



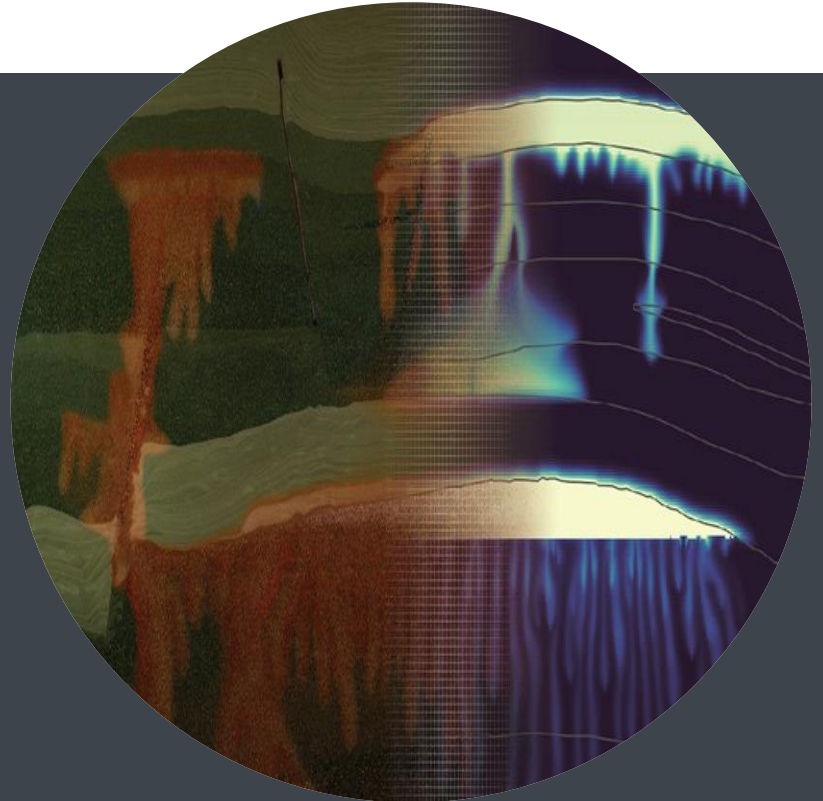
**Universität Stuttgart**

Institute for Modelling Hydraulic and Environmental Systems  
Department of Hydromechanics and Modelling of Hydrosystems

# Benchmarking Computational Models for GCS

Bernd Flemisch

Workshop "Mathematical and numerical modeling  
of CO<sub>2</sub> storage", Rueil-Malmaison, 01.02.2023



# Outline

1. Motivation
2. Categorization
3. Selected GCS Benchmark Studies
  - a. The Classic
  - b. So Simple, Yet So Hard
  - c. Reality Meets Modeling
  - d. Back To Normal, But Bigger
4. Summary and Conclusion

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1. **Motivation**
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**Essentially all models  
are wrong,  
... but some are useful**

**George Box**

”



**One of the most influential statisticians of the 20<sup>th</sup> century and a pioneer in the areas of quality control, time series analysis and design of experiments and Bayesian inference.**

# Motivation

## Model Assessment

- Why do we even bother then?
- Because „Some are Useful“.
- But ... How do we know a model is „Useful“?
- We consider a model "useful" if it provides:
  - enhanced insight into a problem,
  - a means to test a theory/hypothesis.
- What are the approaches to determine if a model is "useful"?

# Motivation

## Model Assessment

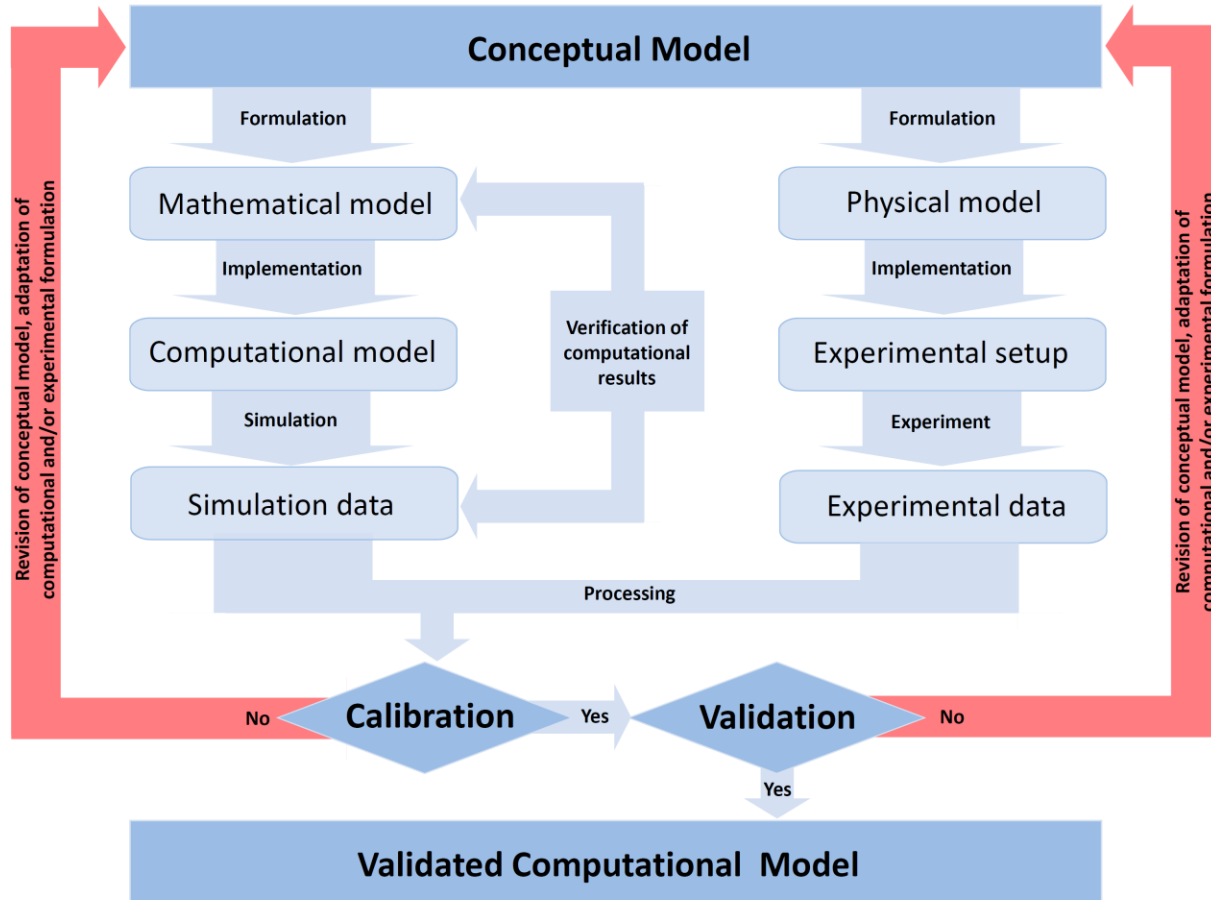
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- But ... How do we know a model is „Useful“?
- We consider a model "useful" if it provides:
  - enhanced insight into a problem,
  - a means to test a theory/hypothesis.
- What are the approaches to determine if a model is "useful"?
  - **Common Methods: Verification and Validation.**

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# Categorization

## Process of Model Development





# Categorization

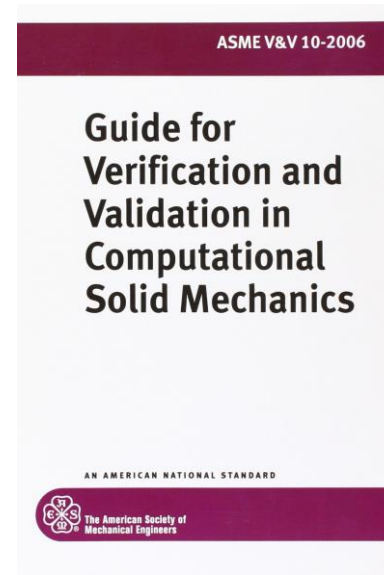
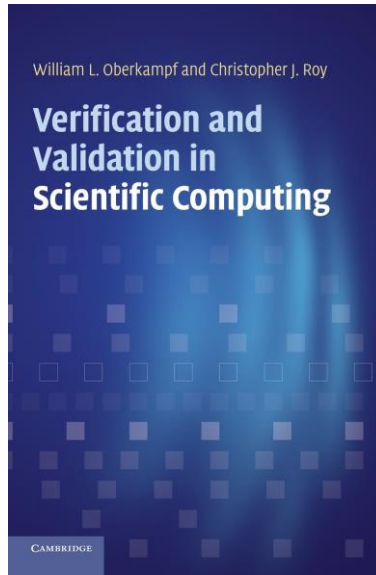
## Terminology

- **Conceptual model:** Idealized **representation of the physical behavior** of the reality of interest.
- **Mathematical model:** Mathematical description of the physical processes represented in this conceptual model.
- **Computational model:** Numerical implementation of the mathematical model that will be solved on a computer to yield the computational predictions of the system response.
- **Verification:** Examines whether the results of a **computational model** are close enough to given solutions of the underlying **mathematical model**.
- **Calibration:** Process of **adjusting parameters** in the computational model to improve **agreement with data**.
- **Validation:** Investigates how accurately a **computational model** describes the **reality**.

# Categorization

## Terminology

- **System Response Quantity (SRQ):** Quantity of interest to be compared. SRQs for one case ideally form a **hierarchy** ranging from globally integrated to local quantities.
- **Comparison/Validation Metric:** Difference in SRQs between the reference data and the computational results.



# Categorization

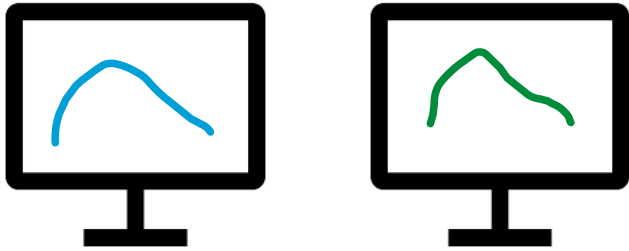
## What is to be compared/verified/validated?

Type	Same	Different	Description granularity	Sanity check	Comparison metric
<b>Code</b>	ConcMod, MathMod, Disc	Imp	Finest	Solution match	Performance
<b>Method</b>	ConcMod, MathMod	Disc, Imp	Fine	Convergence	Diff to reference
<b>Model</b>	ConcMod	MathMod, Disc, Imp	Coarse	Calibration	Diff to (non-deterministic) reference

# Categorization

## Types of Reference Solutions

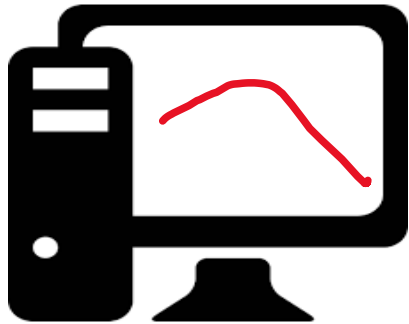
### Code/Model/Method intercomparison



### Analytical solution

$$y = f(t, x, \theta)$$

### Numerical solution



### Experimental data



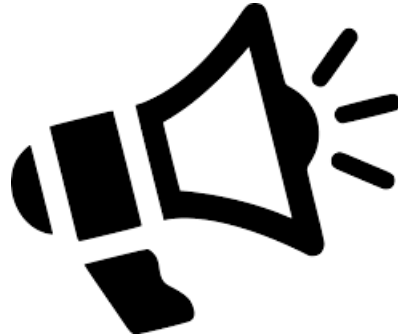
# Categorization

## Benchmarking Processes

Open or blind?



By invitation only or public call for participation?



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## Selected GCS Benchmark Studies

### A benchmark study on problems related to CO<sub>2</sub> storage in geologic formations (2009)

- Code Comparison / Verification
- Public CFP
- First phase blind, second phase open process
- 14 groups, 14 simulators
- 3 Benchmark cases
- 1 case with semi-analytical solution, 2 without reference solution
- SRQs: Leakage rate / time, mass flux / time, arrival time, maximum leakage, saturation snapshots, performance
- Metrics: line plots

