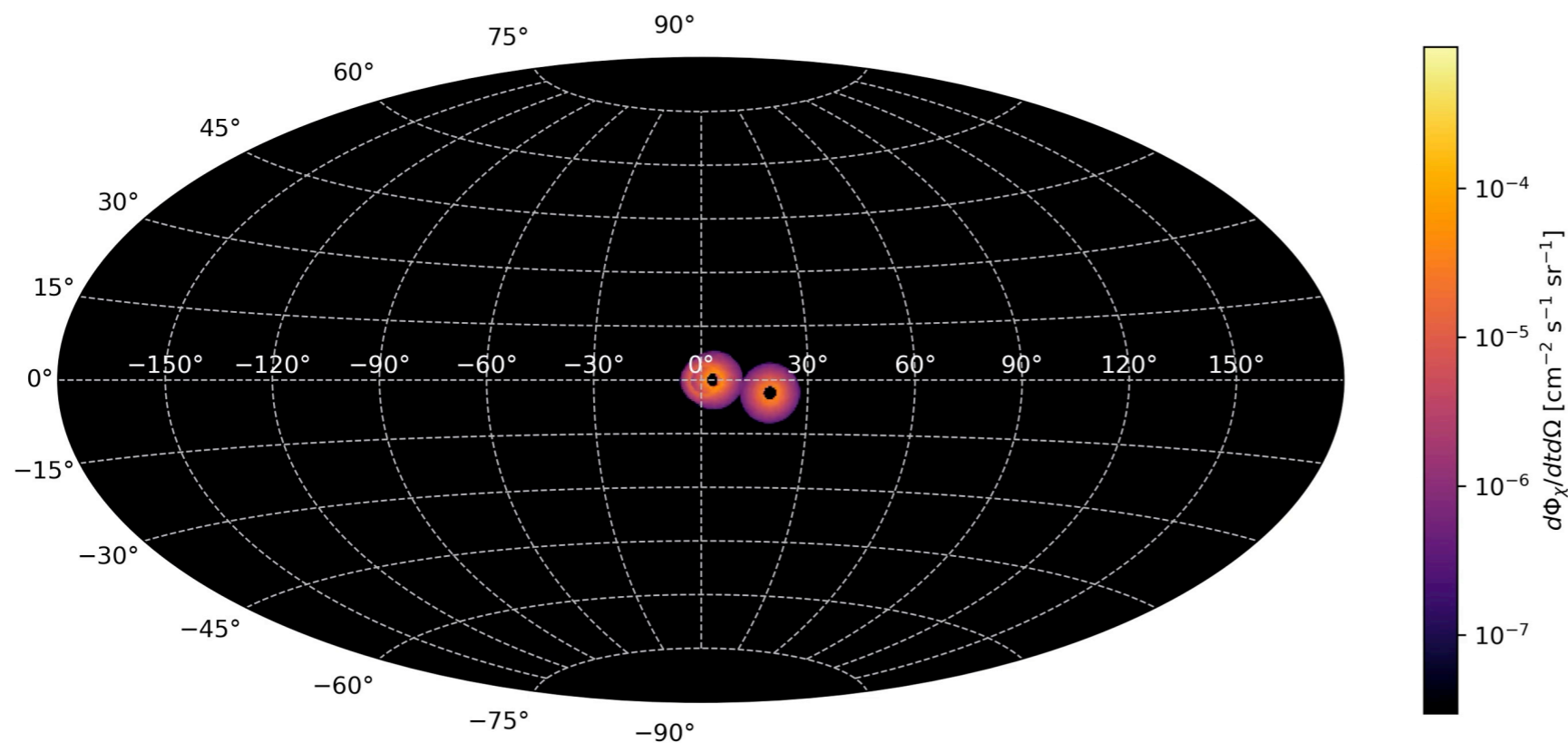


Non-relativistic
 $T_X \in [1, 5] \text{ keV}$
 $m_X/T_X \in [0.1, 1]$

To animation page

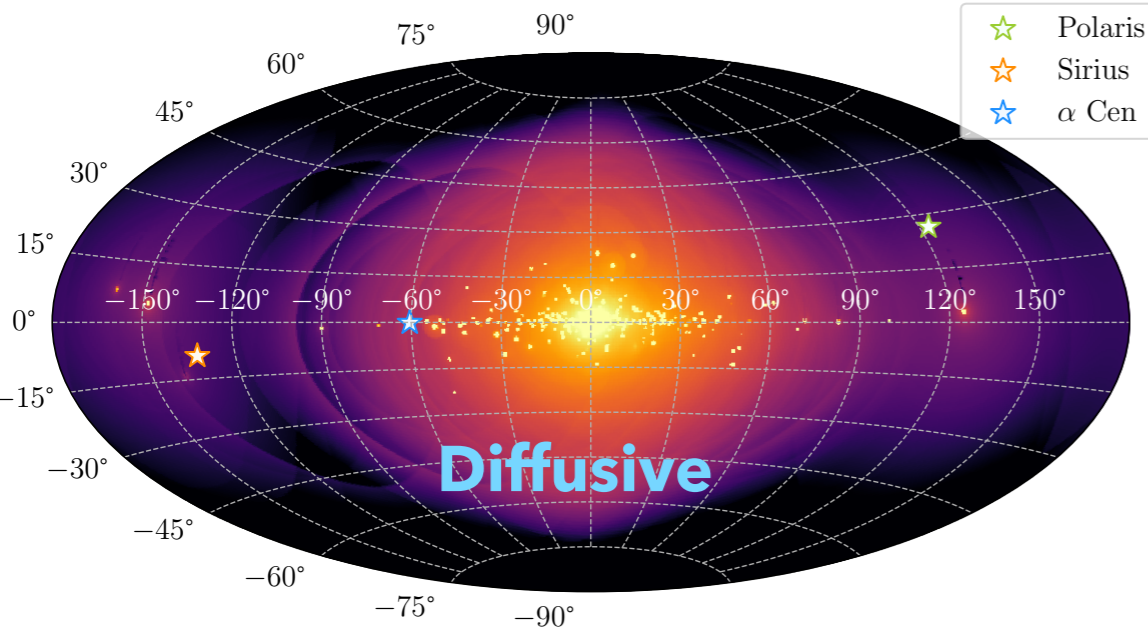


Year 54089

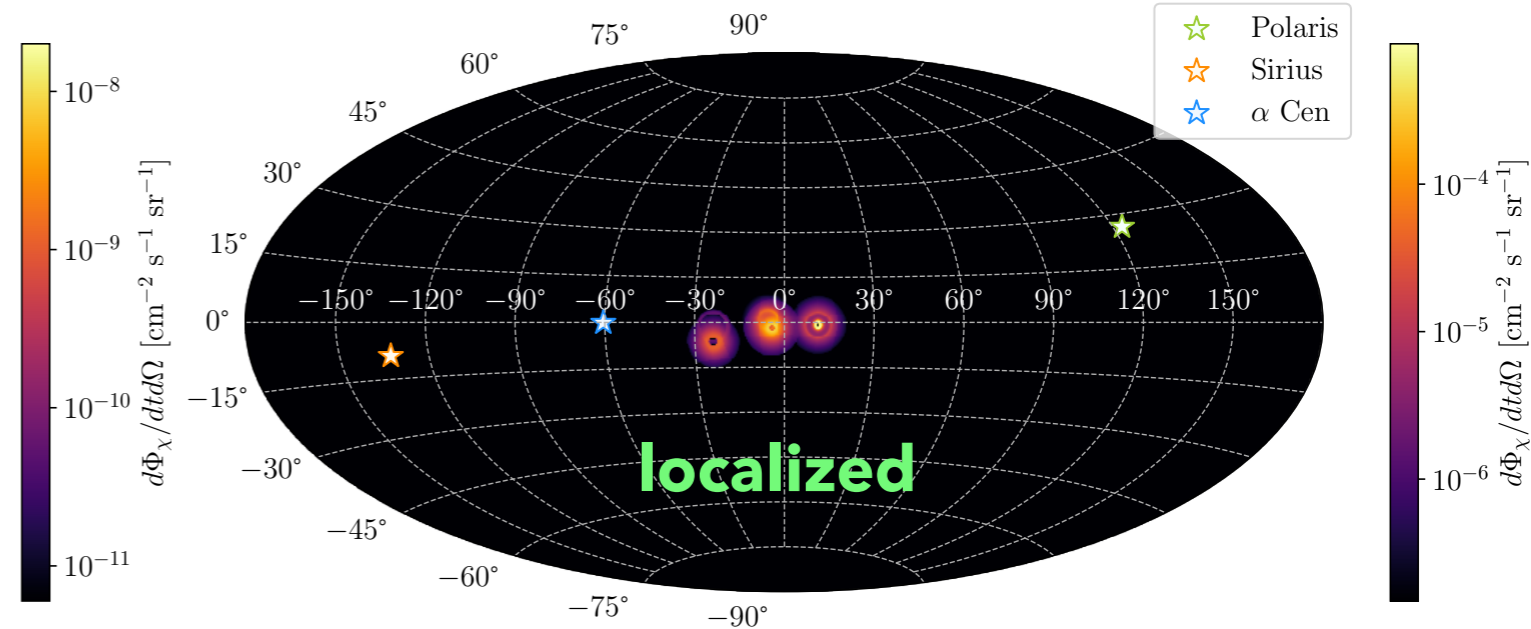


Relativistic
 $T_X \in [300, 1000] \text{ keV}$
 $m_X/T_X \in [0.005, 0.016]$

$$(T_{\chi,\min}, T_{\chi,\max}) = (1, 5) \text{ keV}$$



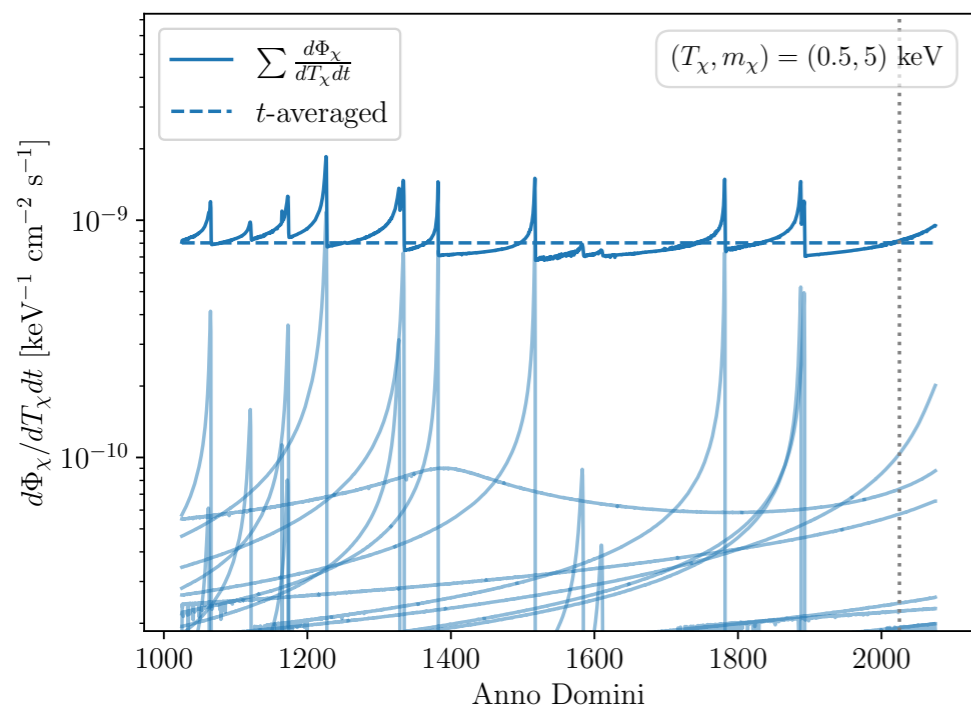
$$(T_{\chi,\min}, T_{\chi,\max}) = (300, 1000) \text{ keV}$$