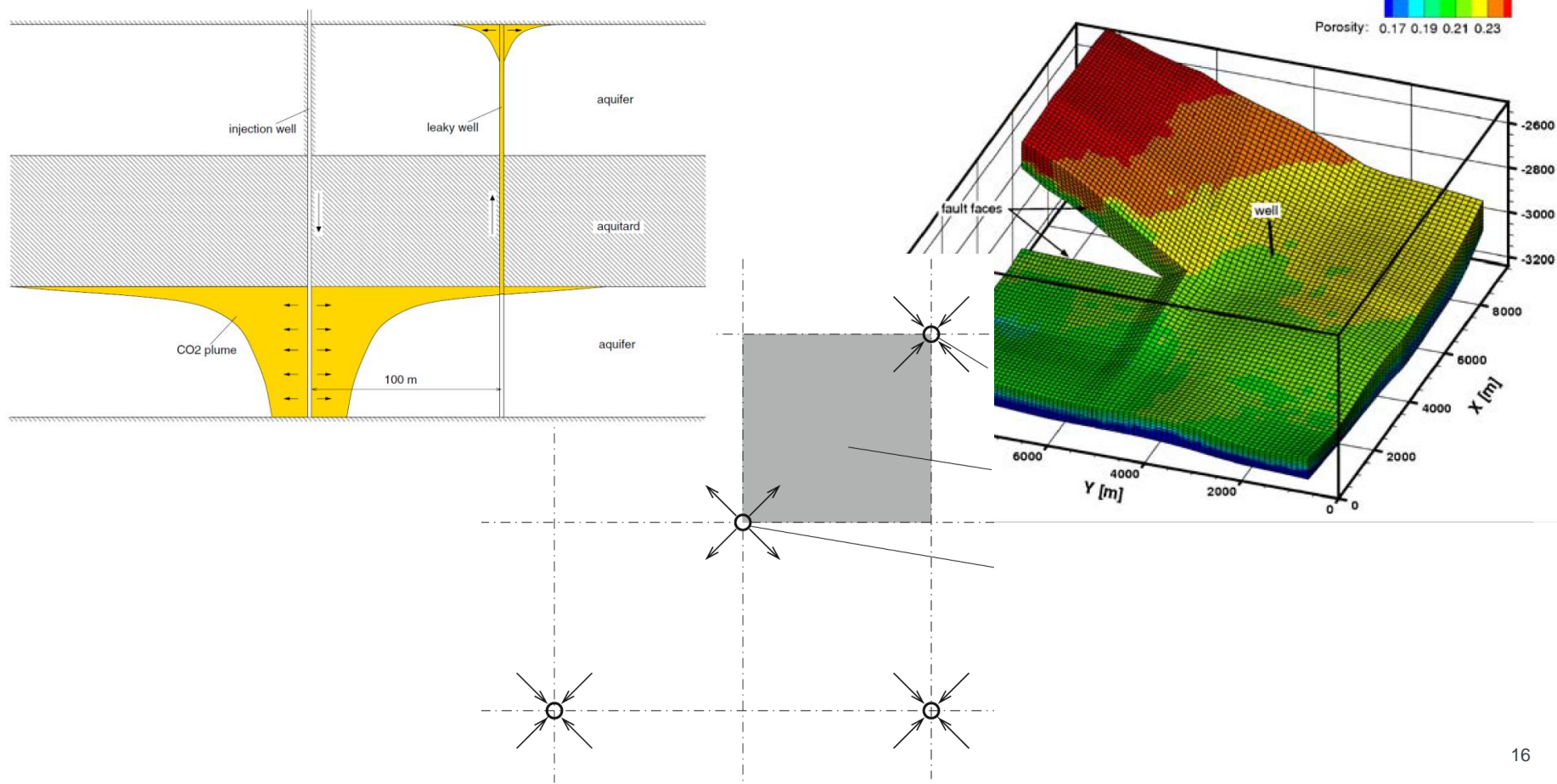


$$y = f(t, x, \theta)$$



# A benchmark study on problems related to CO<sub>2</sub> storage in geologic formations (2009)

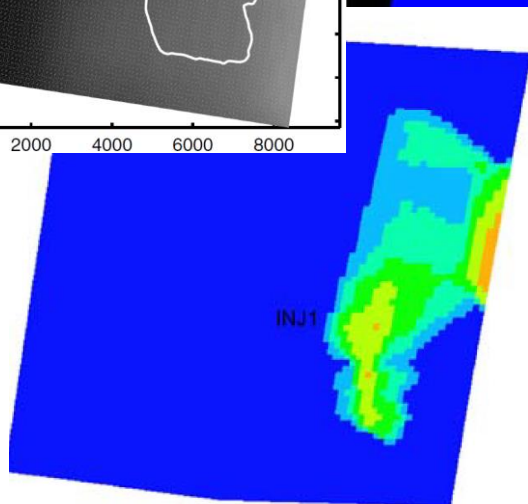
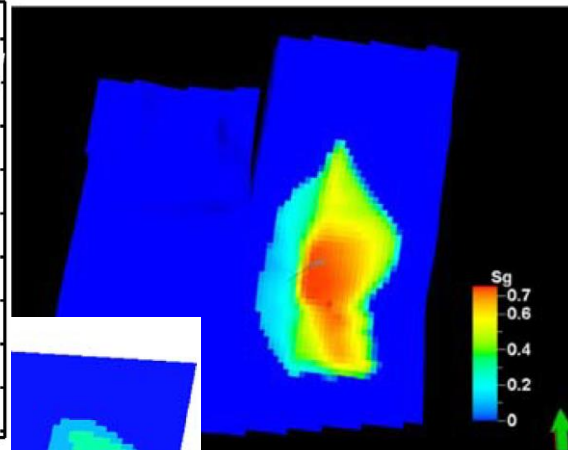
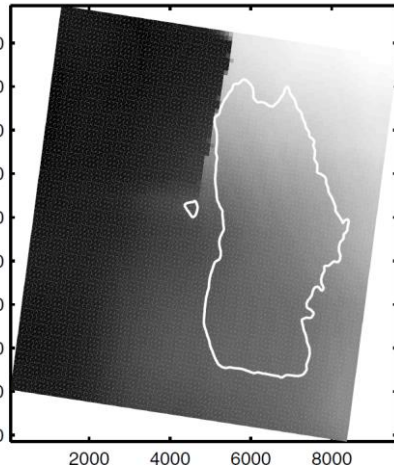
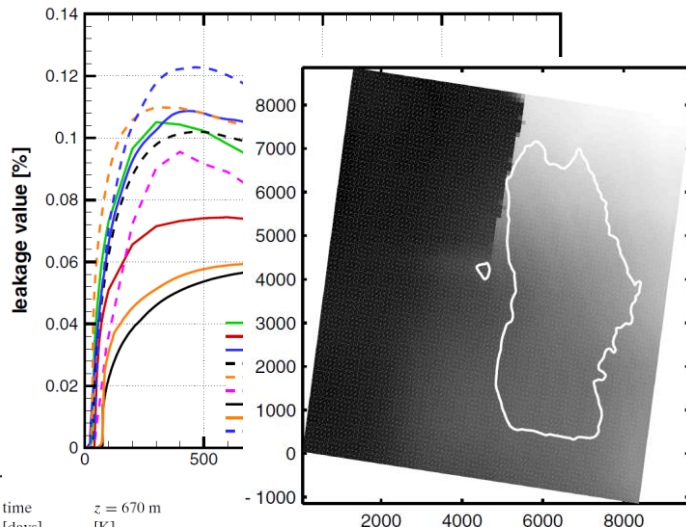
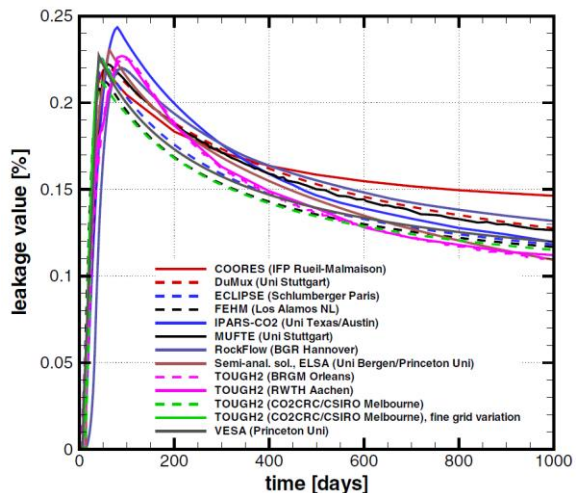
## Benchmark Cases





# A benchmark study on problems related to CO<sub>2</sub> storage in geologic formations (2009)

## SRQs, Measures and Metrics



	leakage [%]	max. leakage [days]	at 2,000 days [%]	time [days]	z = 670 m [K]
COORES (IFP)	0.105	300	0.076	31	Isothermal
ECLIPSE (Heriot-Watt)	0.074	600	0.067	42	Isothermal
ECLIPSE (refined grid) (Schlumberger)	0.109	437	0.086	24	Isothermal
FEHM (Los Alamos NL)	0.102	471	0.085	37	1.20
MUFTE (Uni Stuttgart)	0.058	941	0.052	75	1.91
RockFlow (BGR)	0.11	279	0.09	30	Isothermal
RTAFF2 (BRGM)	0.060	776	0.052	74	1.87
TOUGH2 (RWTH Aachen)	0.096	400	0.067	46	Isothermal

# A benchmark study on problems related to CO<sub>2</sub> storage in geologic formations (2009)

## Infrastructure for Comparison and Reproduction

Comput Geosci (2009) 13:409–434  
DOI 10.1007/s10596-009-9146-x

ORIGINAL PAPER

### A benchmark study on problems related to CO<sub>2</sub> storage in geologic formations

#### Summary and discussion of the results

Holger Class · Anozie Ebigbo · Rainer Helmig · Helge K. Dahle ·  
Jan M. Nordbotten · Michael A. Celia · Pascal Audigane · Melanie Darcis ·  
Jonathan Ennis-King · Yaqing Fan · Bernd Flemisch · Sarah E. Gasda ·  
Min Jin · Stefanie Krug · Diane Labregere · Ali Naderi Beni · Rajesh J. Pawar ·  
Adil Sbai · Sunil G. Thomas · Laurent Trenty · Lingli Wei

Received: 12 August 2008 / Accepted: 15 June 2009 / Published online: 22 July 2009  
© Springer Science + Business Media B.V. 2009

**Abstract** This paper summarises the results of a benchmark study that compares a number of mathematical and numerical models applied to specific problems in the context of carbon dioxide (CO<sub>2</sub>) storage in geo-

vective multi-phase flow, compositional effects due to dissolution of CO<sub>2</sub> into the ambient brine and non-isothermal effects due to temperature gradients and the Joule–Thomson effect. The problems deal with leak-

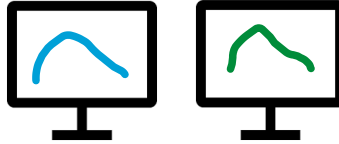
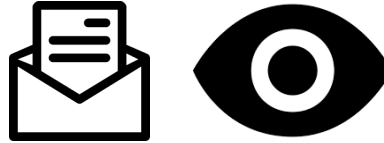
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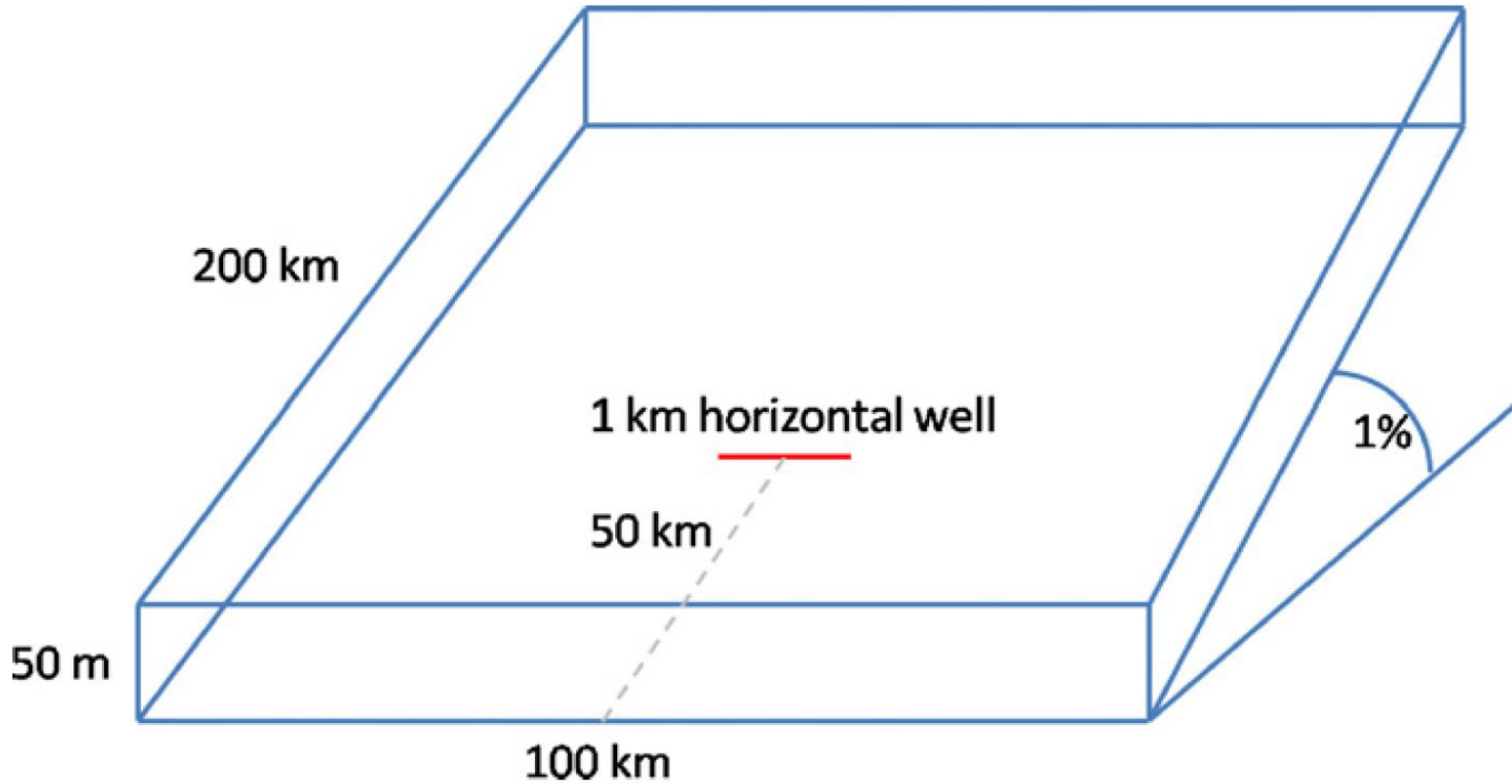
# Selected GCS Benchmark Studies

## Uncertainties in practical simulation of CO<sub>2</sub> storage (2012)

- Model / code comparison
- By invitation, open process
- 6 groups, 6 simulators
- 1 Benchmark case
- No reference solution
- SRQs: phase partitioning, furthest updip plume extent, mean and variance of the location of the CO<sub>2</sub> phase, all over time
- Metrics: Line plots

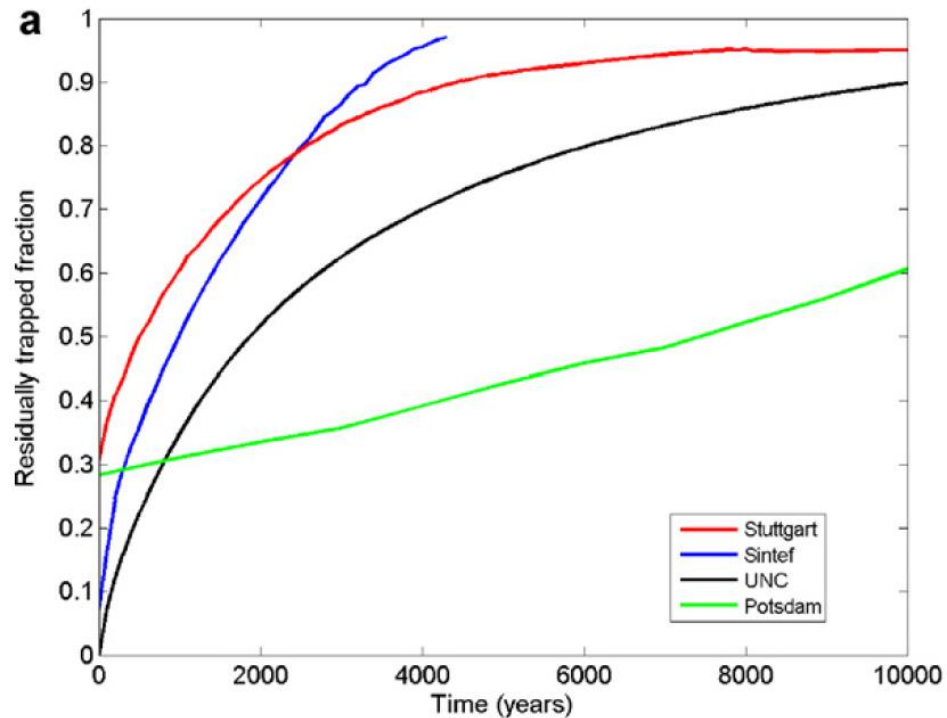
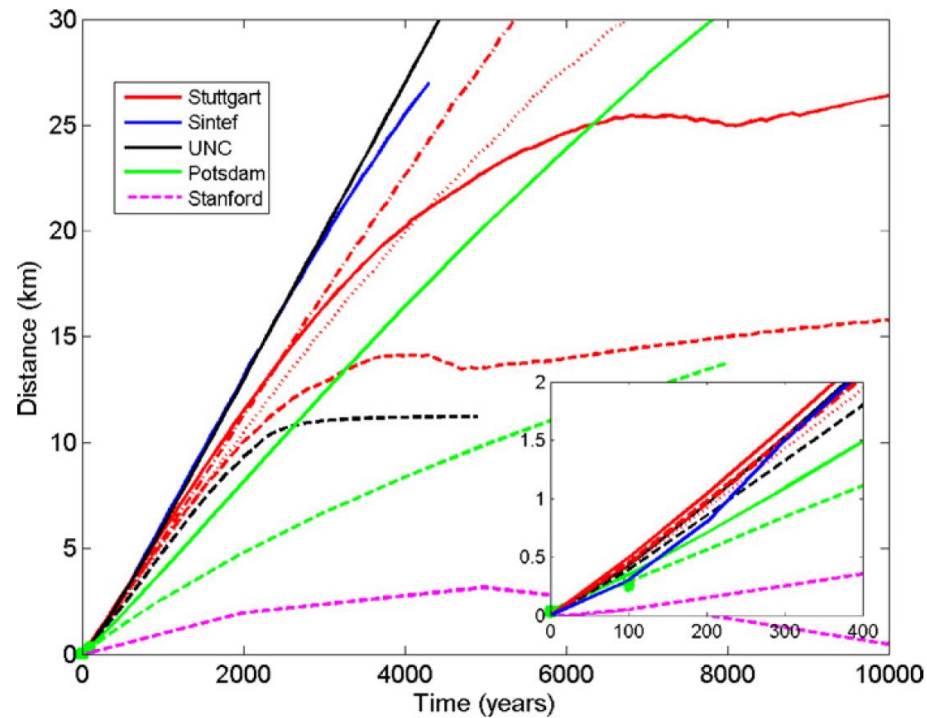


**Benchmark Case**



# Uncertainties in practical simulation of CO<sub>2</sub> storage (2012)

## SRQs, Measures and Metrics



# Uncertainties in practical simulation of CO<sub>2</sub> storage (2012) Infrastructure for Comparison and Reproduction

International Journal of Greenhouse Gas Control 9 (2012) 234–242



Contents lists available at SciVerse ScienceDirect

## International Journal of Greenhouse Gas Control

journal homepage: [www.elsevier.com/locate/ijggc](http://www.elsevier.com/locate/ijggc)



## Uncertainties in practical simulation of CO<sub>2</sub> storage

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### ABSTRACT

Practical simulation of CO<sub>2</sub> storage in geological formations inherently involves decisions concerning relevant physics, upscaling, and numerical modeling. These decisions are unavoidable, since the full problem cannot be resolved by existing numerical approaches. Here, we report on the impact of three distinct approaches to make the problem computationally tractable: reduced physics, upscaling, and non-converged discretizations. Compounding these different strategies, we have used a benchmark study to

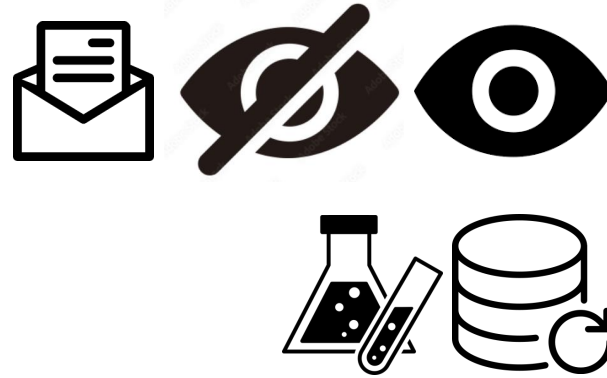
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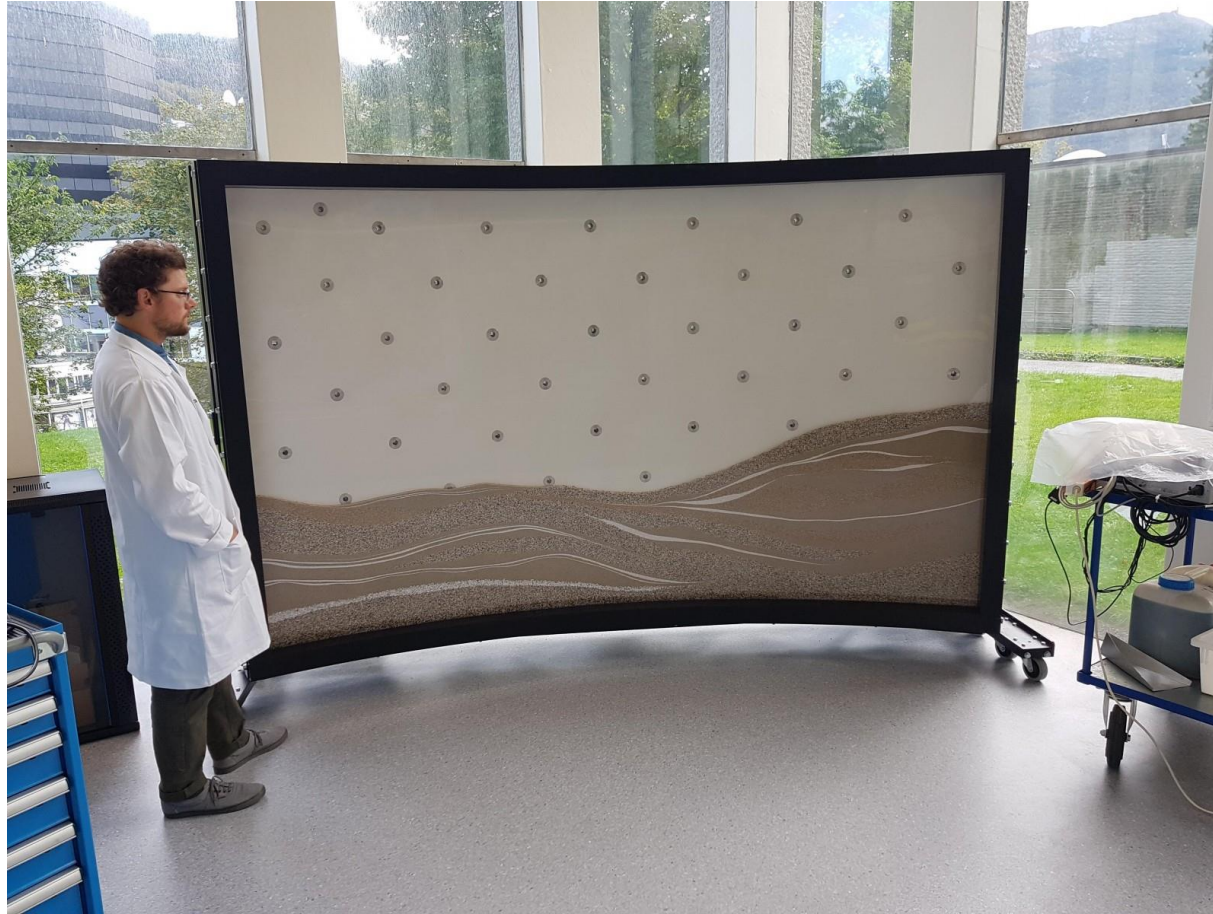
## FluidFlower: A Meter-scale Experimental Laboratory for GCS (2024)

- Validation / Model comparison
- Invitation-only, multi-stage blind/open process
- 9 groups, 9 models
- Data from **5 experimental runs**
- SRQs:
  - Saturation and concentration fields at selected time steps
  - Integrated phase composition ... over time
  - **Mean and std dev** for various quantities
- Metrics: Multiple, e.g., Wasserstein distance
- Other reported characteristics: Model assumptions, implementation details, ...



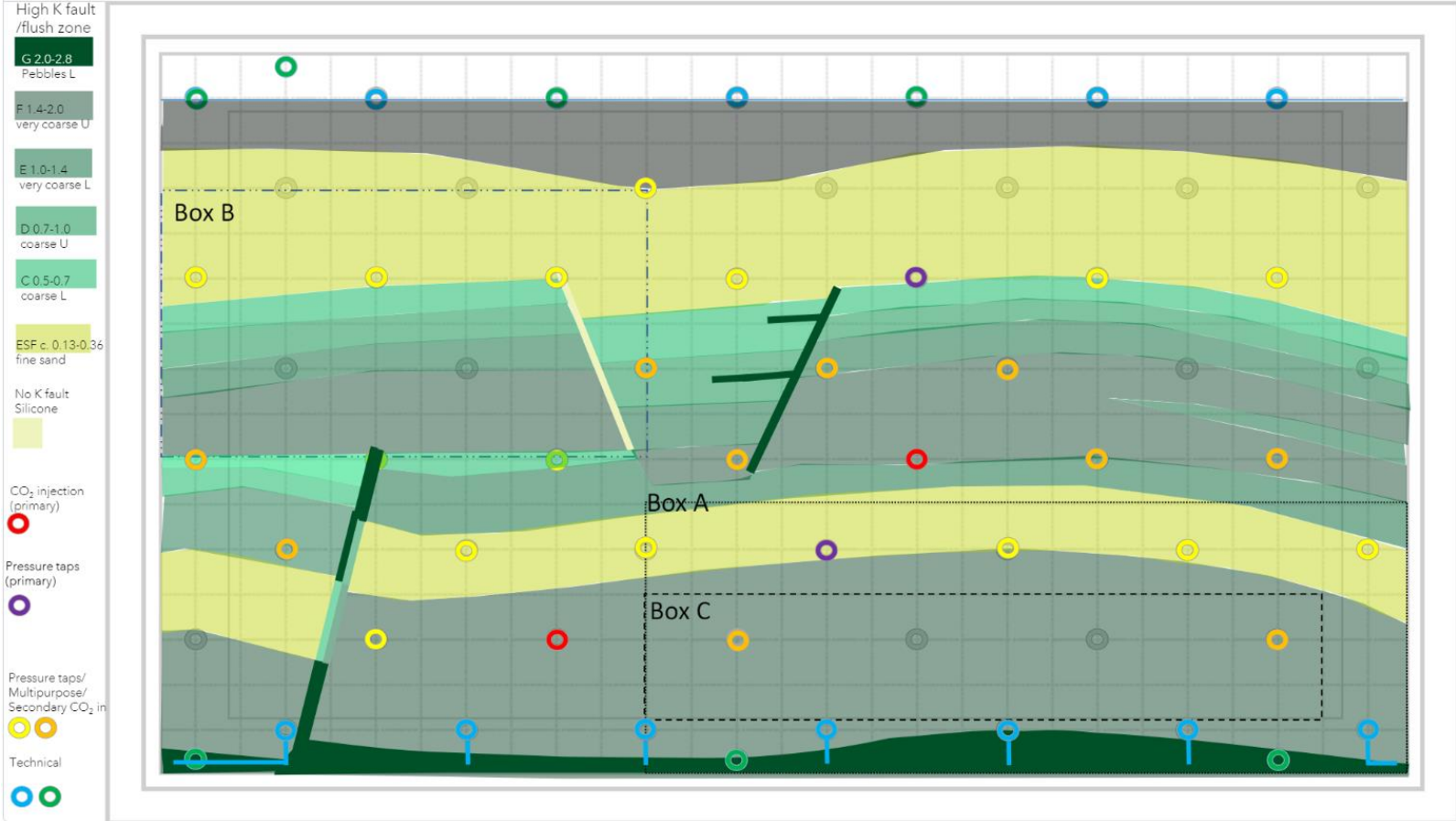
# FluidFlower: A Meter-scale Experimental Laboratory for GCS (2024)

## Experimental Rig



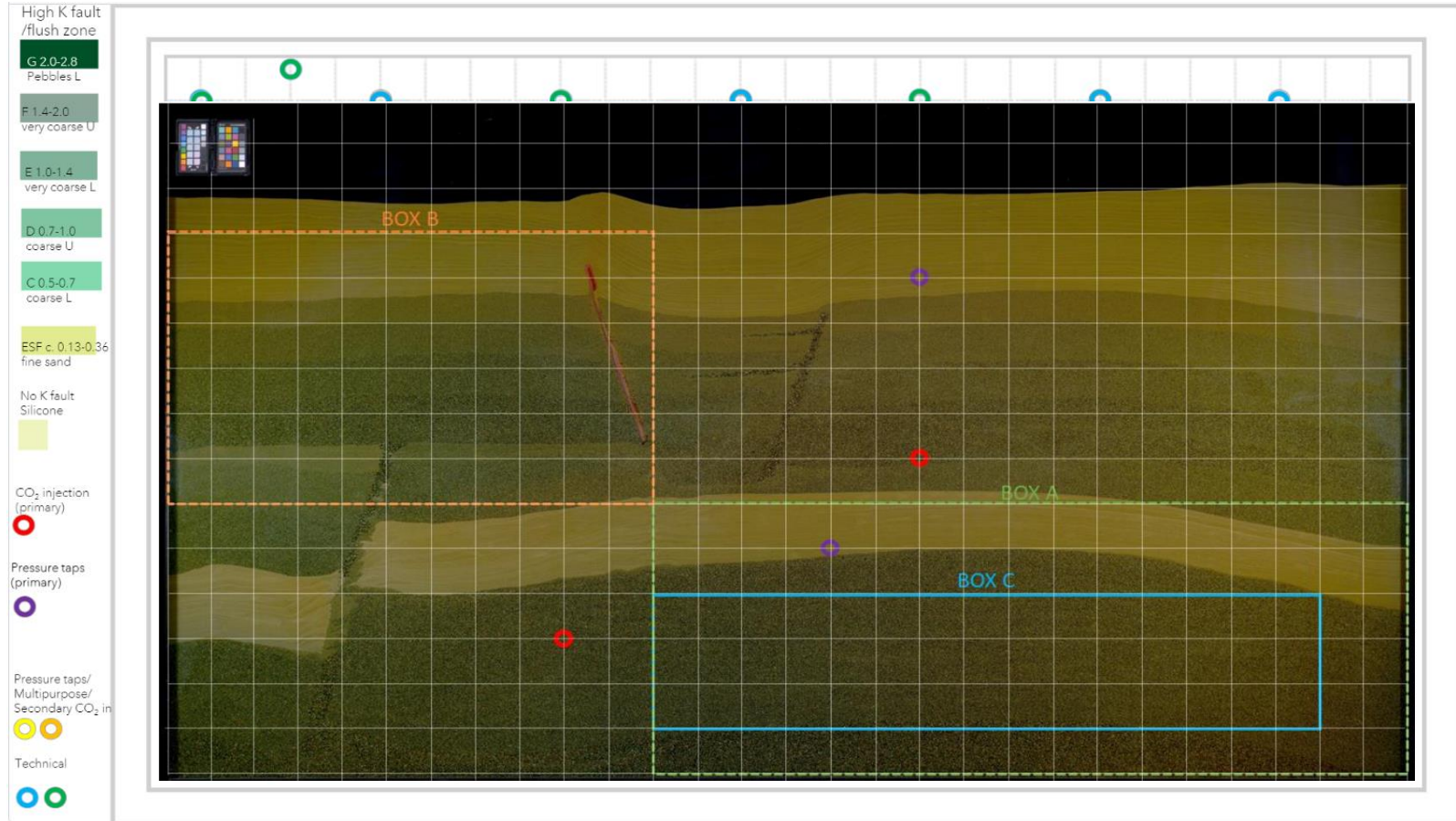
# FluidFlower: A Meter-scale Experimental Laboratory for GCS (2024)

## Intended Geometry



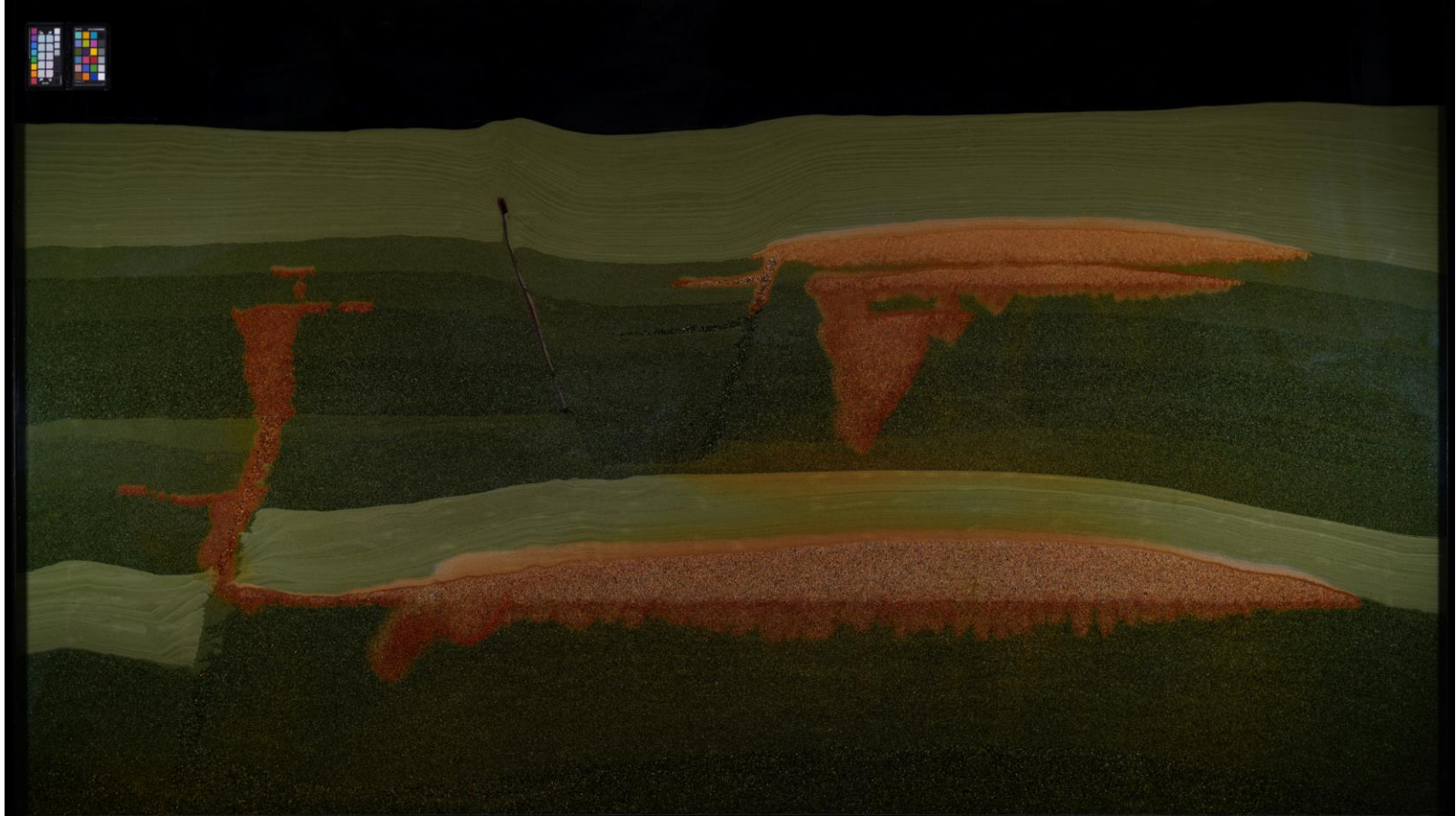
# FluidFlower: A Meter-scale Experimental Laboratory for GCS (2024)