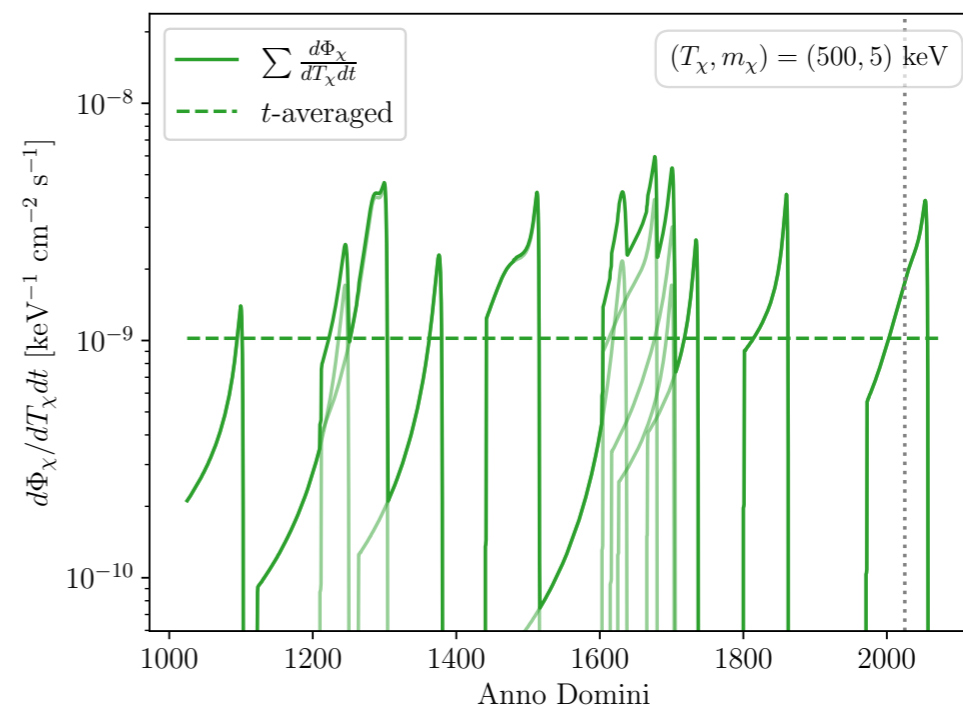
→ Distribution across the spatial dimension

Where and **when** to look for the signature

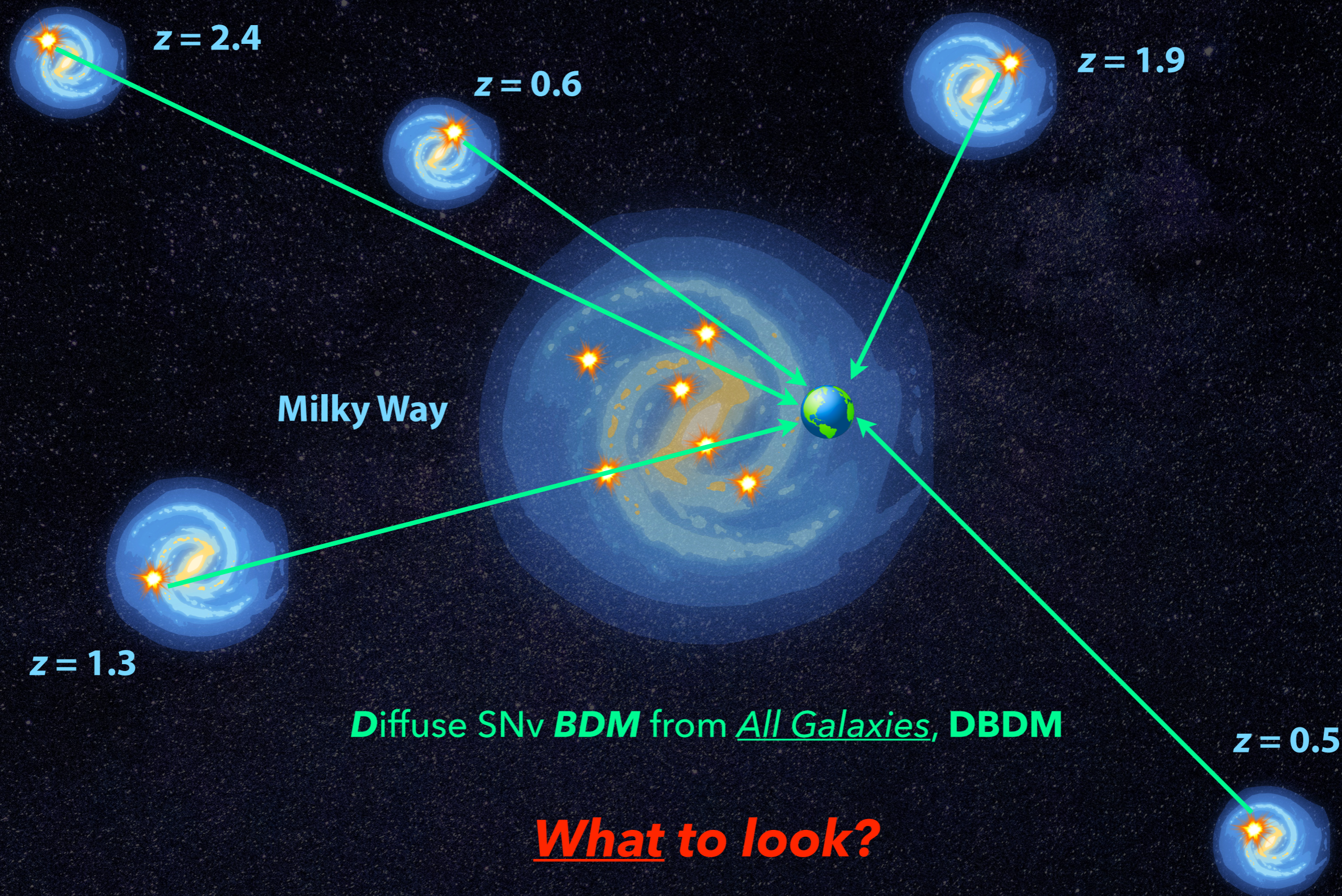
→ Distribution across the temporal dimension



$$m_{\chi}/T_{\chi} \gtrsim 0.1$$



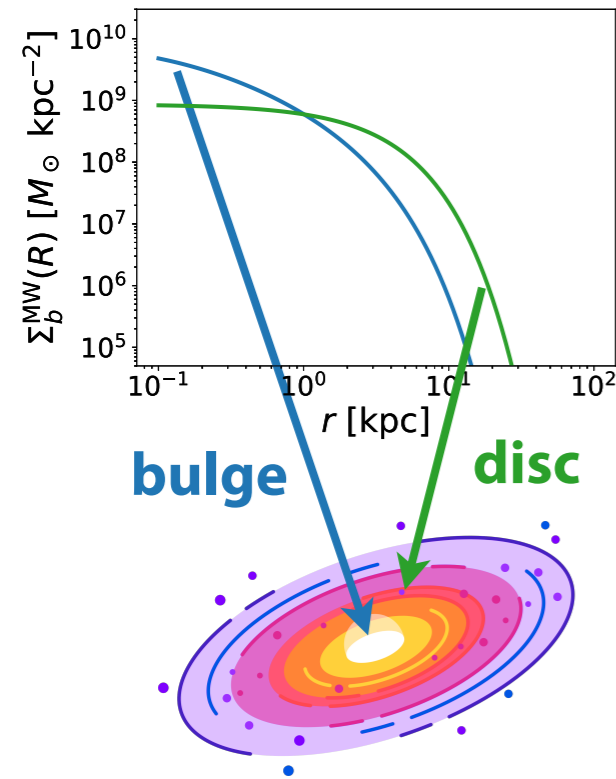
$$m_{\chi}/T_{\chi} \ll 0.1$$



Diffuse SNIv **BDM** from All Galaxies, **DBDM**

What to look?

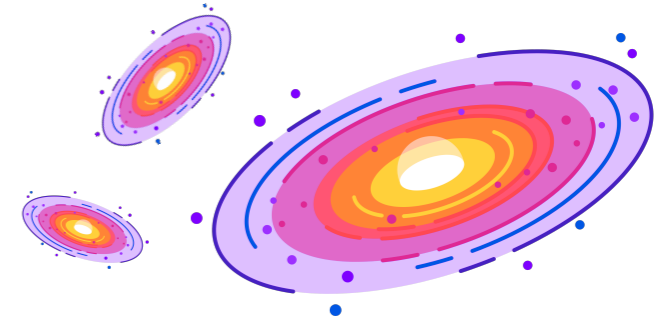
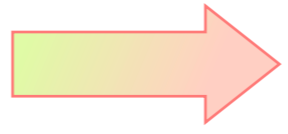
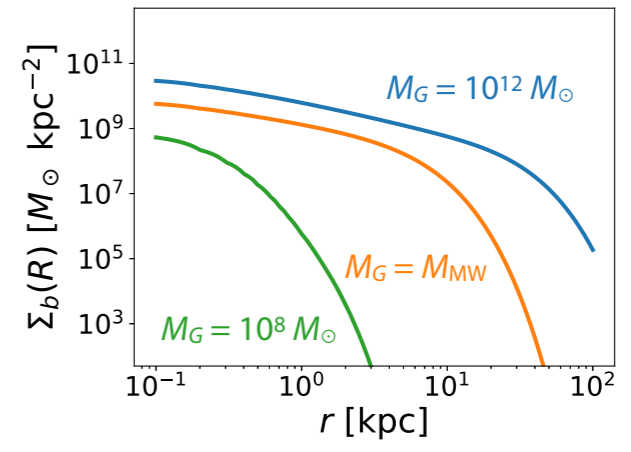
DBDM or local MW diffuse flux



McMillan 2017

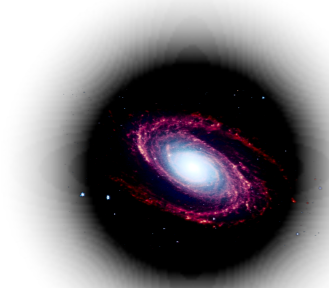
$$\rho_b(R, h) = \frac{\rho_{0,b}}{[1 + r'(R, h)/r_0]^\alpha} e^{-\frac{r'^2(R, h)}{r_{cut}^2}}$$

$$\rho_d(R, h) = \frac{\Sigma_0}{2h_d} e^{-\frac{|h|}{h_d} - \frac{R}{R_d}}$$



The DBDM flux

MW

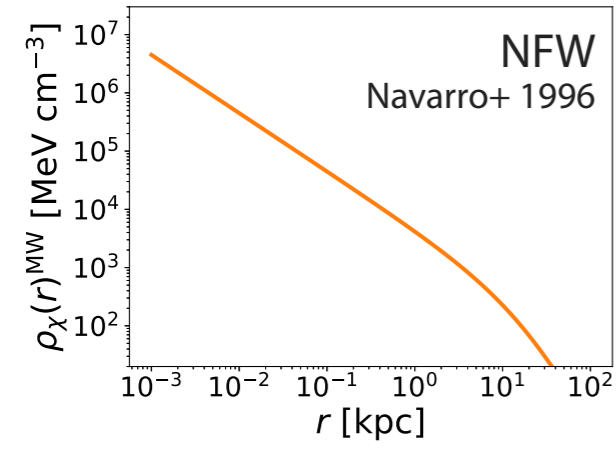


$$\frac{d\Phi_\chi}{dT_\chi} = \frac{v_\chi}{H_0} \int_0^{z_{max}} \frac{dz}{\epsilon(z)} \int dM_G \frac{d\Gamma_{SN}(z)}{dM_G} \frac{d\bar{N}_\chi(M_G)}{dT'_\chi}$$

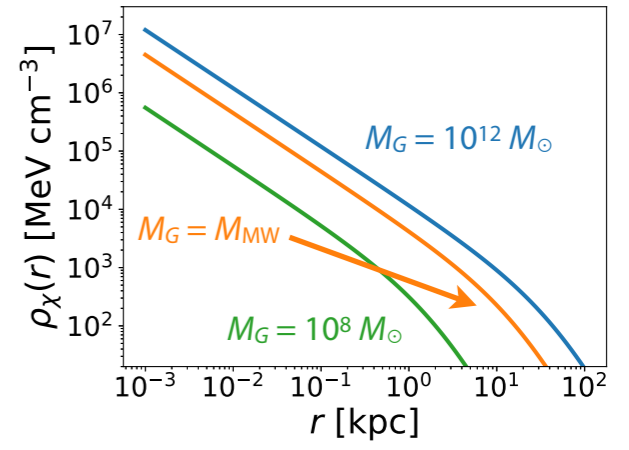
Arbitrary galaxy



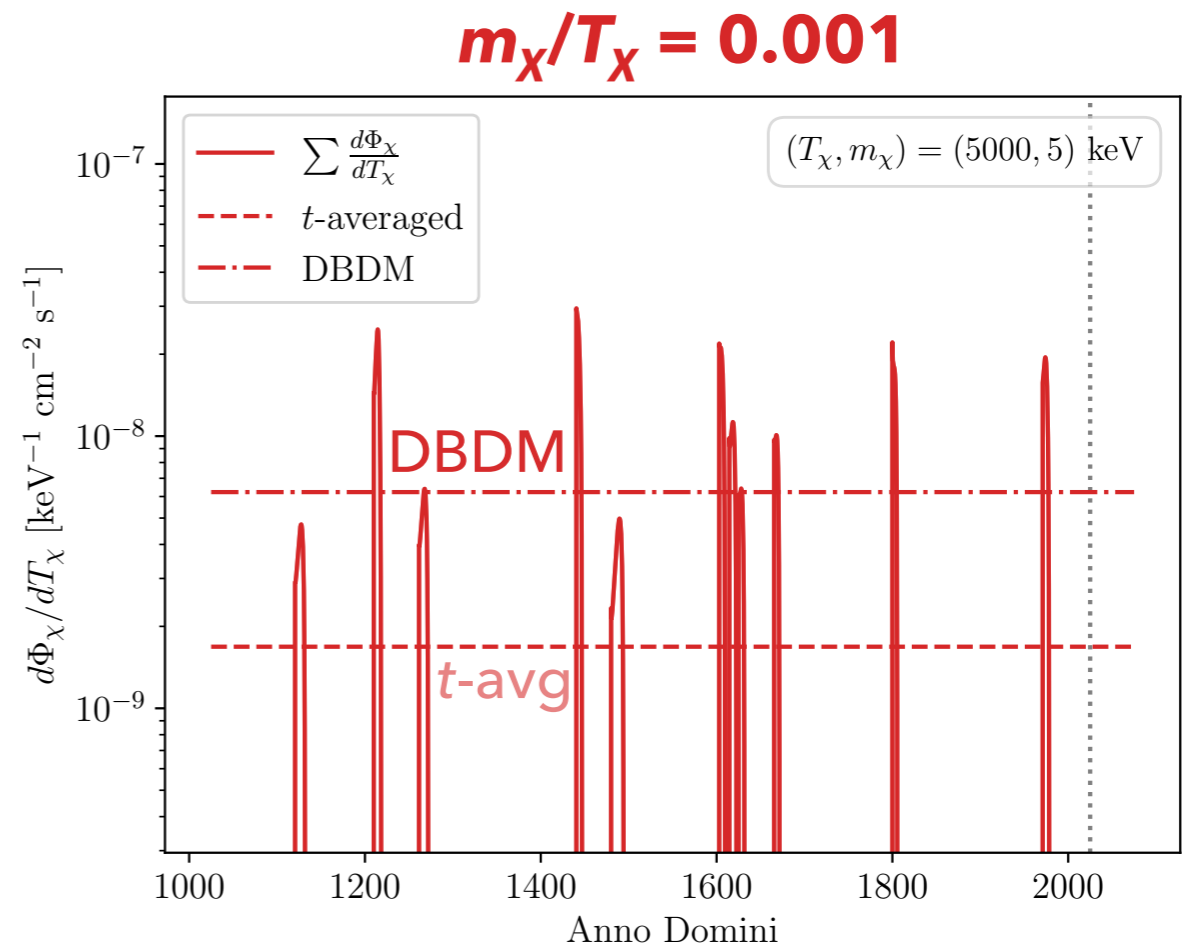
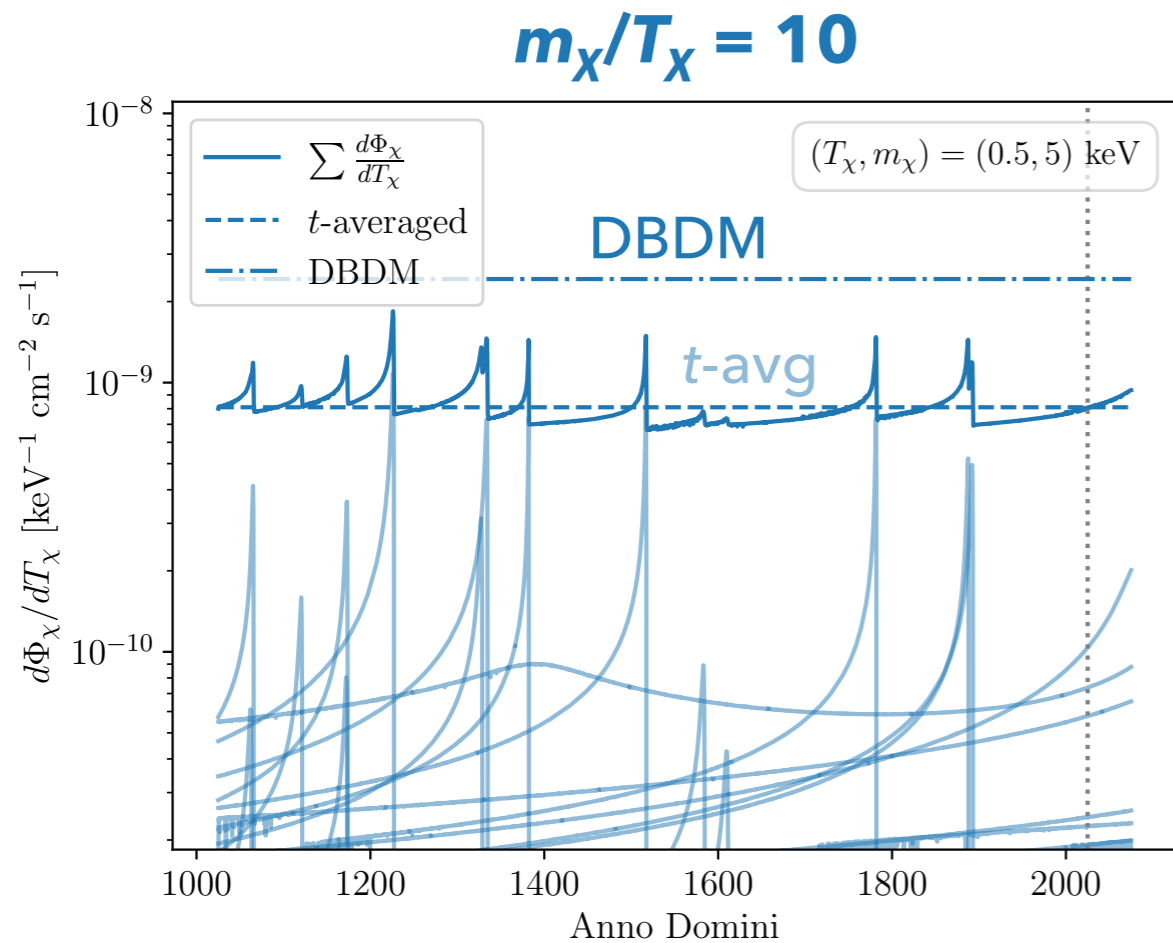
$M_{halo} = \eta M_G$
 $\eta \sim 20 - 50$
 Moster+ 2010
 Grielli+ 2020