## Implemented Geometry



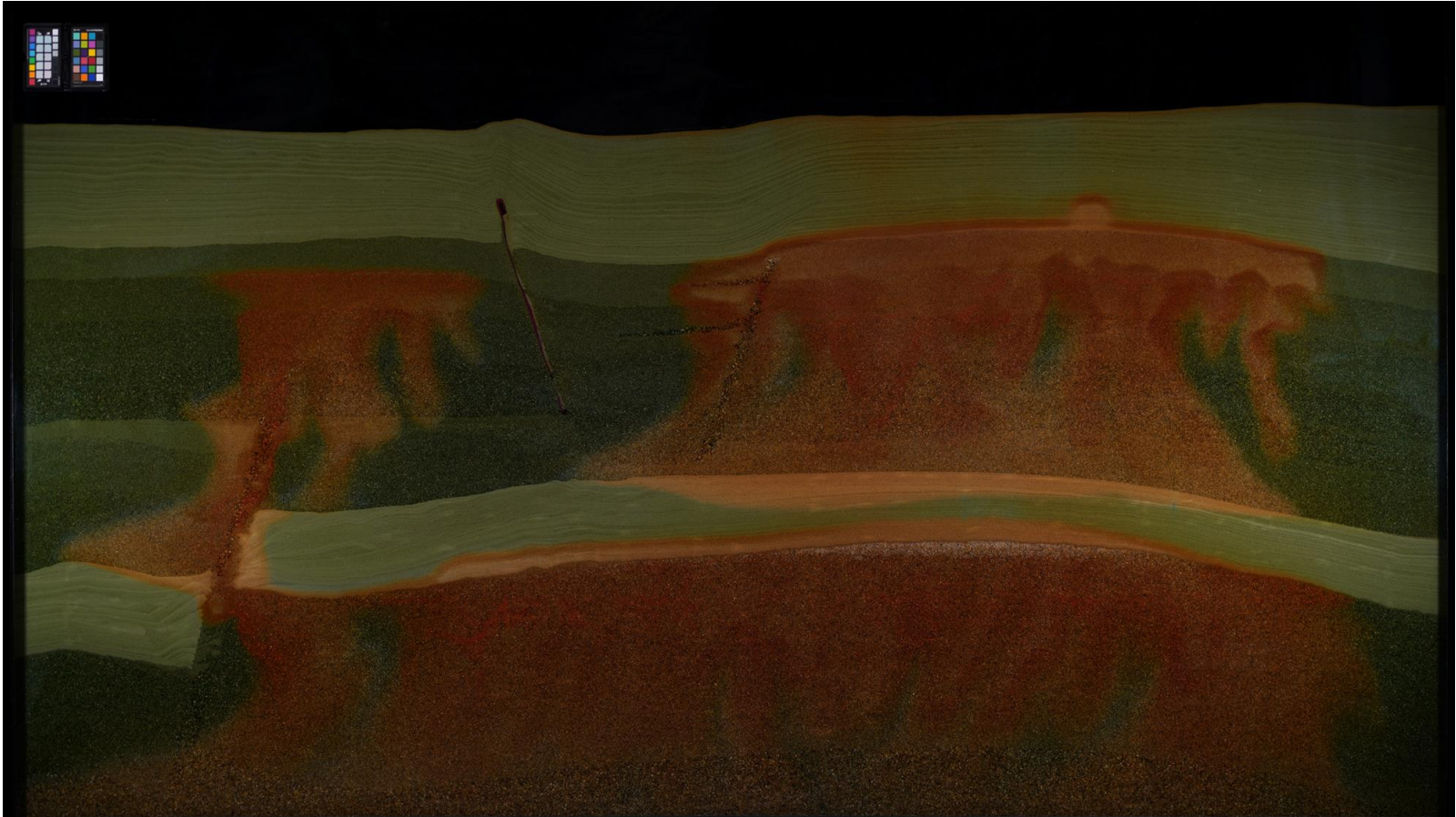
# FluidFlower: A Meter-scale Experimental Laboratory for GCS (2024)

**Snapshot after 240 Minutes = 4 Hours**



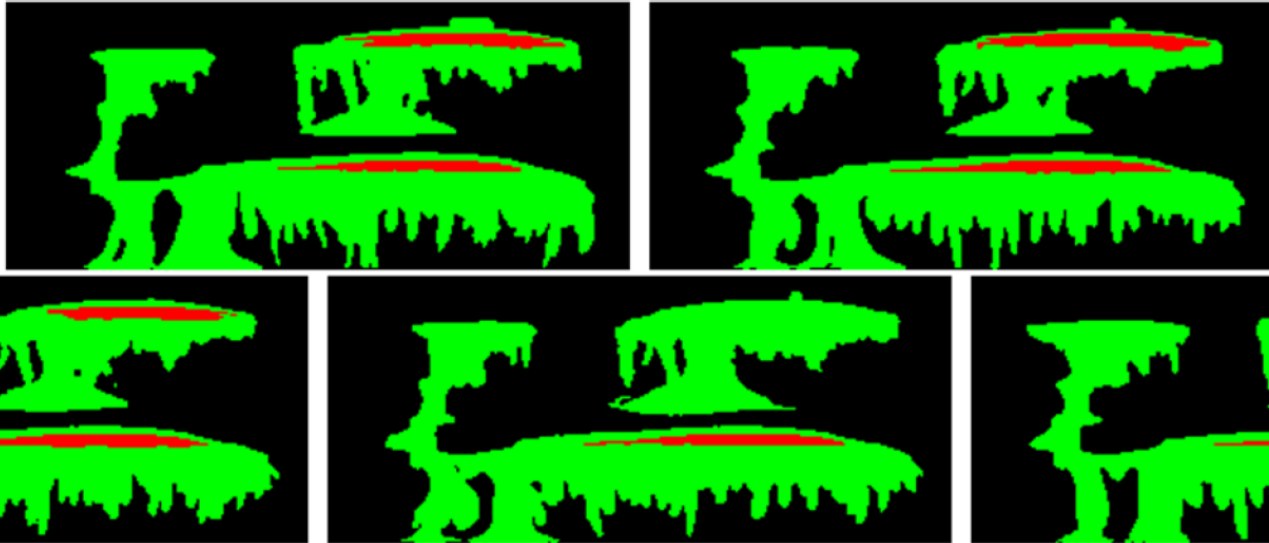
# FluidFlower: A Meter-scale Experimental Laboratory for GCS (2024)

## Snapshot after 4320 Minutes = 72 Hours



# FluidFlower: A Meter-scale Experimental Laboratory for GCS (2024)

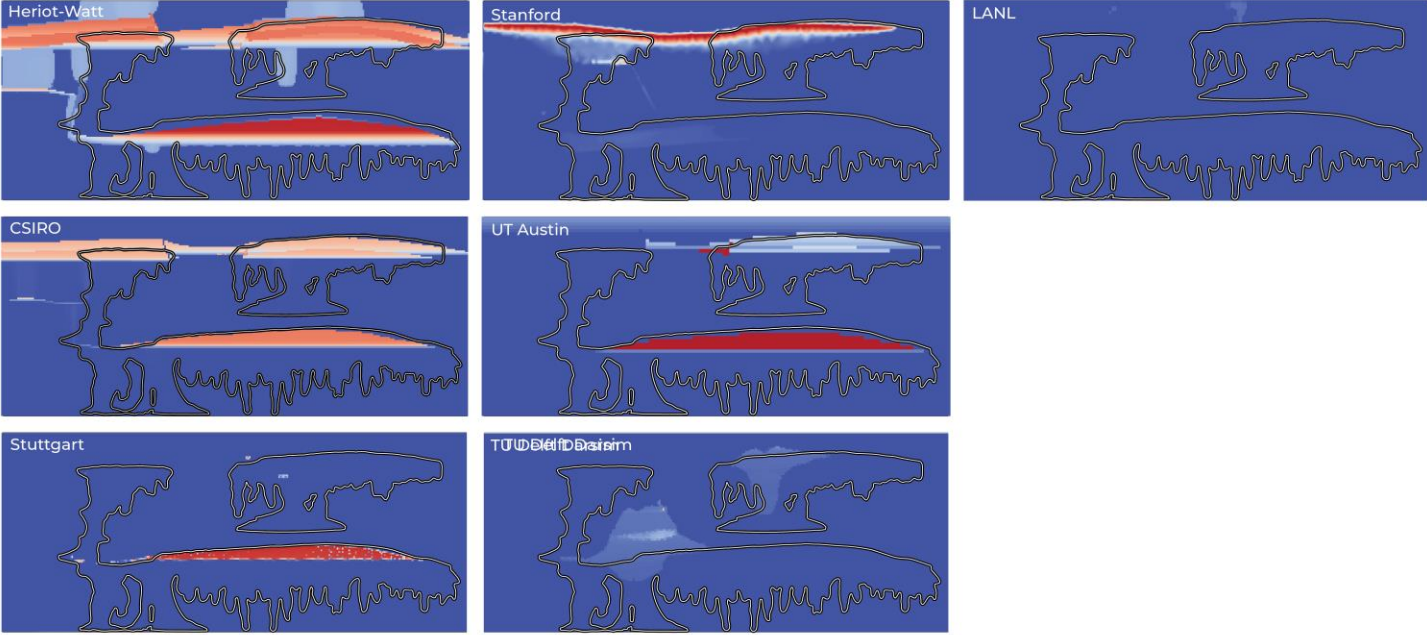
## Five Operationally Identical Experimental Runs




Segmentation data after 24 hours.

# FluidFlower: A Meter-scale Experimental Laboratory for GCS (2024)

This experiment is hard to forecast **independently**



  
physical ground truth

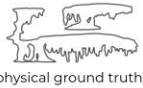
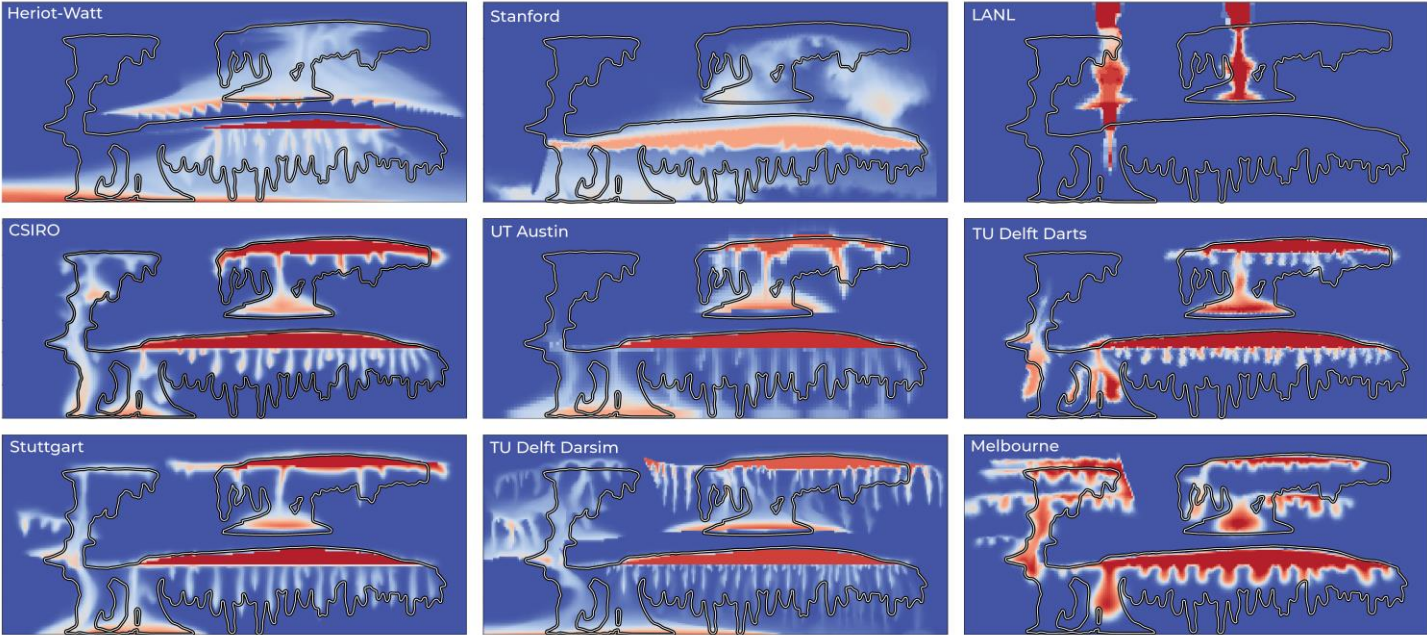
CO<sub>2</sub> concentration after 24 hours

CO<sub>2</sub> concentration  
LOW HIGH



# FluidFlower: A Meter-scale Experimental Laboratory for GCS (2024)

This experiment is hard to forecast **collaboratively**



CO<sub>2</sub> concentration after 24 hours



## Can We Quantify the Difference?

- Apply the **Wasserstein metric**, working on distributions of equal mass.
- Measures “the **minimal effort required to reconfigure the mass** of one distribution in order to recover the other distribution”.
- Approximate roughly the **CO<sub>2</sub> mass density in each cell** by

$$\tilde{m} = \rho_g s + c(1 - s)$$

- **Normalize** these values to two-dimensional probability distributions.
- Apply the Python library **POT** to calculate the Wasserstein distances.
- **Rescaling** to the injected CO<sub>2</sub> mass yields distances of dimension **mass times length**.

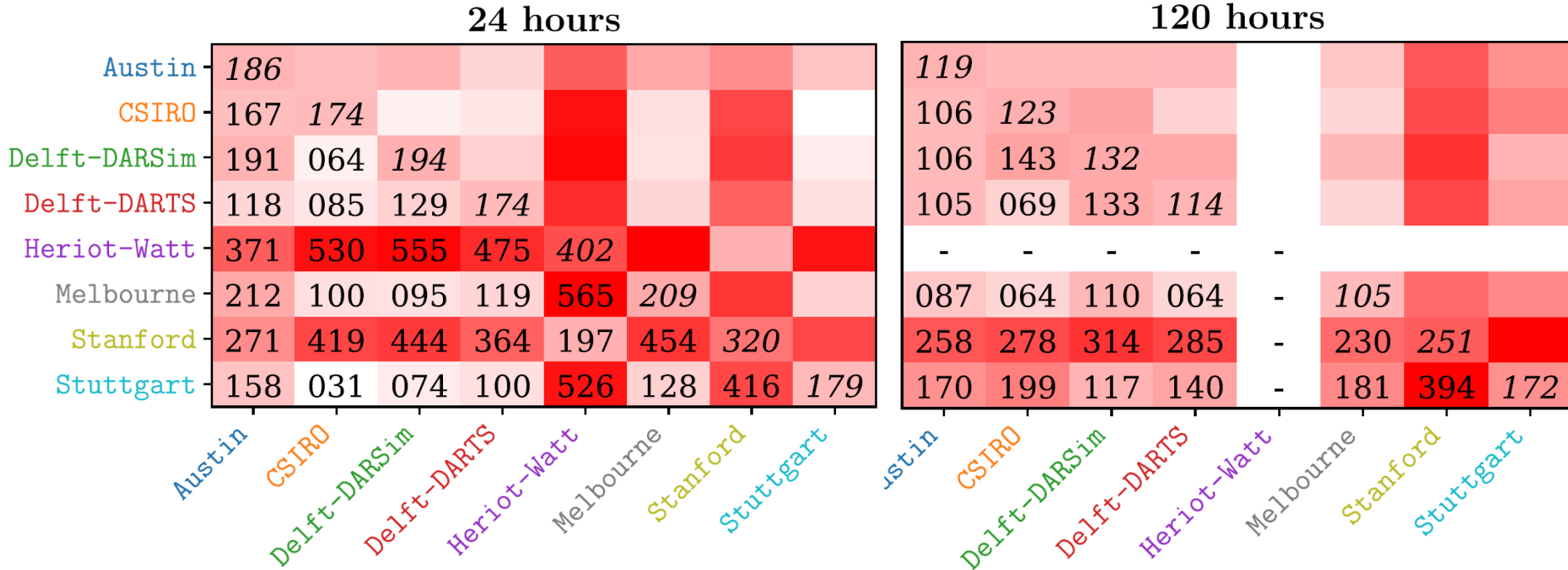
V. Panaretos, Y. Zemel (2019): “Statistical aspects of Wasserstein distances”, *Ann. Rev. Stat. Appl.* 1, 405–431.

DOI [10.1146/annurev-statistics-030718-104938J](https://doi.org/10.1146/annurev-statistics-030718-104938J).

R. Flamary et al. (2021): „POT: python optimal transport“, *J. Mach. Learn. Res.* 22, 1–8. Repo at [github.com/PythonOT/POT](https://github.com/PythonOT/POT).