$$\rho_\chi(r) = \frac{\rho_s}{\frac{r}{r_s} (1 + \frac{r}{r_s})^n}$$

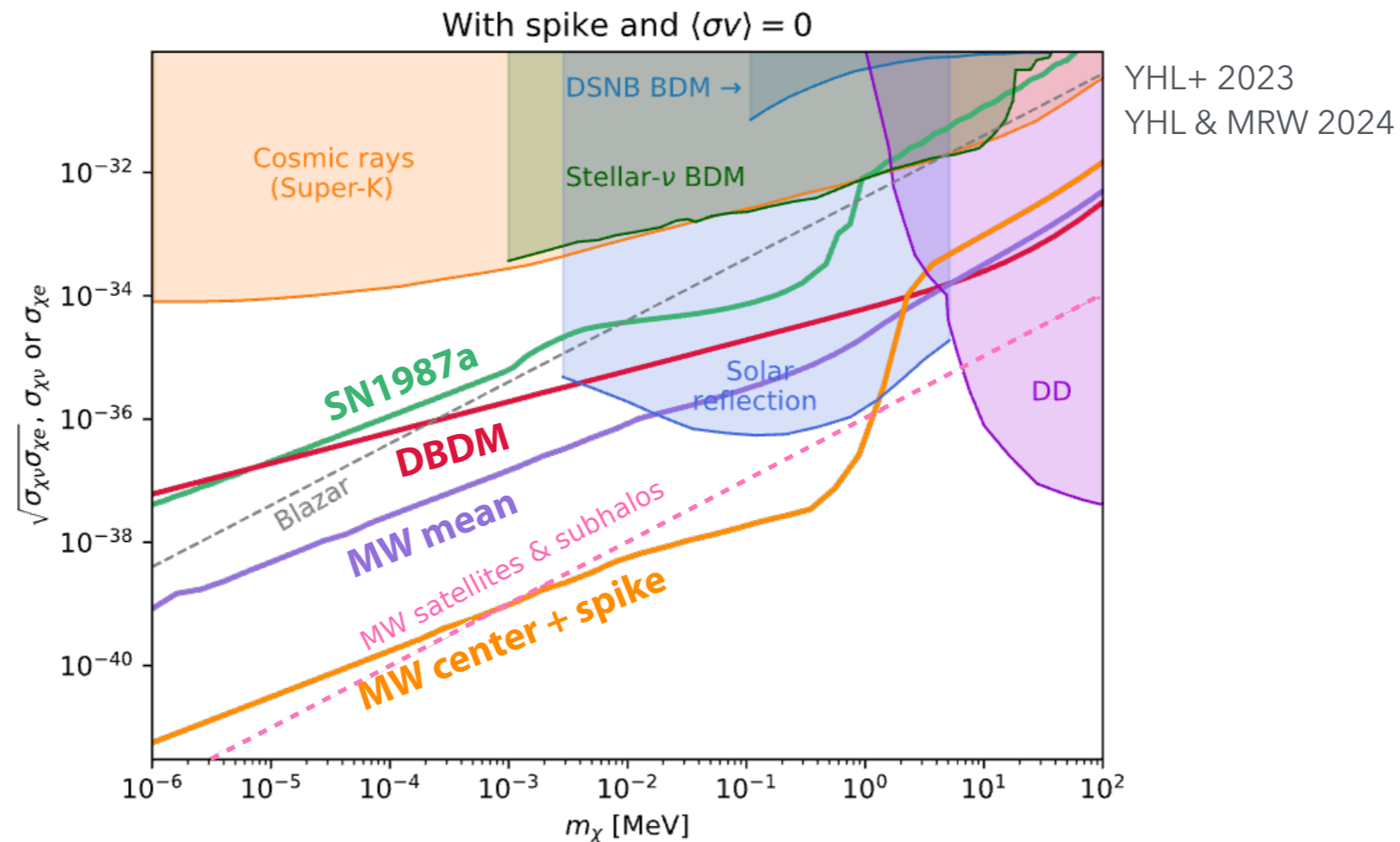


Flux revisited

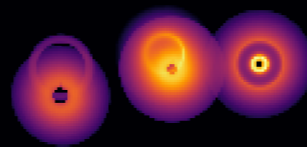


- DBDM flux $>$ MW t -averaged flux when $m_\chi/T_\chi > 0.1$ (non-relativistic)
- BDM flux from individual SN $>$ DBDM flux when $m_\chi/T_\chi \ll 0.1$ (relativistic)

Constraints & sensitivities



- Assuming energy-independent cross sections and $\sigma_{\chi\nu} = \sigma_{\chi e}$
- SN1987a 90%CL in Kamioka + Super-K
- 2-sigma projected sensitivity in Hyper-K



Summary

- **BDM signature from individual SN (next galactic SN)**

- ▶ Time-dependent feature can be used to measure DM mass directly

$$m_\chi \simeq 9.7 \text{ keV} \times \left(\frac{t_p}{10 \text{ days}} \right)^{1/2} \left(\frac{T_\chi}{10 \text{ MeV}} \right)$$

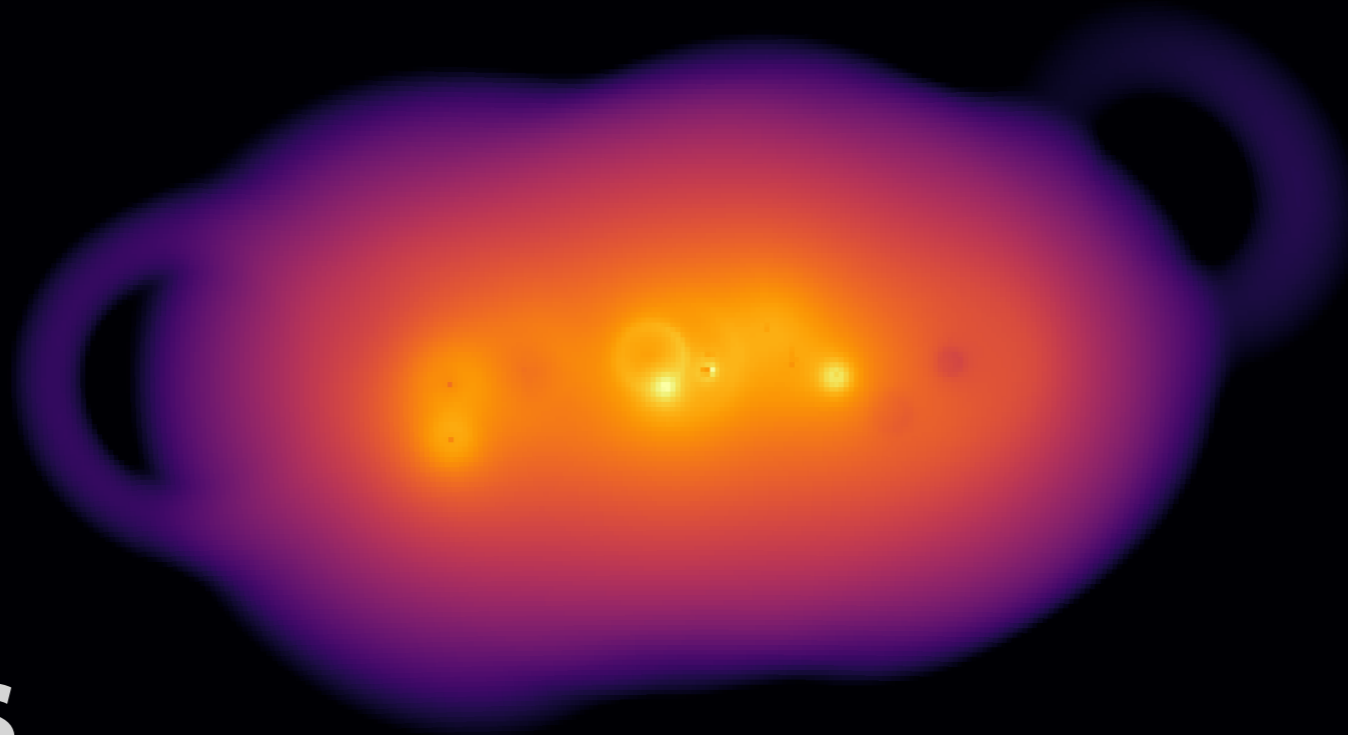
- ▶ Suppressing the background accumulation → enhancing the sensitivity

- **BDM flux behaves diffusively or not that depends on m_χ/T_χ (t_{van}/τ)**

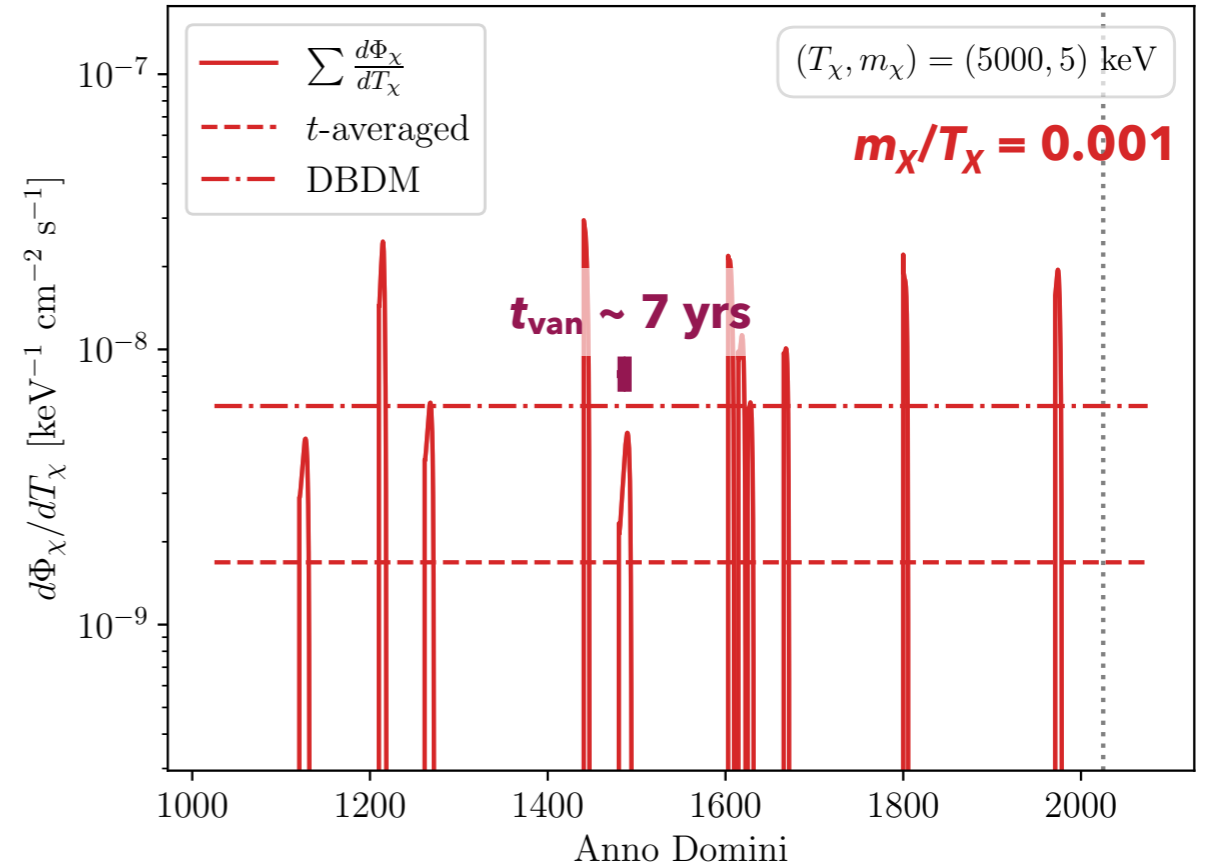
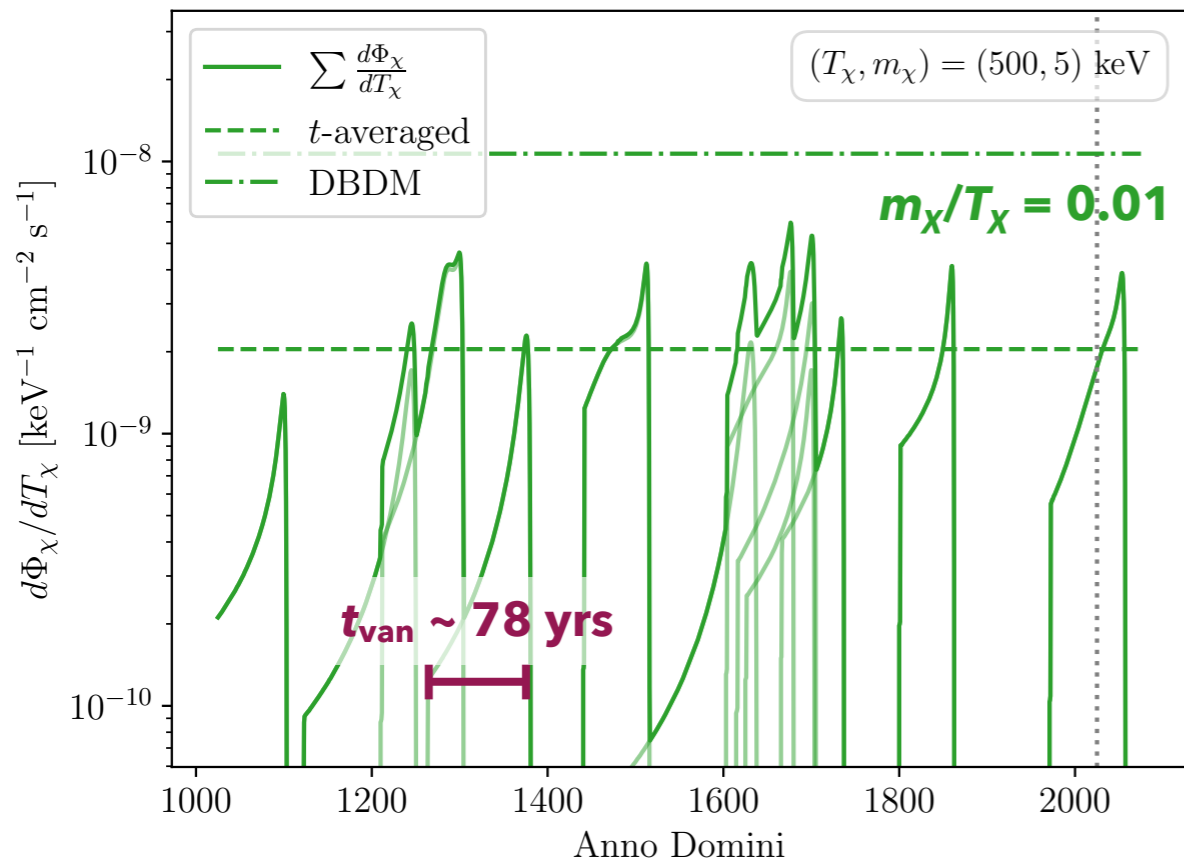
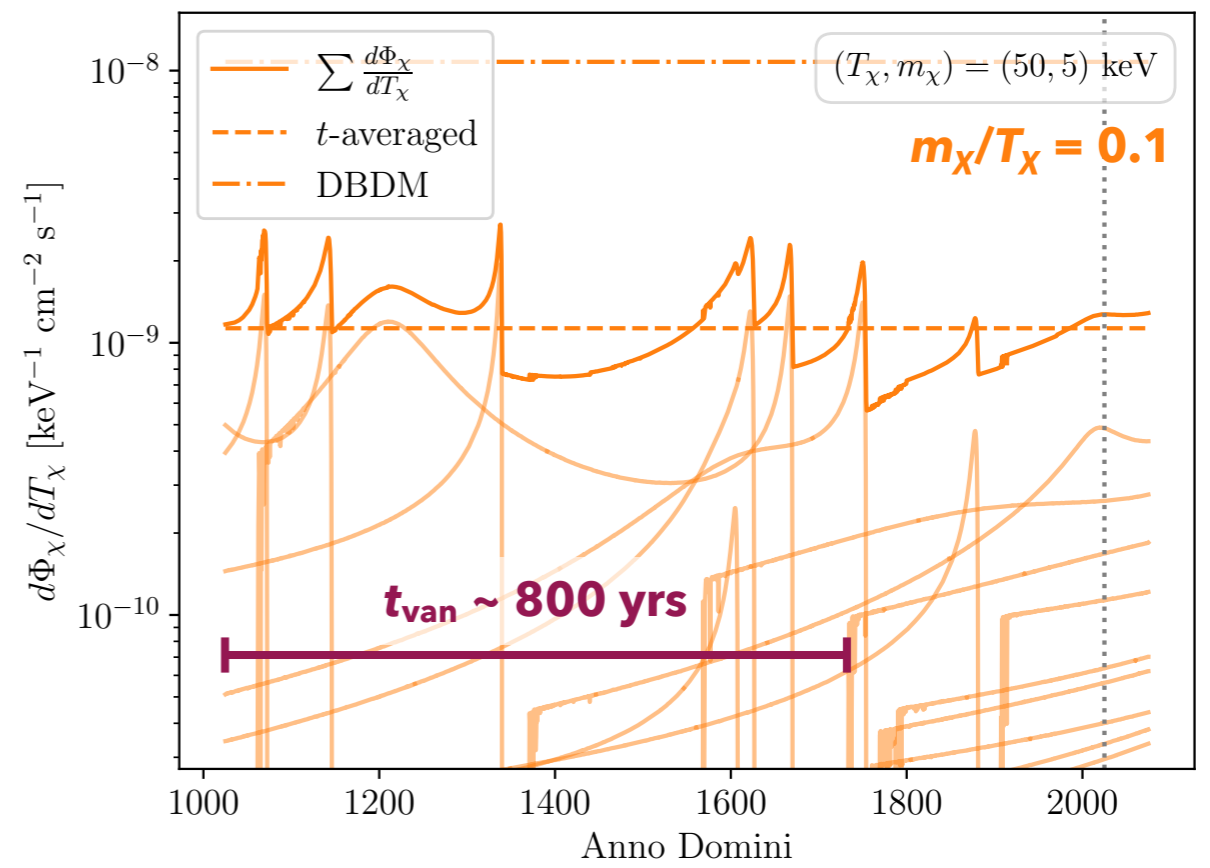
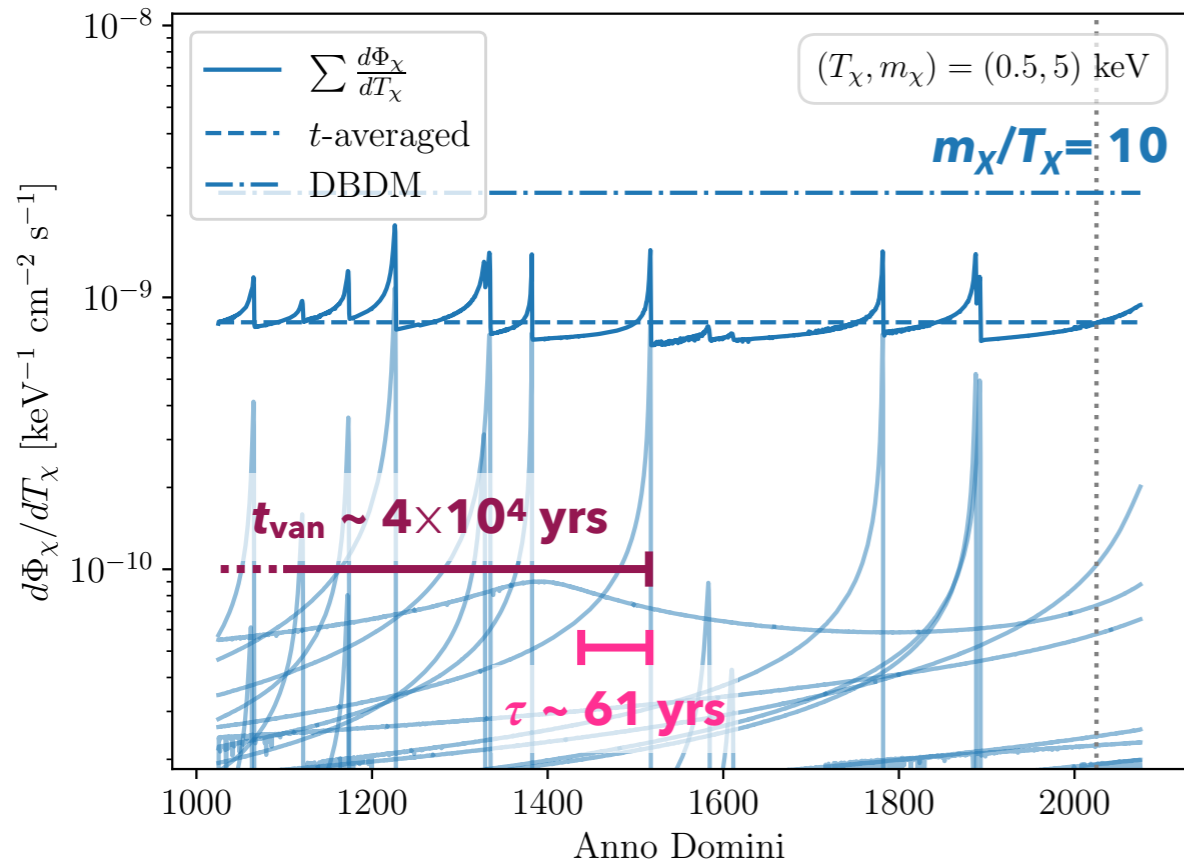
- **What BDM component is more promising to look for**

- ▶ Diffuse SNv BDM from all galaxies (DBDM) provides better constraint
- ▶ Next galactic SN will offer exciting opportunity for BDM search