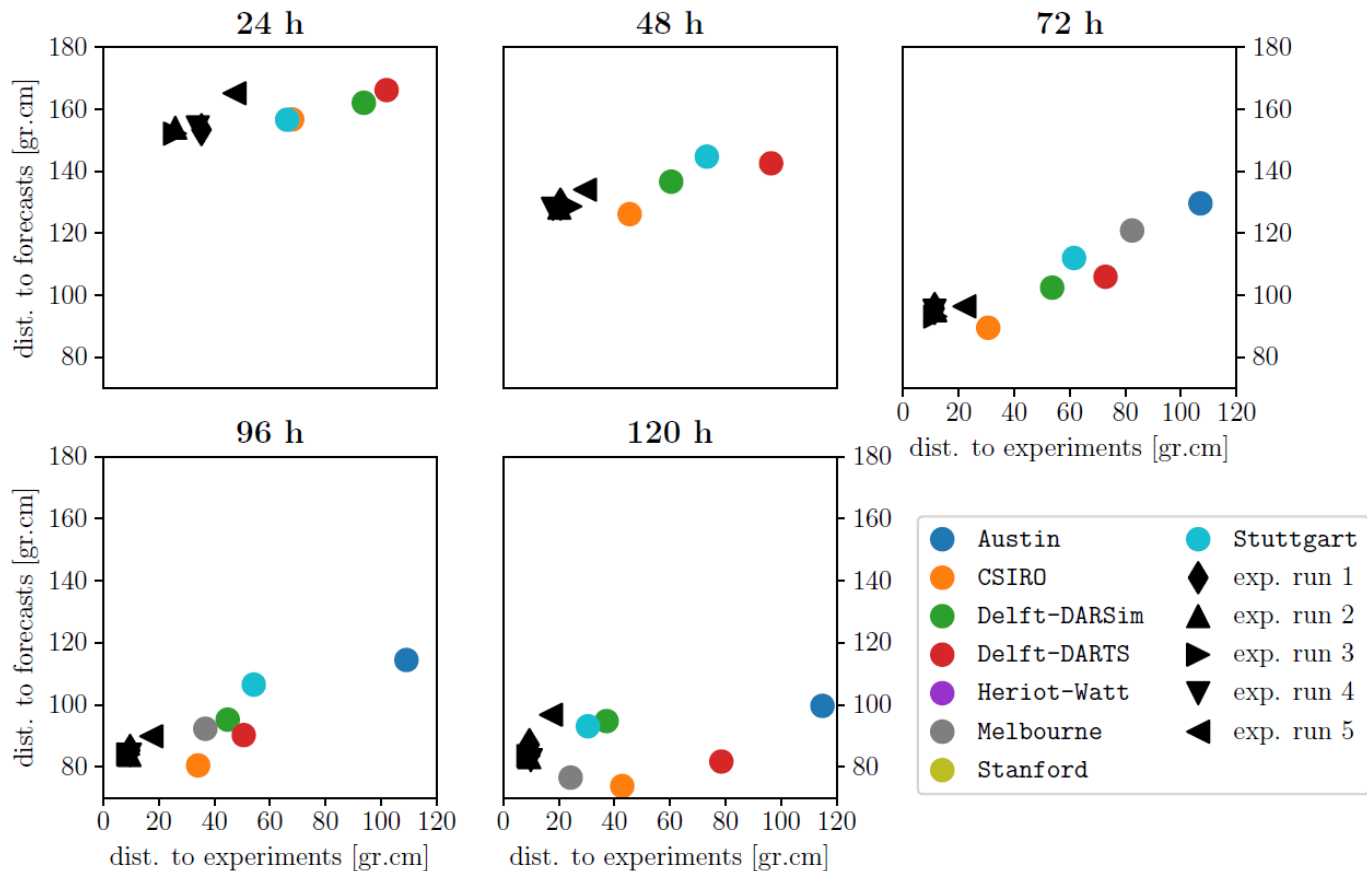
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## Wasserstein Distances Between Forecasts

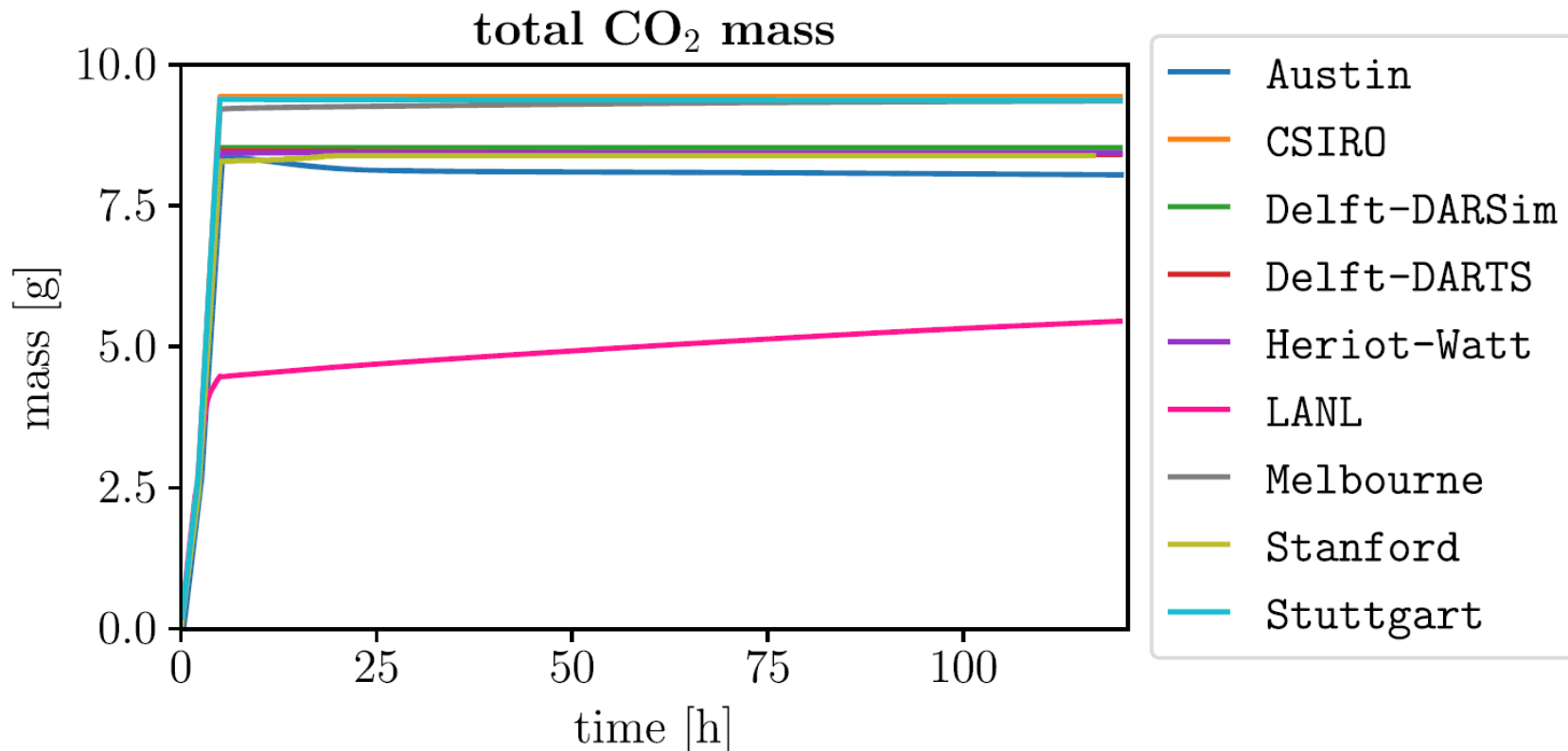


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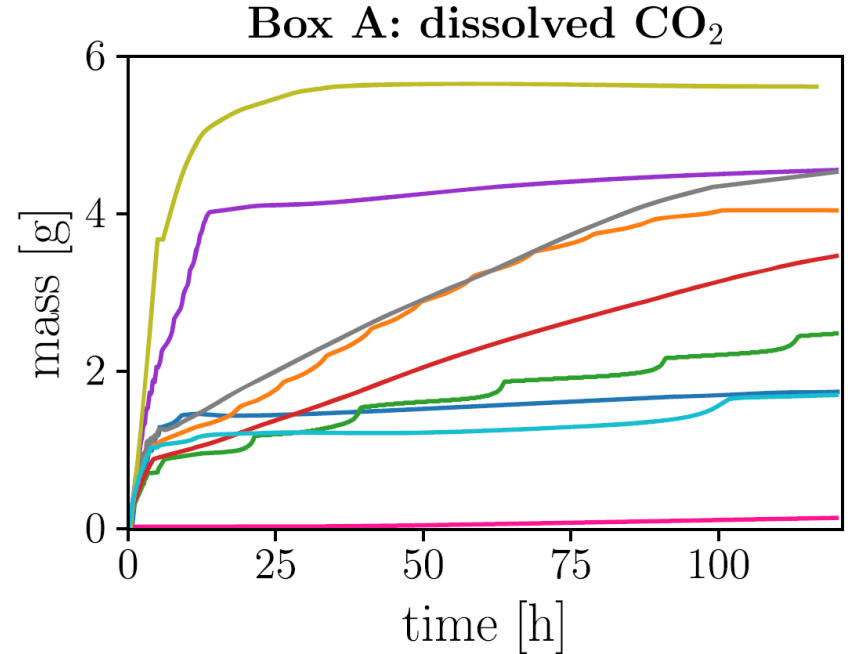
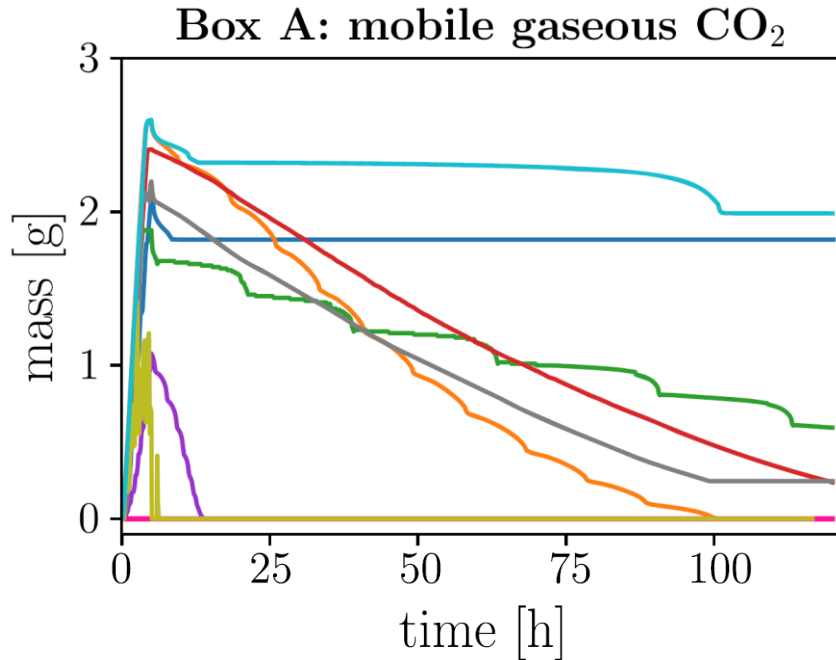
## Mean Wasserstein Distances To Forecasts and Experiments



## Temporal Evolution of Total CO<sub>2</sub> mass in the computational domain



## CO<sub>2</sub> Phase Distribution in Box A: Forecasts





## Sparse Data: SRQs

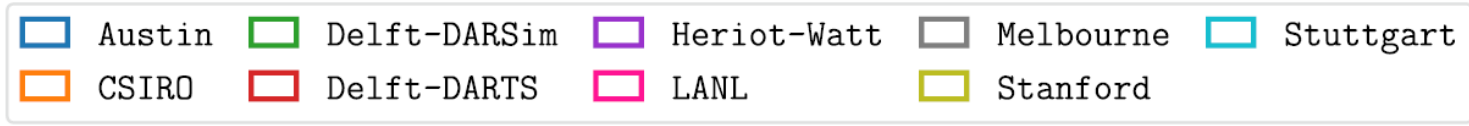
1. As a proxy for assessing **risk of mechanical disturbance** of the overburden:  
Maximum pressure at sensor number 1 and 2.
2. As a proxy for when **leakage risk** starts declining:  
Time of maximum mobile free phase in Box A.
3. As a proxy for our ability to accurately predict **near well phase partitioning**:  
CO<sub>2</sub> phase distribution in Box A at 72 hours after injection starts.
4. As a proxy for our ability to **handle uncertain geological features**:  
CO<sub>2</sub> phase distribution in Box B at 72 hours after injection starts.
5. As a proxy for our ability to capture **onset of convective mixing**:  
Time for which a measure for finger length first exceeds 110% of the width of Box C.
6. As a proxy for our ability to capture **migration into low-permeable seals**:  
Total mass of CO<sub>2</sub> in the top seal facies at final time.



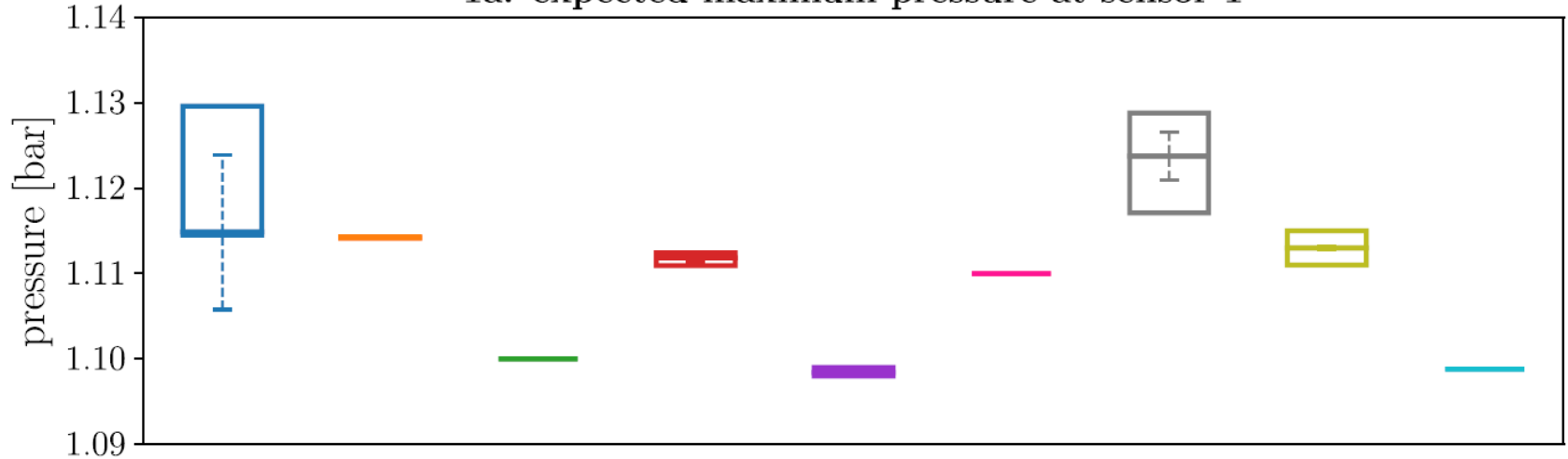
## Sparse Data: Reporting

- Each item had to be reported as **six numbers**:
  - prediction of the **mean** (stated as P10, P50 and P90)
  - prediction of the **standard deviation** (again as P10, P50, P90)
- **Any preferred methodology** could be chosen
  - ensemble runs
  - formal methods of uncertainty quantification
  - human intuition from experience
  - ...
- Most groups **did not report** P10 and P90 for the standard deviations.