Backups

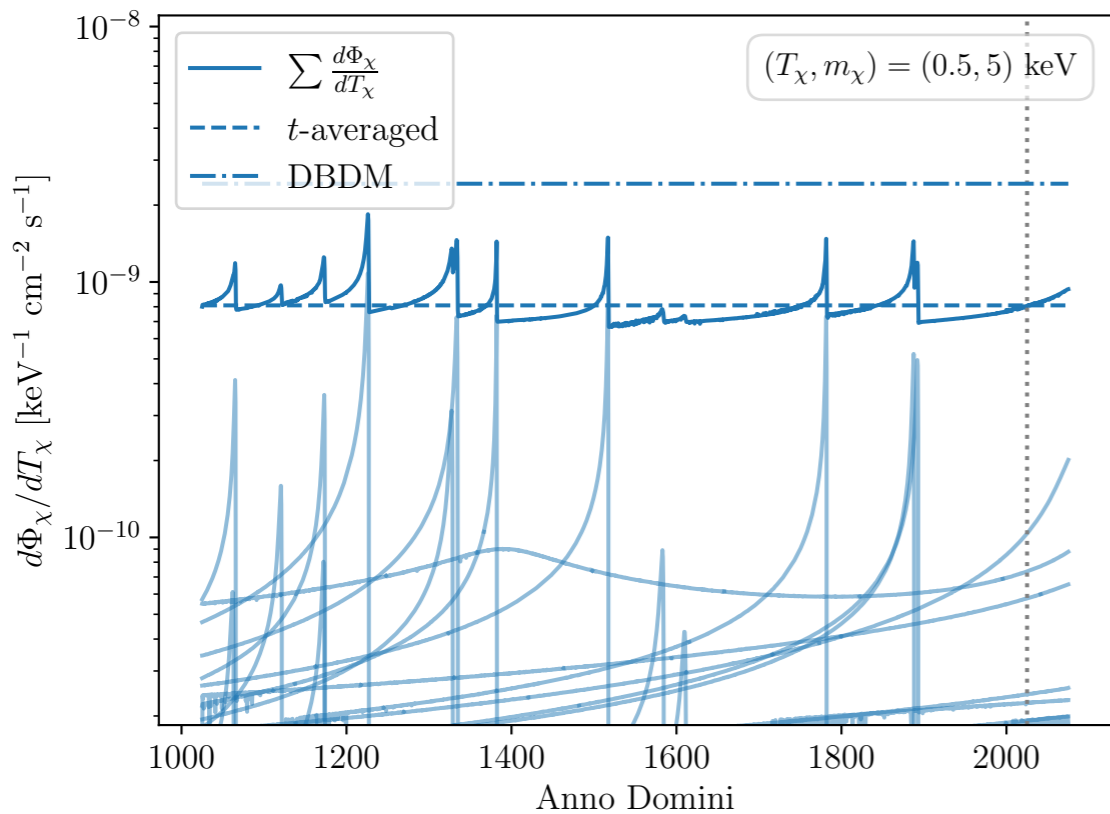


Total BDM flux vs. time

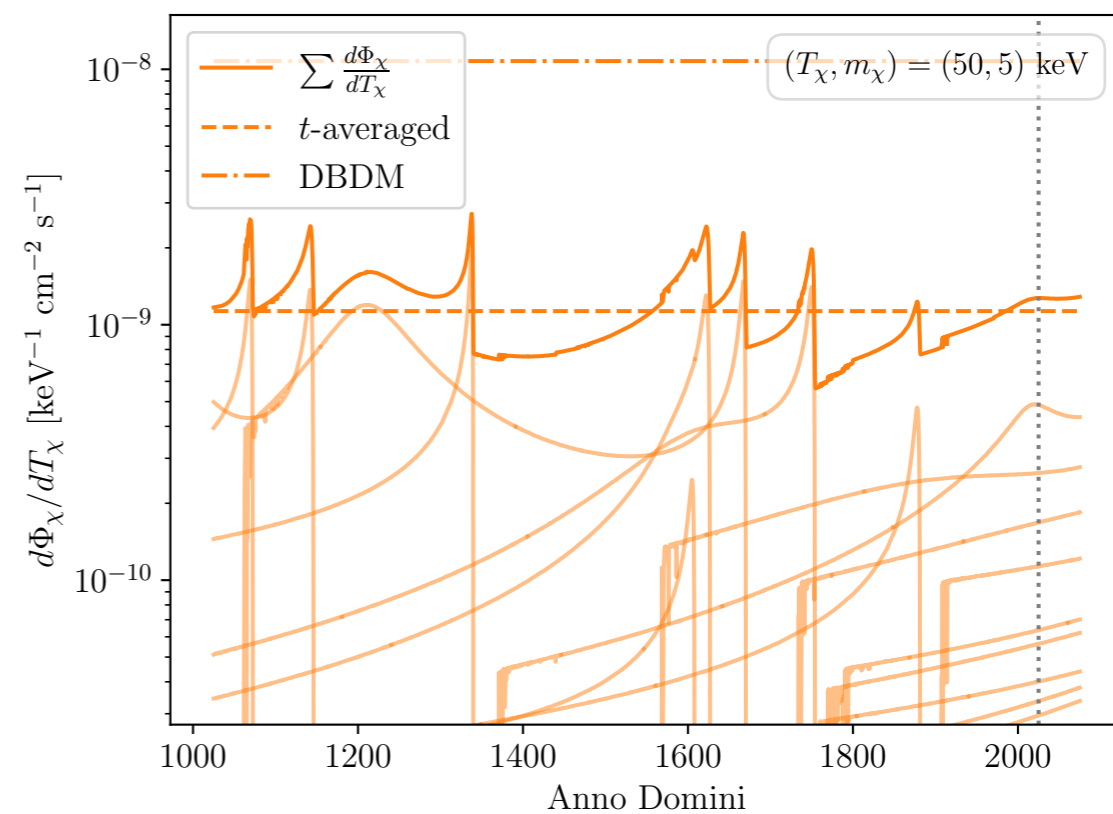


$T_\chi \sim \mathcal{O}(\text{keV})$

$m_\chi/T_\chi = 10$

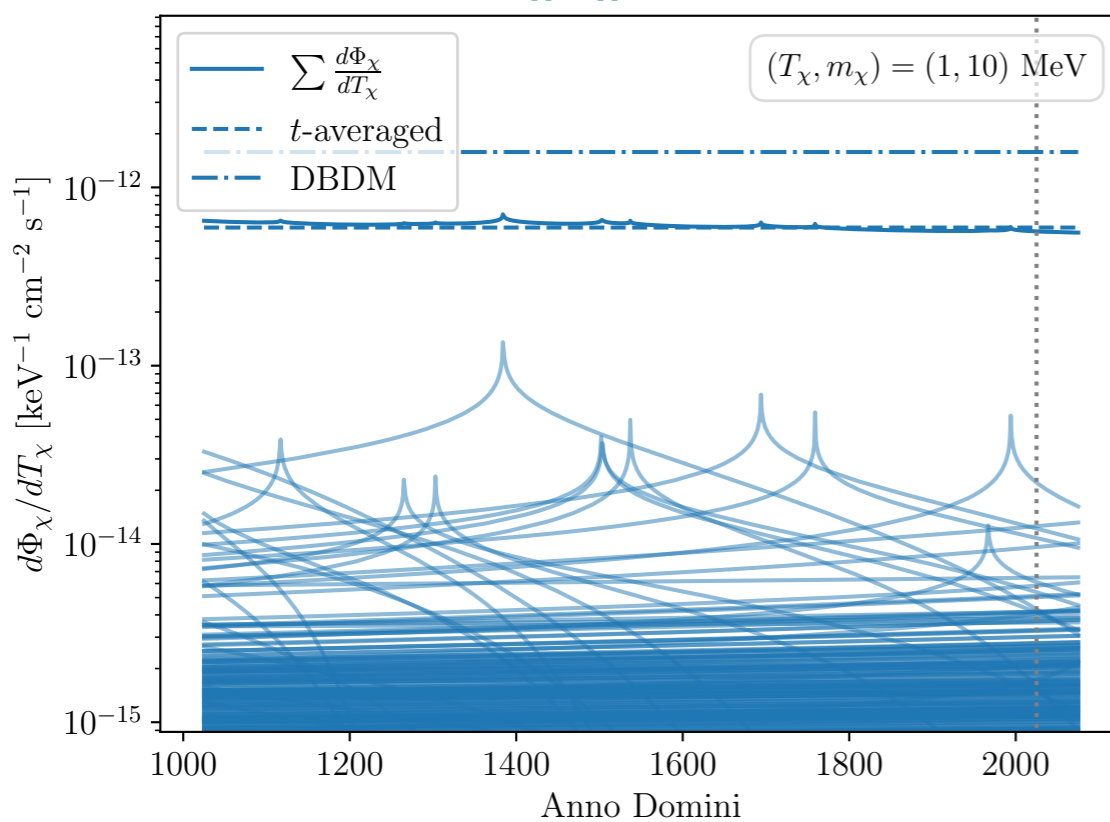