## Sparse Data: Forecasts of Pressure at Sensor 1



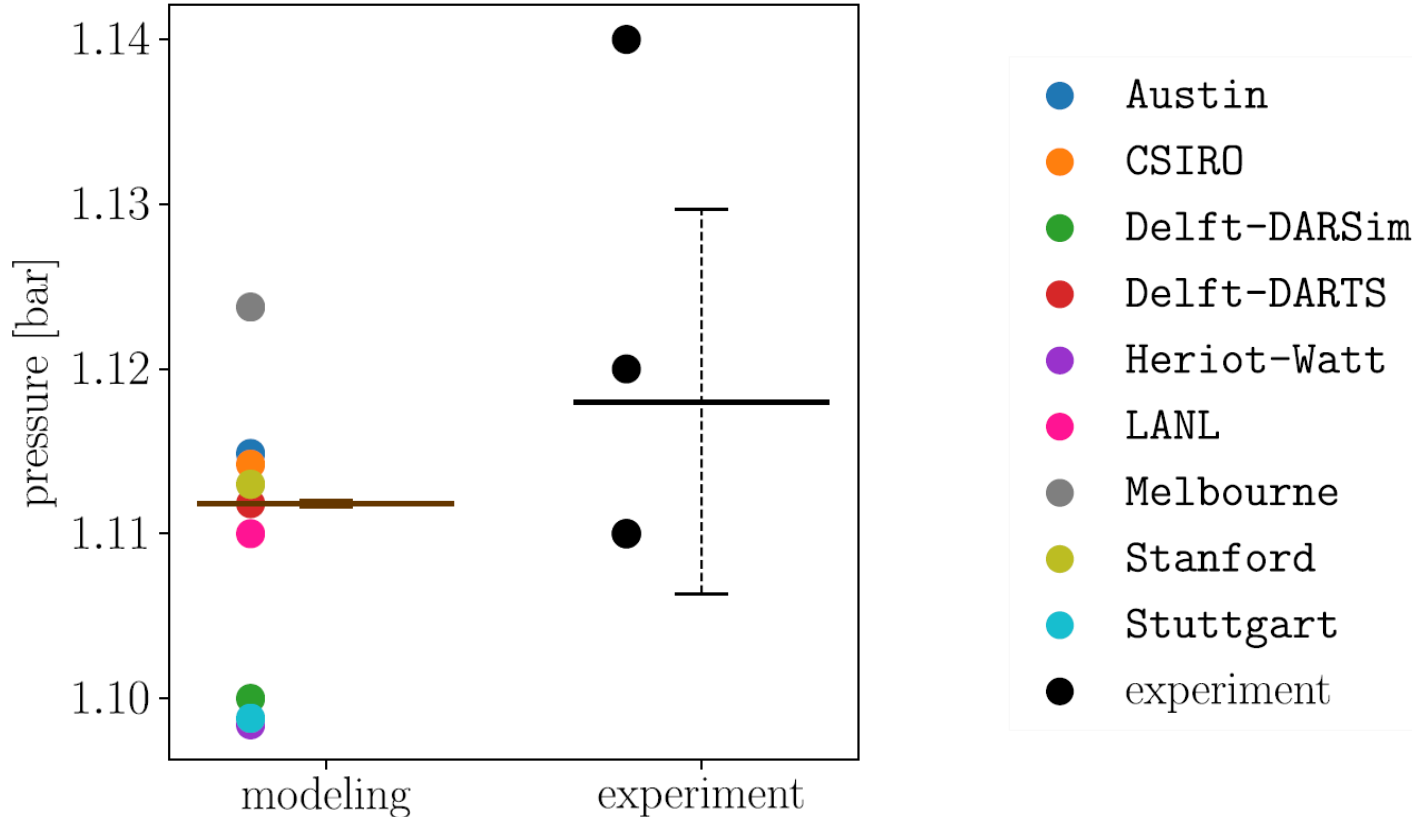
1a: expected maximum pressure at sensor 1



↑  
Typical pressure variation in Bergen during experim. timespan  
↓

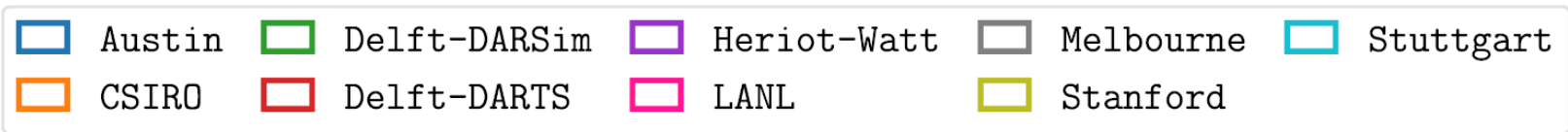
## Sparse Data: Comparison of Pressure at Sensor 1

1a: expected max. pressure at sensor 1

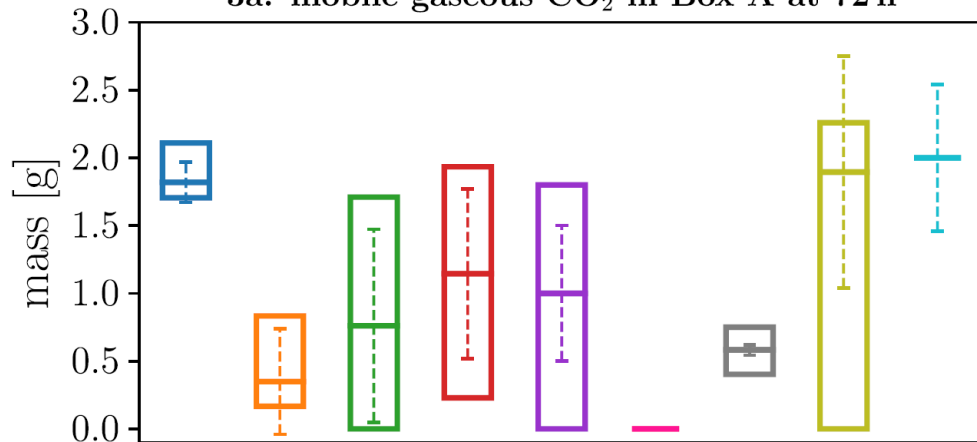


# FluidFlow: A Meter-scale Experimental Laboratory for GCS (2024)

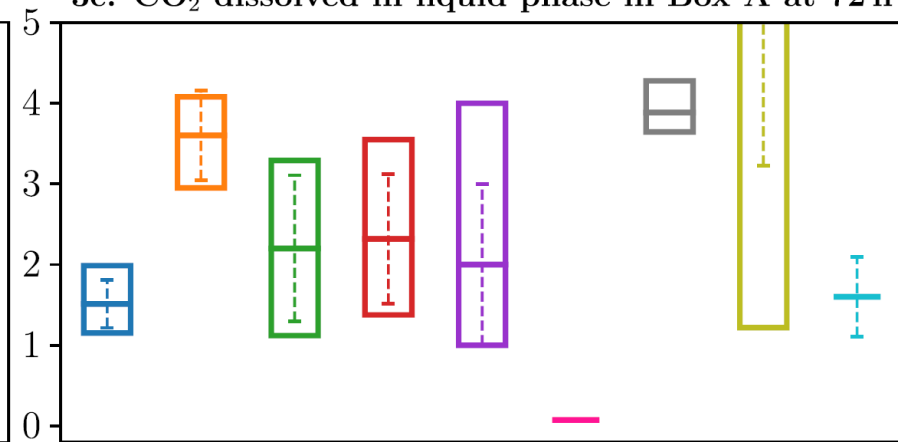
## Sparse Data: Forecasts of CO<sub>2</sub> Phase Composition in Box A at 72 hours



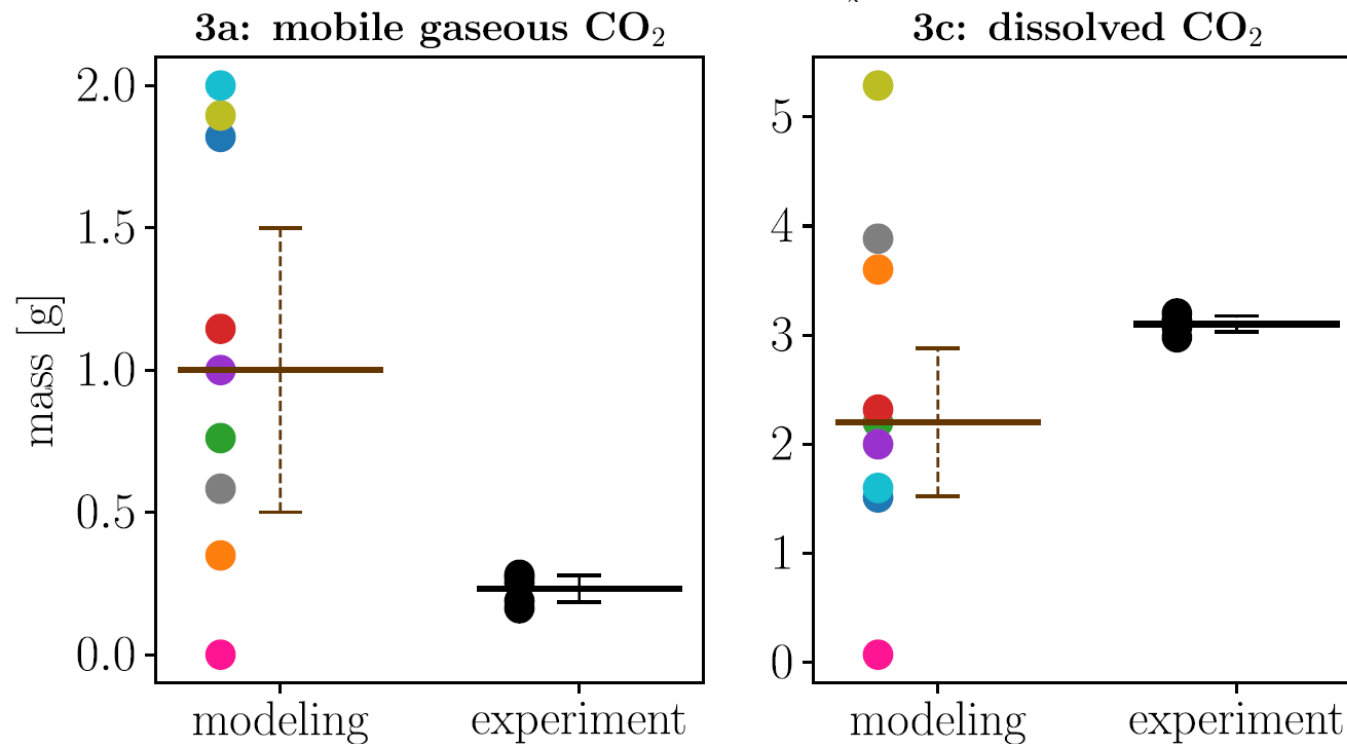
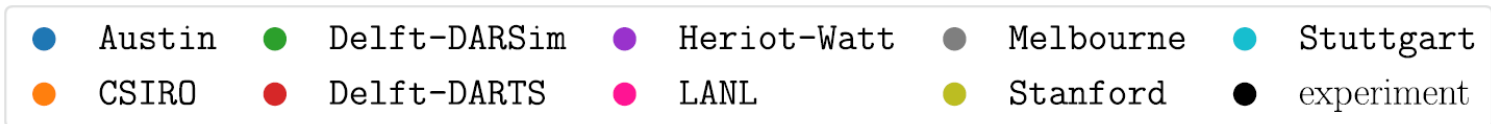
3a: mobile gaseous CO<sub>2</sub> in Box A at 72 h



3c: CO<sub>2</sub> dissolved in liquid phase in Box A at 72 h



## Sparse Data: Comparison of CO<sub>2</sub> Phase Composition in Box A at 72 hours



# FluidFlower: A Meter-scale Experimental Laboratory for GCS (2024) Infrastructure for Comparison and Reproduction

FluidFlower international benchmark study

Repositories

- modeling Private
- imperial Private
- austin Private
- csiro Private

#modeling

Bernd Flemisch (Stuttgart) 03/24/2022  
Thank you for participating in yesterday's third meeting! It's nice to see how things are evolving. Please find the meeting slides at [https://github.com/FluidFlow/benchmark/blob/main/meetings/FluidFlow\\_3rd\\_participants\\_meeting.pdf](https://github.com/FluidFlow/benchmark/blob/main/meetings/FluidFlow_3rd_participants_meeting.pdf).

Bernd Flemisch (Stuttgart) 03/24/2022  
As announced yesterday, Jan Nordbotten and his team heartily invite you to the "FluidFlower Benchmark Workshop", taking place **26-28.4.** at the obviously beautiful Bekkjarvik Geotriever in the proximity of Bergen, Norway, <https://www.bekkjarvikgeotriever.no/>. In particular, they manage to pay for accommodation and food, you only have to cover your travel expenses.

Bernd Flemisch (Stuttgart) 03/24/2022  
They "would be pleased to meet as many of you as possible in person. There exists however also the possibility to participate online." In any case, please register for the workshop **before Wednesday, 30.3.** at <https://forms.gle/W9w9d3T7NgQ3eA>.

Bernd Flemisch (Stuttgart) 03/24/2022  
Please upload all results as required by the description <https://github.com/FluidFlow/benchmark/blob/main/description.pdf> **before Friday, 22.4. 23:59 h CET.** This deadline is hard as I need the few days until the workshop to assemble all results in a decent form.

Bernd Flemisch (Stuttgart) 03/29/2022  
@everyone Thank you for registering for the workshop, we currently count 14 participants joining physically! Nevertheless, it would be fantastic if every participating group could send at least one member to Bekkjarvik. The organizers kindly extended the deadline to **Monday, 4.4.** <https://forms.gle/W9w9d3T7NgQ3eA>. **Please register!**

Samuel Jackson (CSIRO) 03/29/2022  
Thanks Bernd. We currently can only travel within Australia as per CSIRO policy, so won't be able to physically join

Bernd Flemisch (Stuttgart) 04/25/2022  
@everyone I have one rather urgent request: Can you please double-check your "D" entries in your sparse data files? If you actually mean "0", everything is fine, but if it is more a "not applicable" or "don't know", please enter a non-numerical value such as "N/A" instead or just leave the entry empty.

I remember that I said something different in one of our meetings, sorry for this.

If you change some "0"s, please let me know.

I generated figures and movies from your results and placed them in the "figures" folder of your repository. Please feel free to use them in your presentations tomorrow. Also kindly double-check if I probably messed up something.

main general / visualization / visualize\_spatial\_maps.py /

berndflemisch update visualization scripts

1 contributor

98 lines (78 sloc) 3.72 KB

```

1 #!/usr/bin/env python3
2
3 ----
4 Script to visualize the gas saturation and CO2 concentration
5 on an evenly spaced grid as required by the benchmark description
6 ---
7
8 import os
9 import argparse
10 import numpy as np
    
```

main austin / sparse\_data.csv

mjamouil Add files via upload

2 contributors

14 lines (14 sloc) 1.24 KB

Search this file...

idx	p10_mean	p50_mean	p90_mean	p10_dev	p50_dev	p90_dev
1a	111448.8311728	111486.7523528	112960.6107242	920.615104022203	907.914354190899	1466.23219142009
1b	105447.080488	105490.2072118	106343.9508688	433.555782215953	413.53747503411	775.213265491324
2	18600	18600	18600	0	0	0
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3b	0.0002295837675955342	0.000315298738951949	0.000345241731864876	2.96101590329268e-05	2.04093521021527e-05	3.44637186458377e-05
3c	0.00115141630959182	0.00151292977138066	0.00198666554352747	0.000472465912296314	0.000296239812953546	0.000553107231052641
3d	8.36964379052006e-05	0.000135819163802201	0.000330924268202632	0.000134793886279262	0.000111806574070829	0.000198789301357645

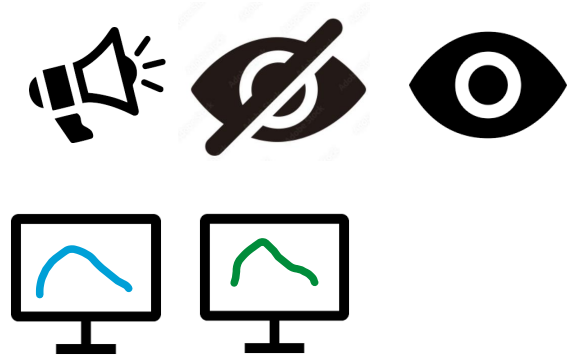
# Outline

1. Motivation
2. Categorization
- 3. Selected GCS Benchmark Studies**
  - a. The Classic
  - b. So Simple, Yet So Hard
  - c. Reality Meets Modeling
  - d. Back To Normal, But Bigger**
4. Summary and Conclusion

# Selected GCS Benchmark Studies

## The 11th SPE Comparative Solution Project (2024)

- Code comparison / Verification
- Public CFP, multi-stage blind/open process
- More than 40 signed participation agreements
- 3 Benchmark cases
- No reference solutions (yet)
- SRQs:
  - Saturation and concentration fields at selected time steps
  - Integrated phase composition ... over time
- Metrics: Multiple, e.g., Wasserstein distance
- Other reported characteristics: Implementation details, numerical performance





# The 11th SPE Comparative Solution Project

## Challenges

- Simulations are highly sensitive to implementation of non-linear constitutive laws
- Simulations display strong sensitivity to grid types and refinement
- Non-linear solvers appear to be not robust and small timesteps are required even at moderate grid sizes
- Majority of computational difficulties are localized in (time-dependent) parts of the domain
- Grid convergence studies require physical diffusion or dispersion for reference solution to exist

***Claim: State-of-the-art is not sufficient for reliable forecasts***

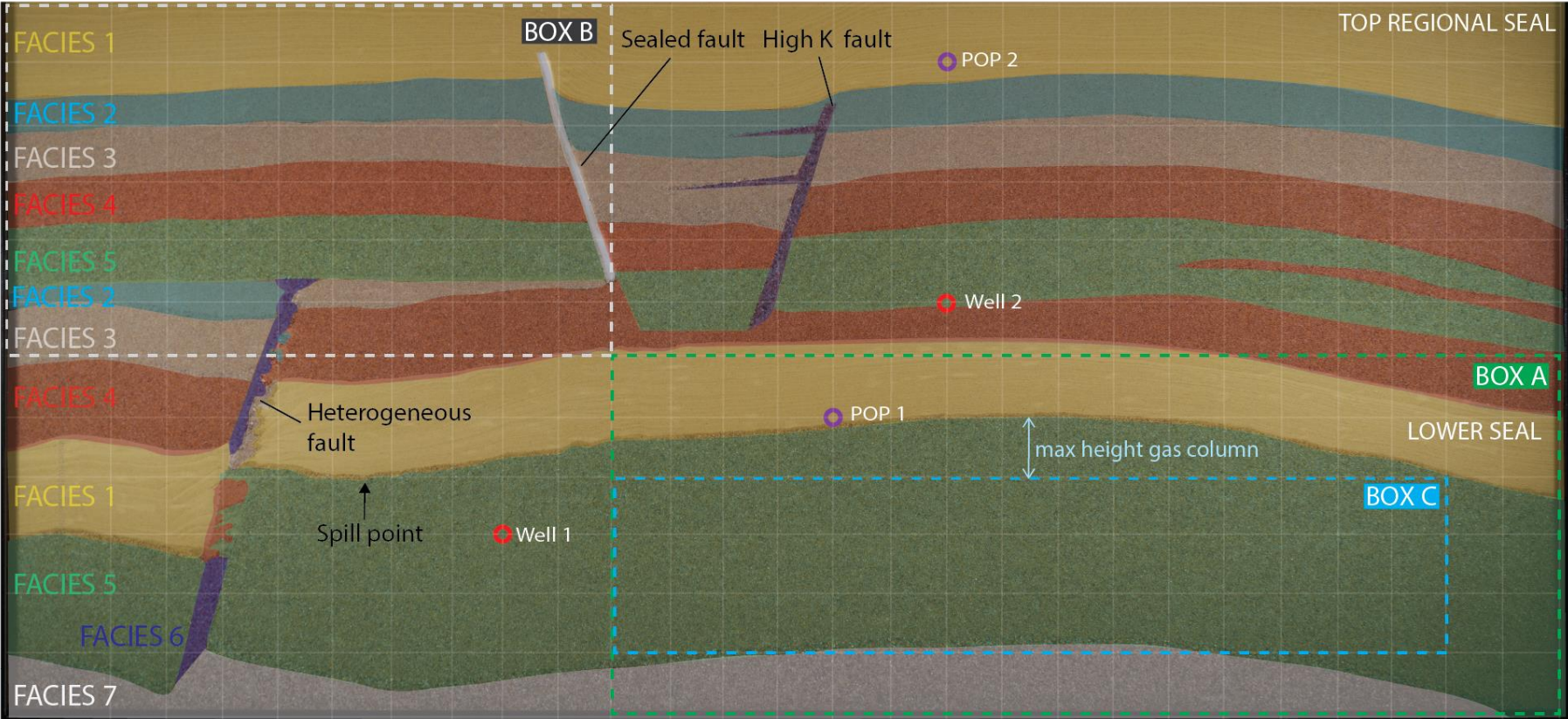
# The 11th SPE Comparative Solution Project

## Basic Setting

- Three **fully specified** simulation problems
  - Two-phase, two-component flows with thermal effects
  - All geometry and constitutive laws precisely defined
  - In principle, a unique solution should exist in the mathematical sense
  - No geomechanics, no geochemistry
- All three versions use the same baseline geometry as the original experimental validation study

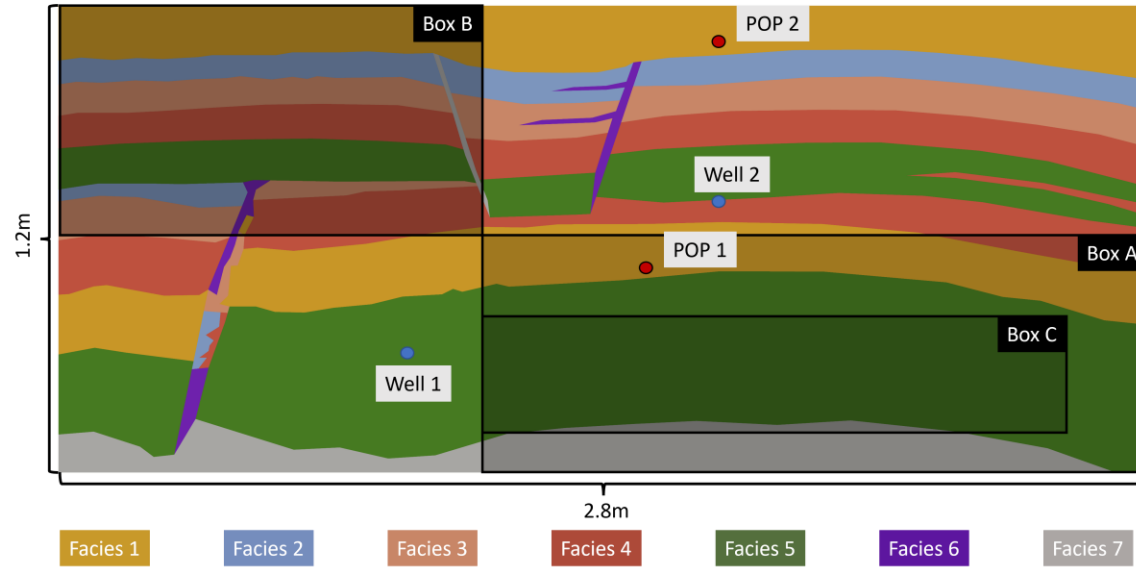
# The 11th SPE Comparative Solution Project

## Baseline Geometry



# The 11th SPE Comparative Solution Project

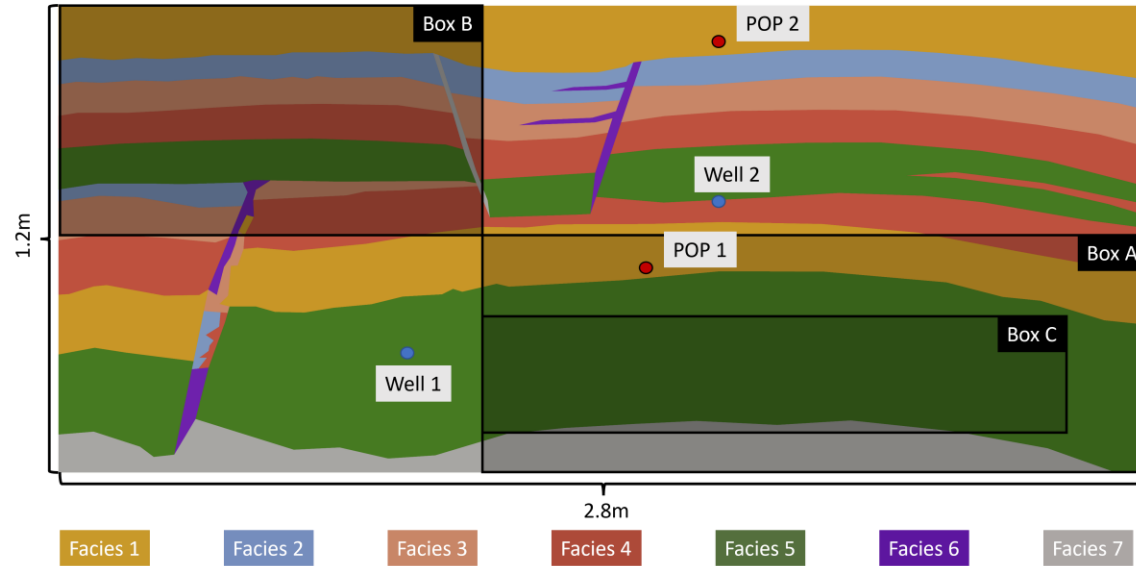
## SPE11A – Lab Conditions



- Two-phase, two-component, isothermal
- 5 hour injection in Well 1, 2.5 hour injection in Well 2
- 120 hour total simulation time

# The 11th SPE Comparative Solution Project

## SPE11A – Lab Conditions

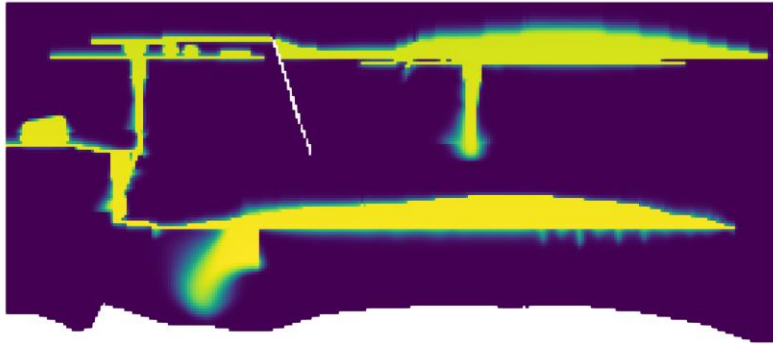


### Reporting requirements

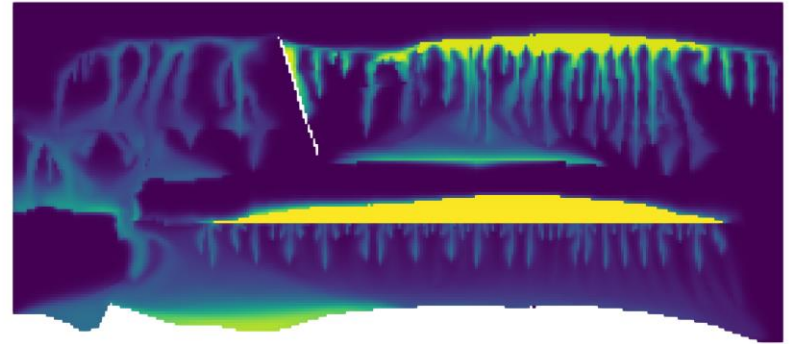
- Time-history of target quantities (proxies for storage safety)
- All field variables at 1 hour intervals on a 1 cm by 1 cm grid
- Various performance metrics

# The 11th SPE Comparative Solution Project

## Example Simulation of SPE11A



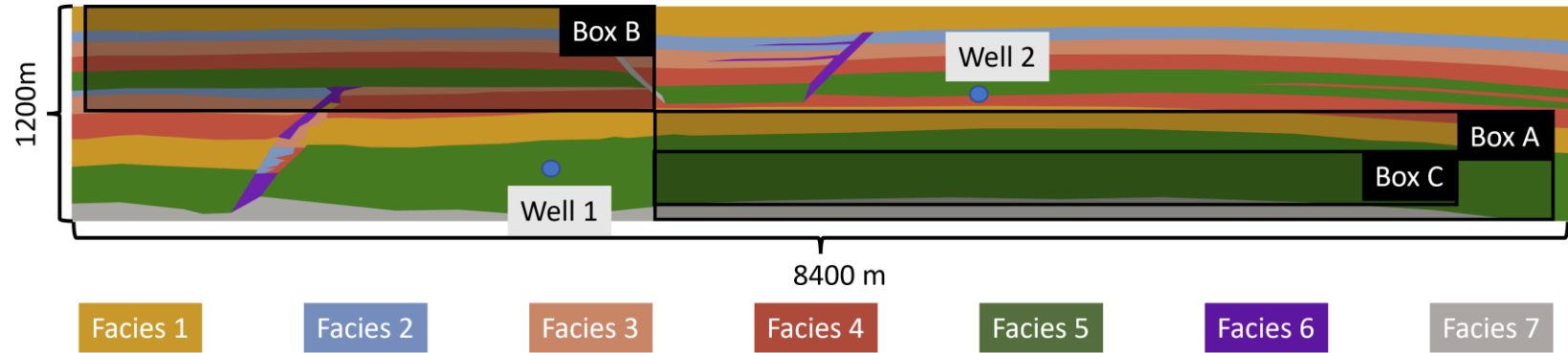
Injection stop



48 hours

# The 11th SPE Comparative Solution Project

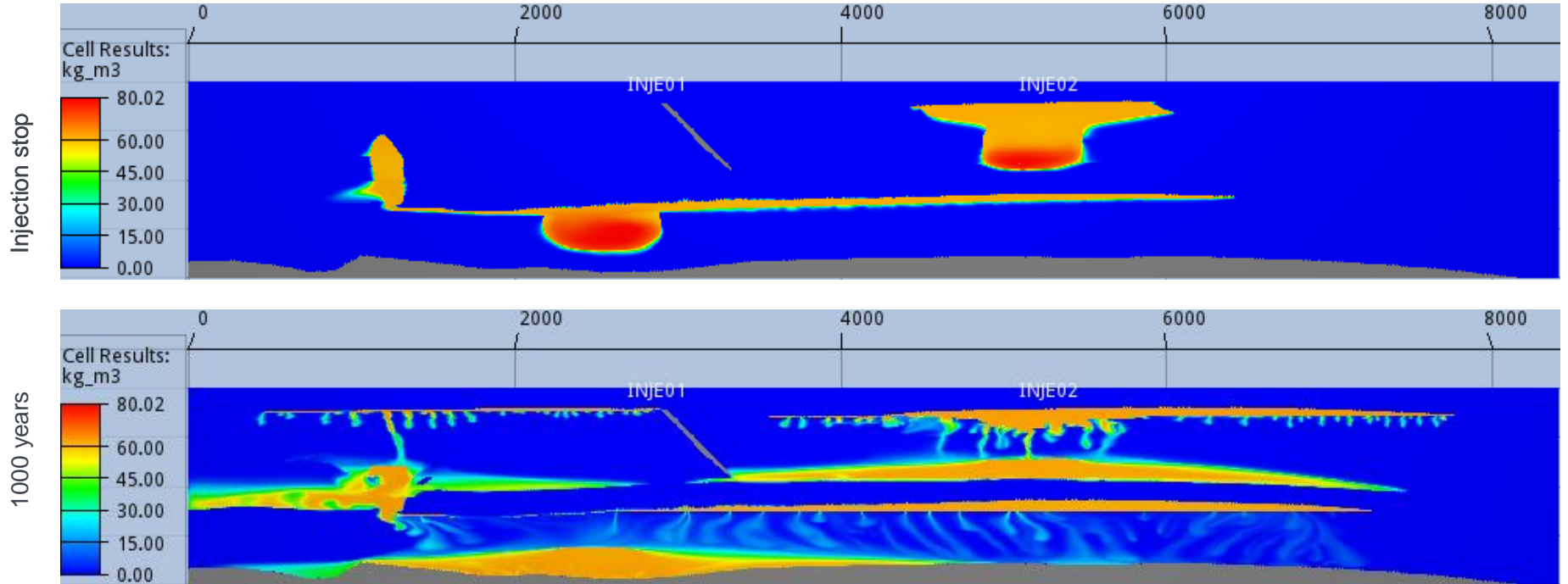
## SPE11B – 2D Field Transect



- Geometry from 11A stretched 3000:1 and 1000:1
- Two-phase, two-component, thermal
- 1000 year pre-injection equilibration
- 50 year injection in Well 1, 25 year injection in Well 2, at 10 degrees Celsius
- 2000 year total simulation time
- Reporting requirements as for 11A, but sparser in space and time