$m_\chi/T_\chi = 0.1$

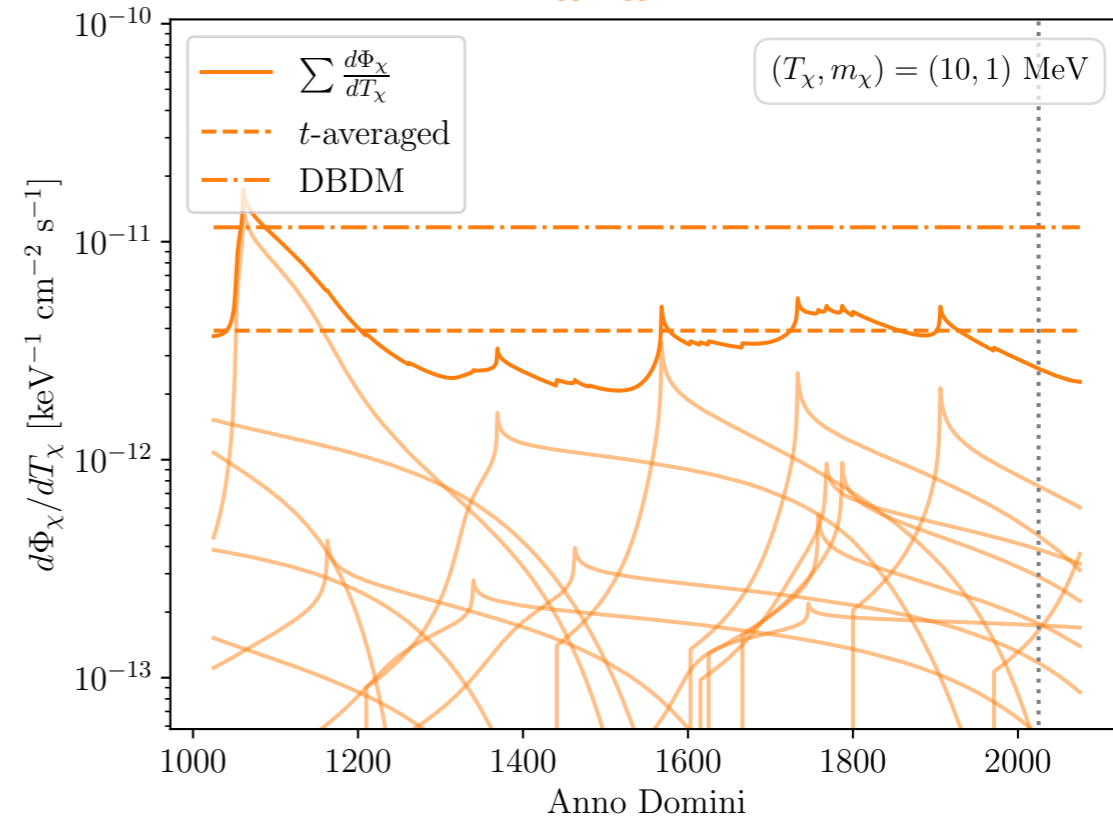


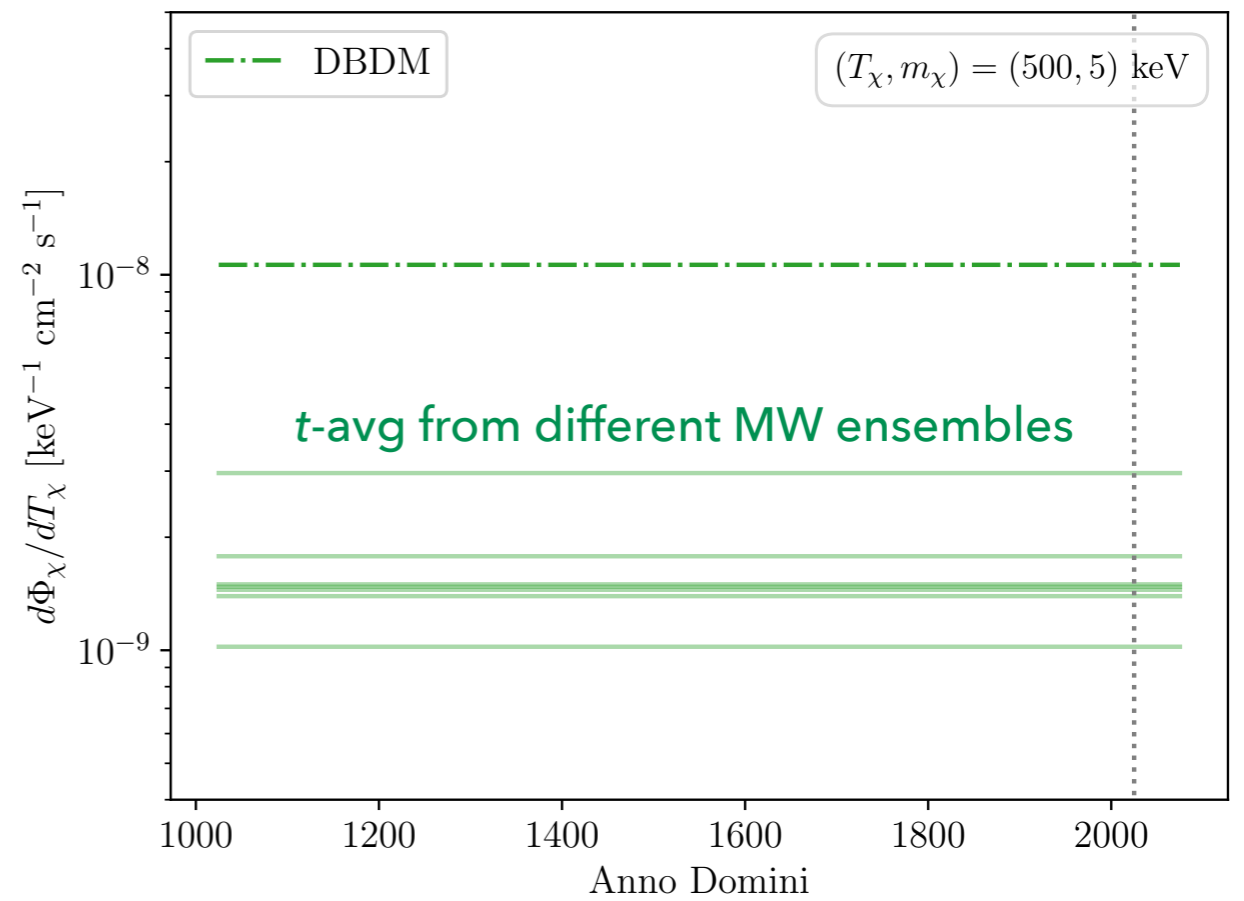
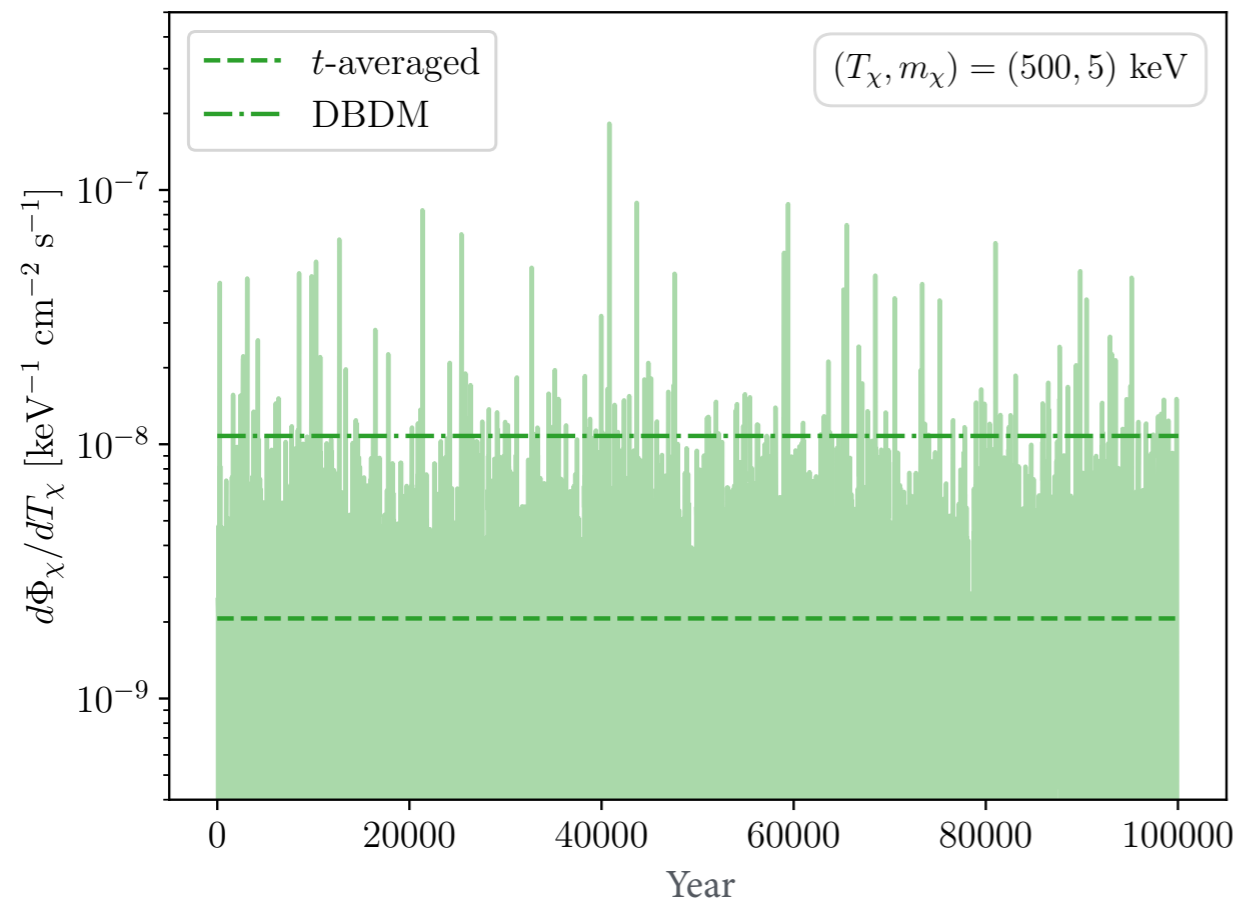
$T_\chi \sim \mathcal{O}(\text{MeV})$

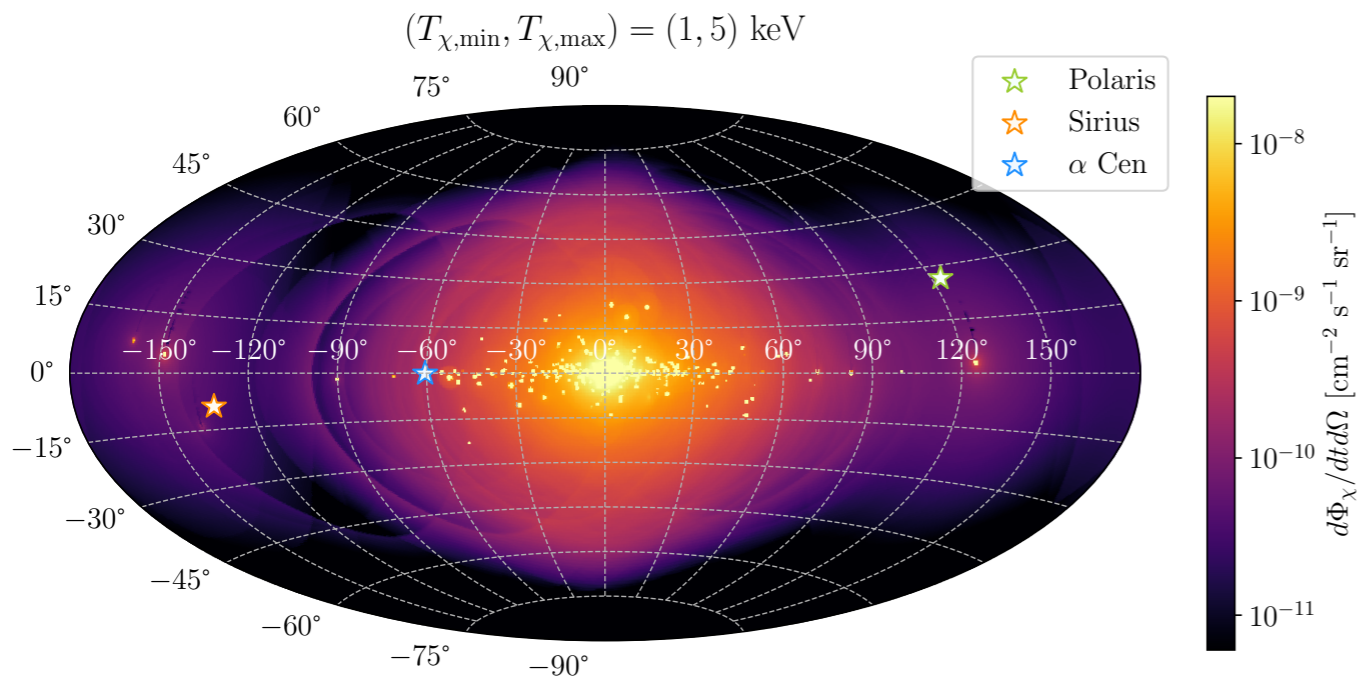
$m_\chi/T_\chi = 10$



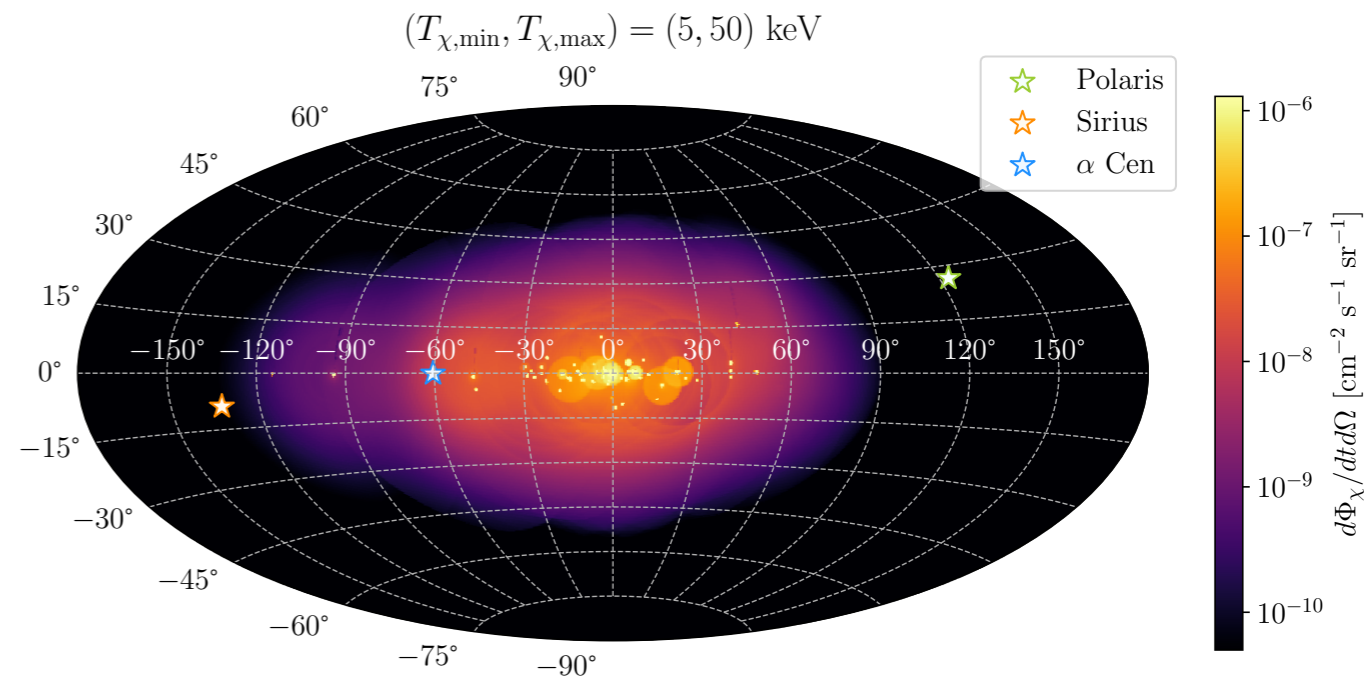
$m_\chi/T_\chi = 0.1$





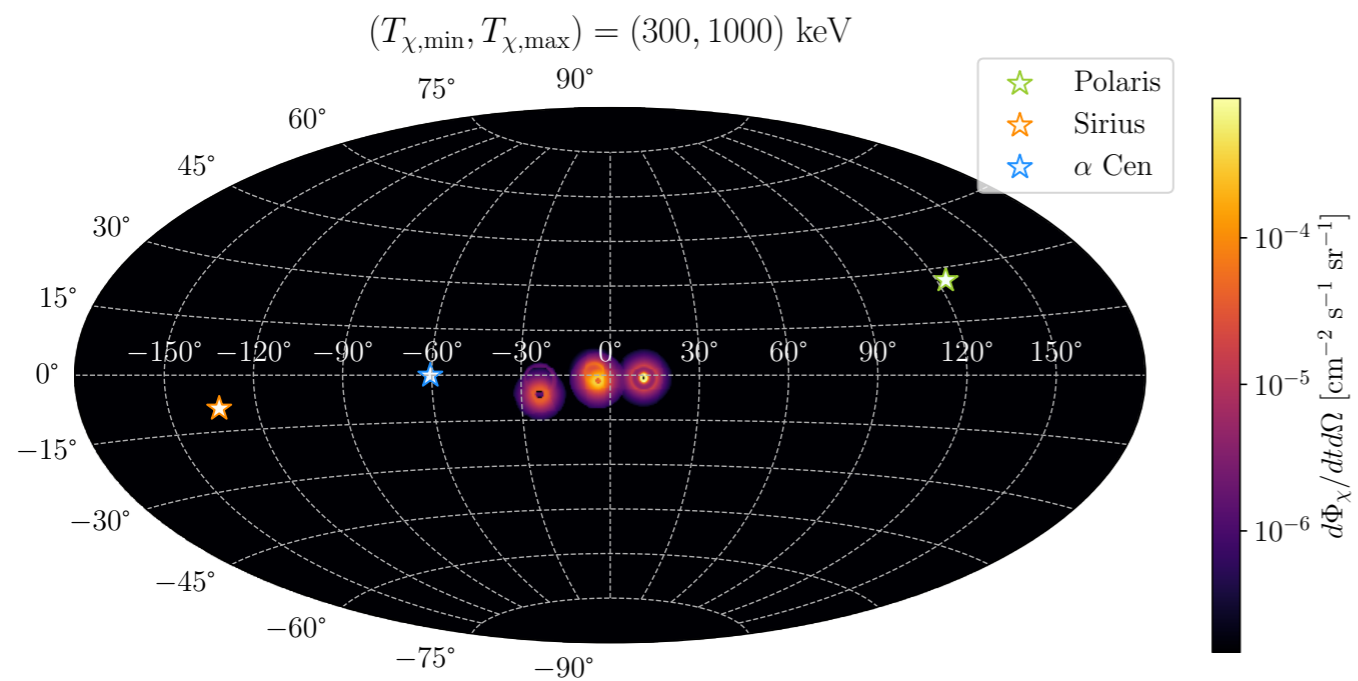


$m_{\chi}/T_{\chi} \in [1, 5]$

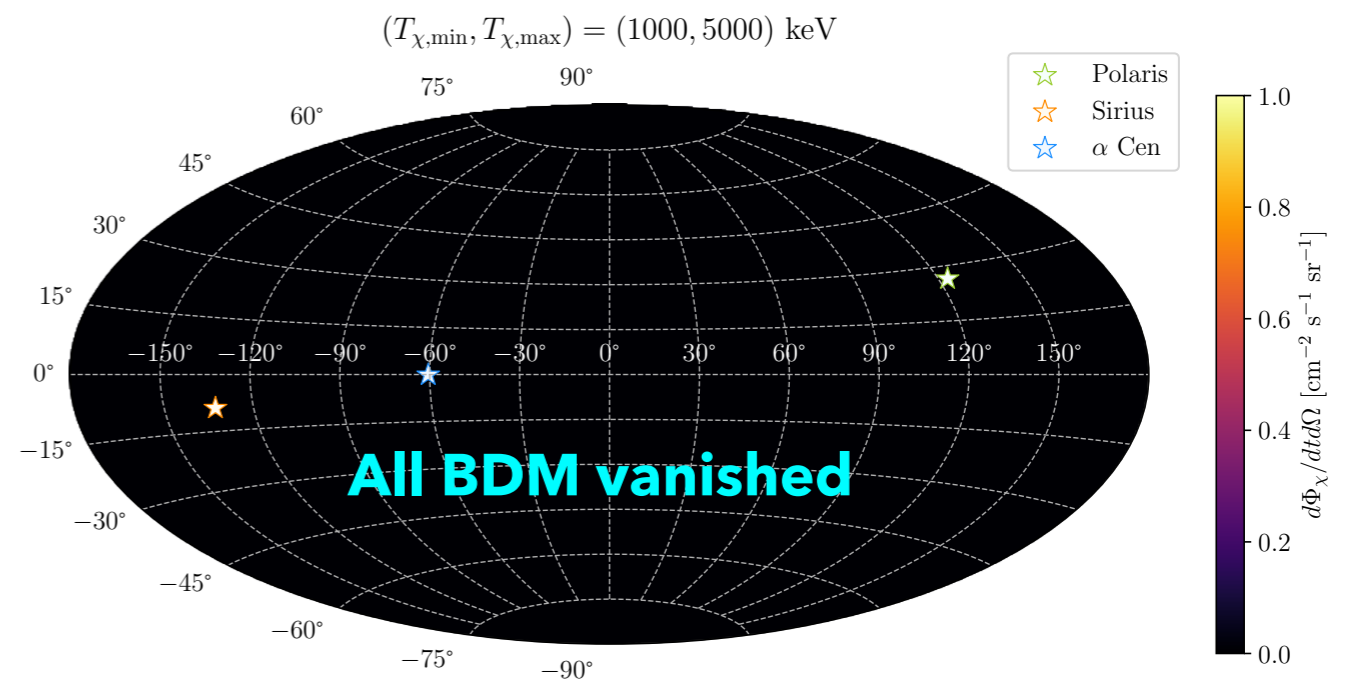


$m_{\chi}/T_{\chi} \in [0.1, 1]$

$m_{\chi}/T_{\chi} \in [0.005, 0.016]$

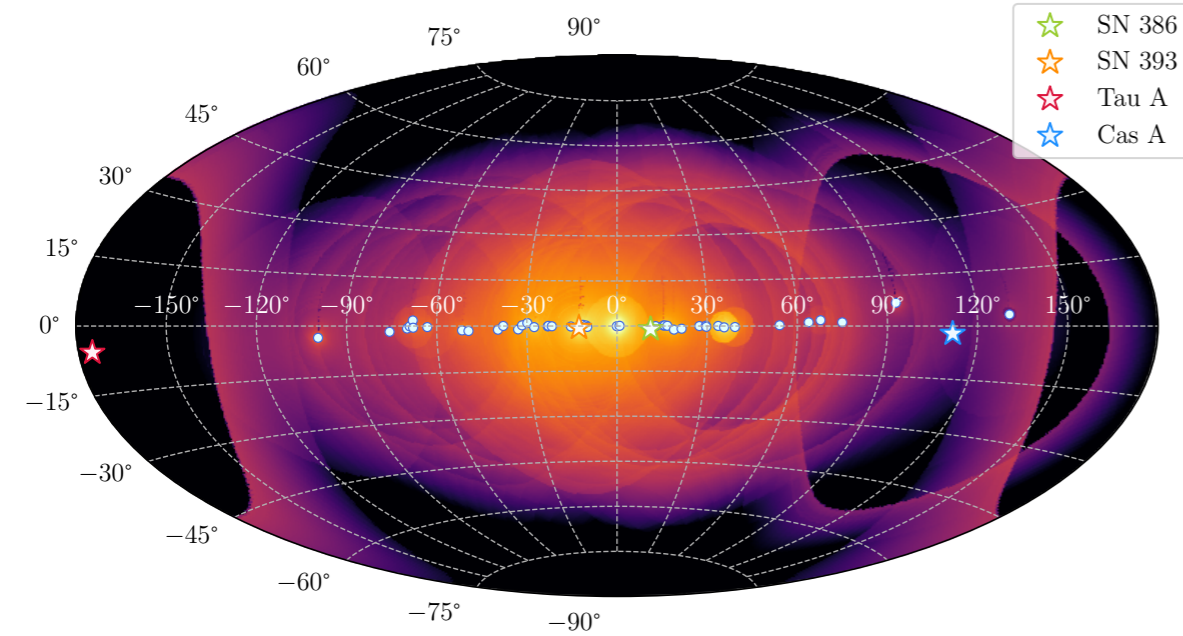


$m_{\chi}/T_{\chi} \in [0.005, 0.001]$



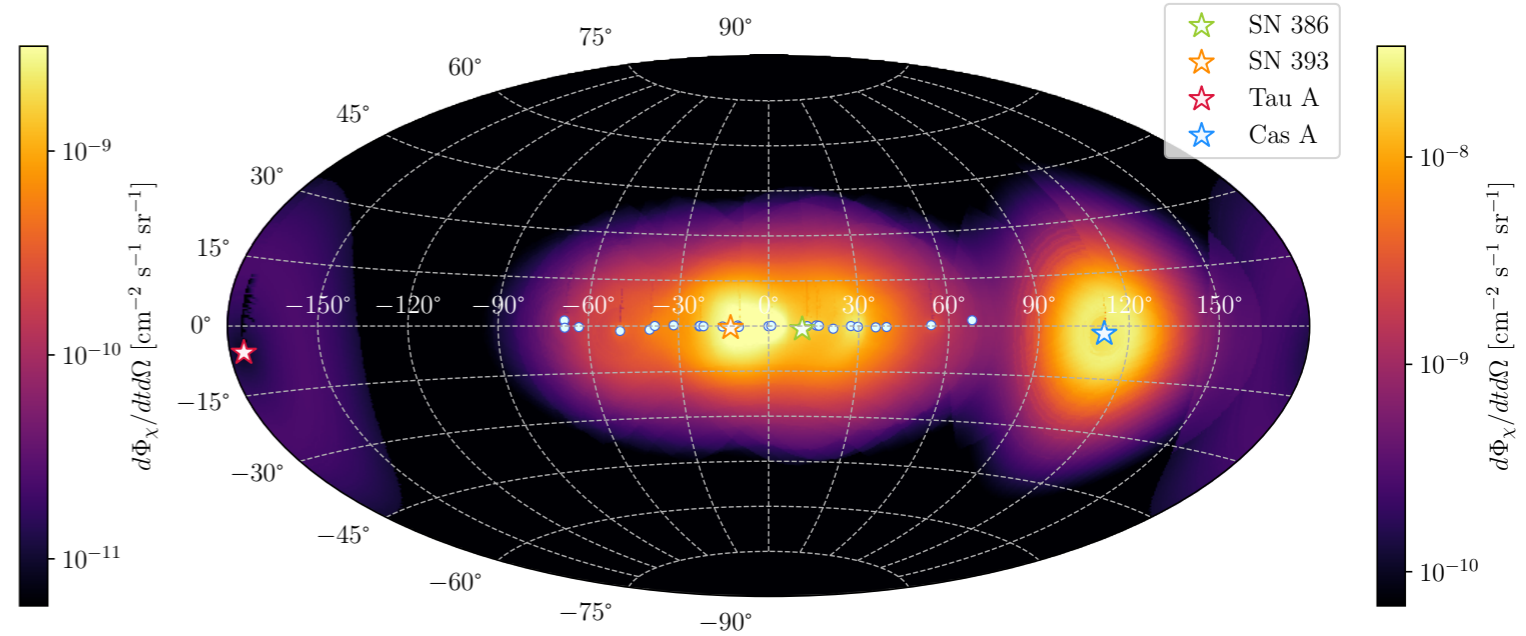
BDM from documented SNRs

SNRcat: $(T_{\chi,\min}, T_{\chi,\max}) = (1, 5)$ keV



$m_{\chi}/T_{\chi} \in [1, 5]$

SNRcat: $(T_{\chi,\min}, T_{\chi,\max}) = (5, 50)$ keV



$m_{\chi}/T_{\chi} \in [0.1, 1]$