# The 11th SPE Comparative Solution Project

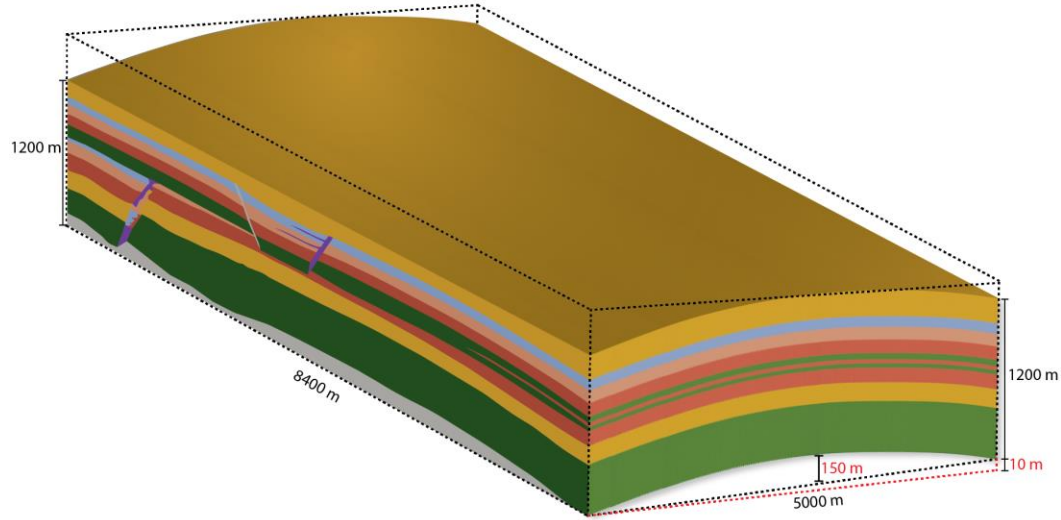
## Example Simulation of SPE11B





# The 11th SPE Comparative Solution Project

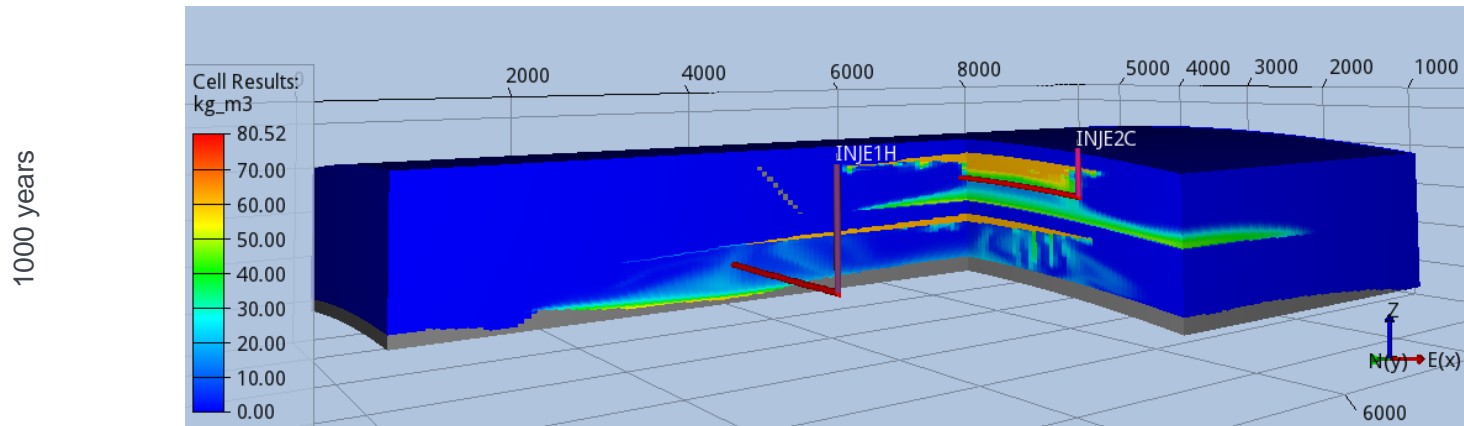
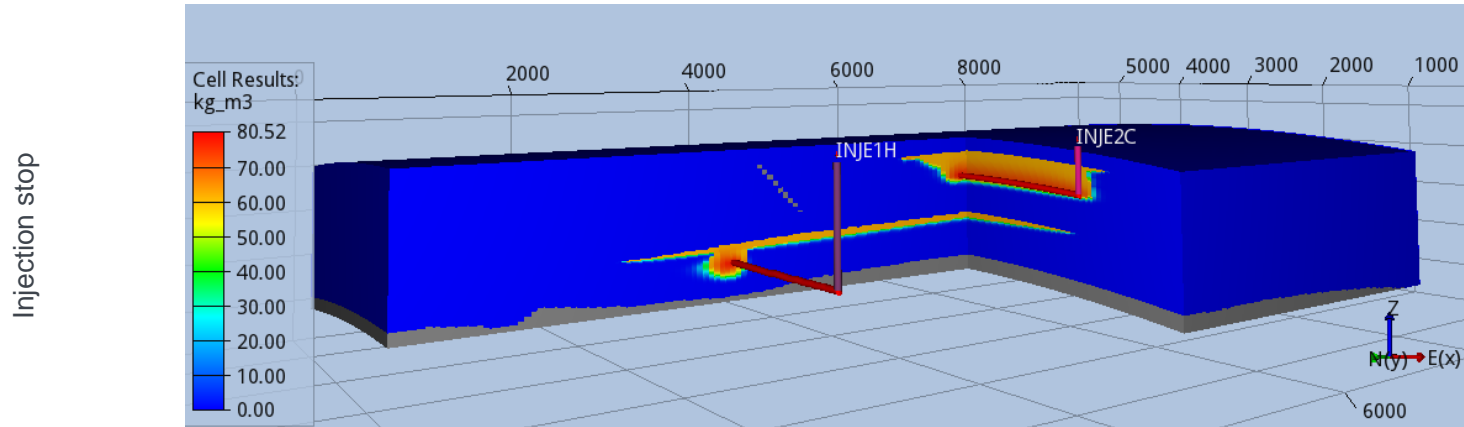
## SPE11C – 3D Field



- Geometry from 11B stretched 5000 meters along a parabola with slight skew
- All model equations and parameters as in 11B
- Well 1 is horizontal, Well 2 is arched following the layering
- Injection schedule and simulation time as for 11B
- Reporting requirements as for 11B, but yet sparser in space and time

# The 11th SPE Comparative Solution Project

## Example simulation of SPE11C



# The 11th SPE Comparative Solution Project

## Some Known Challenges

- Common for all three versions:
  - Capillary entry pressure is a leading storage mechanism during injection
  - Injection of dry CO<sub>2</sub> leads to essentially immobile water saturation with very high capillary pressures
  - Convective mixing is the dominant physical process post-injection, but is difficult to resolve without an excessive number of grid cells
  - Cartesian grids tend to give unphysical “stair-case-like” dissolution rates post-injection.
  - Reporting metrics are sensitive to numerical errors

• SPE11A: Low density of CO<sub>2</sub> in gas phase leads to particularly strong non-linearities as gas “vanishes” into the water phase.

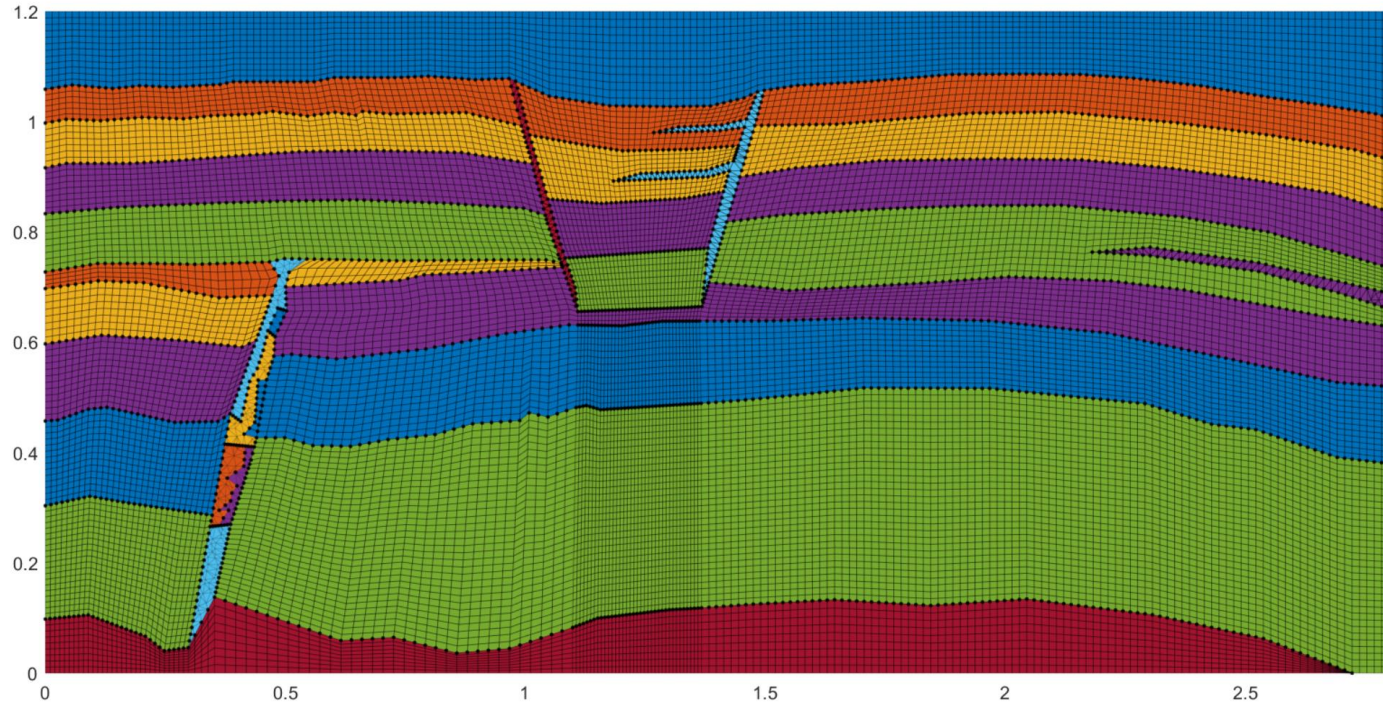
• SPE11B: Two-phase flow physics easier(?) than 11A, but thermal effects must be resolved.

• SPE11C:

- The computational cost of three dimensions implies that properly resolving convective mixing is almost impossible on standard hardware.
- Results will likely show strong grid dependence, or require upscaling methods.

# The 11th SPE Comparative Solution Project

## Example Challenge: Gridding



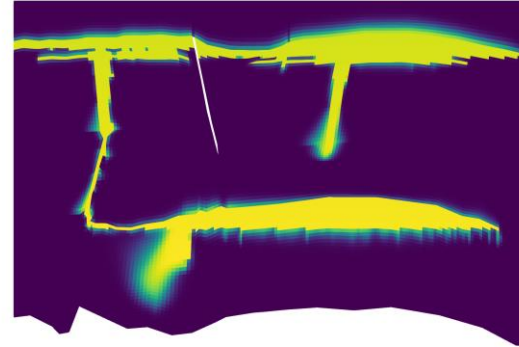
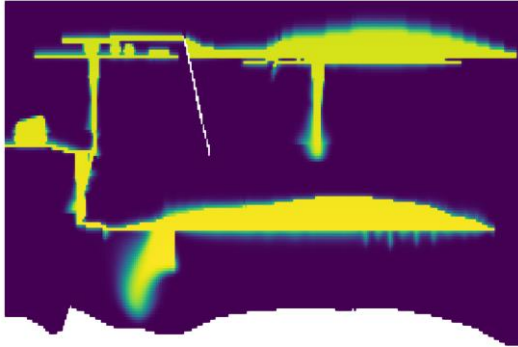
# The 11th SPE Comparative Solution Project

## Example Challenge: Grid-dependent solutions on 11A

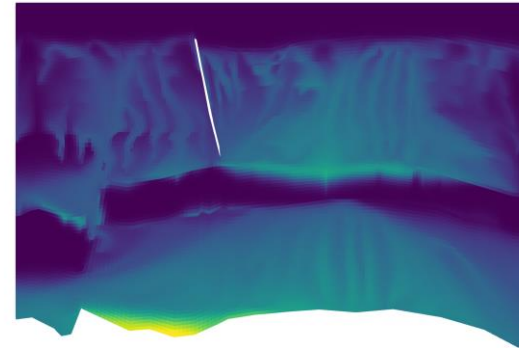
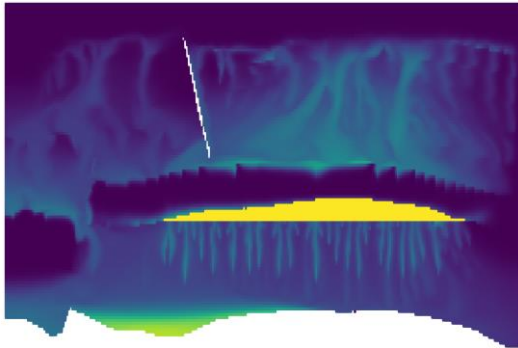
Cartesian grid

Unstructured grid

Injection stop

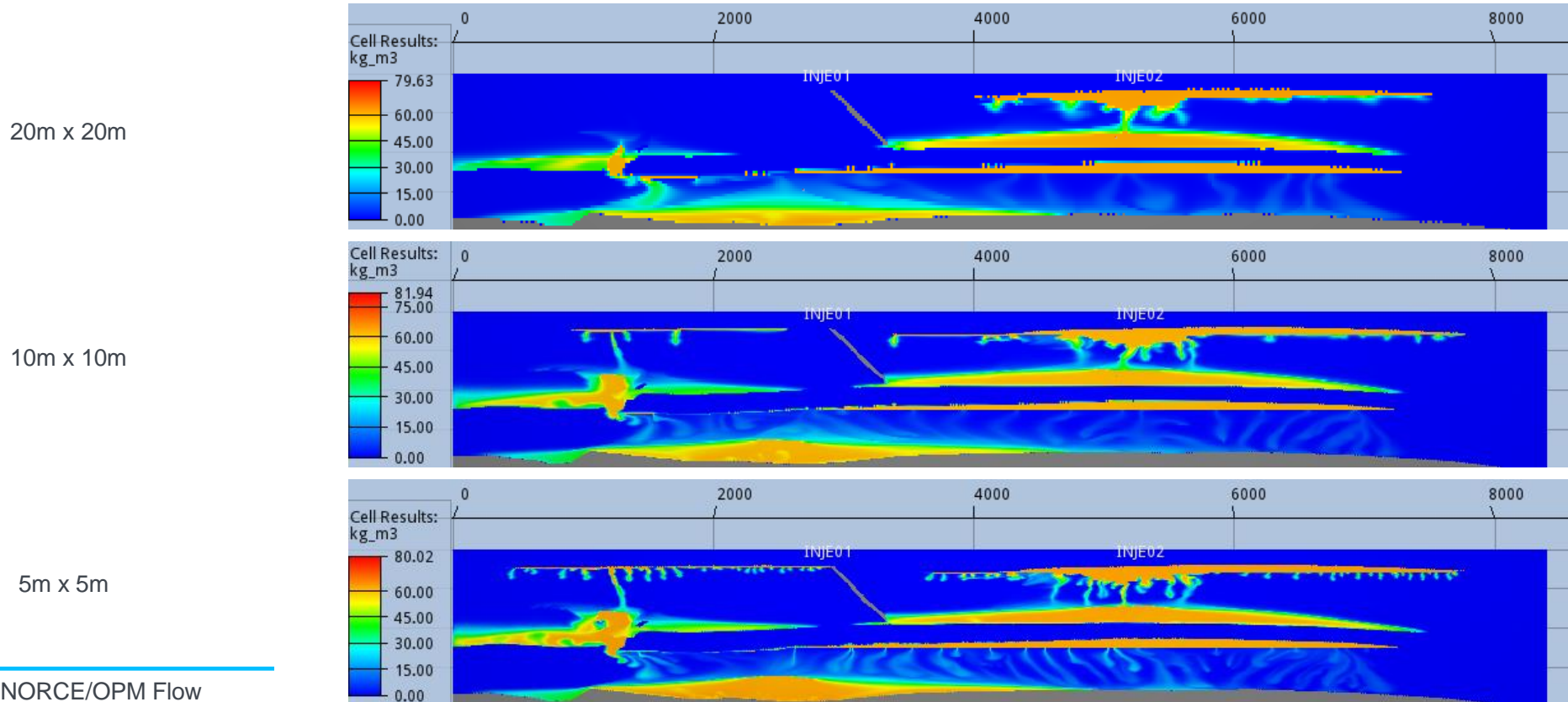


5 days



# The 11th SPE Comparative Solution Project

## Example challenge: Sensitivity to grid resolution for 11B



# The 11th SPE Comparative Solution Project

## Example challenge: Computational times

Case	Dimensions [m]	Max. grid size [m]	No. grid cells	Total no. cells	No. active cells	Solver time step [d]	Total simulation time [s]
spe11a^	[2.8, 0.01, 1.2]	[0.01, 0.01, 0.01]	[280, 1, 120]	33600	31034	1e-5	2118.30
spe11b^*	[8400, 1, 1200]	[10, 1, 10]	[842, 1, 120]	101040	93318	50	1420.15
spe11c^*	[8400, 5000, 1350]	[50, 50, 10]	[170, 100, 120]	2040000	1885200	50	25450.68

^ All three cases were run with 70 MPI processes and 2 threads per MPI process. i.e., 140 cpu cores.  
\* spe11b and spe11c have an extra layer [1 m] of grid cells on the left and right boundaries to include the buffer volume  
.. The solver time step is the maximum value allowed by the simulator

CPU time used is over 50 days for the SPE11C at this resolution

# The 11th SPE Comparative Solution Project

## Expected developments in the context of SPE11

- Development and verification of **accurate and efficient discretization methods** for multiphase, multicomponent flow and transport.
- Development and verification of **space-time adaptive gridding and domain decomposition methods**.
- Development of **upscaling methods for convective mixing and dispersion** of in the context of CO<sub>2</sub> dissolution into water.
- Development and verification of **robust and efficient linear and non-linear solvers** and solution and time-stepping strategies for 2D and 3D at laboratory and field conditions.
- Assessment of the **importance of physical processes omitted from this study**, including (but not limited to) geochemical reactions, mechanical response, and more realistic boundary conditions.



# The 11th SPE Comparative Solution Project Resources

Official webpage:


<https://spe.org/csp>

Community resources:

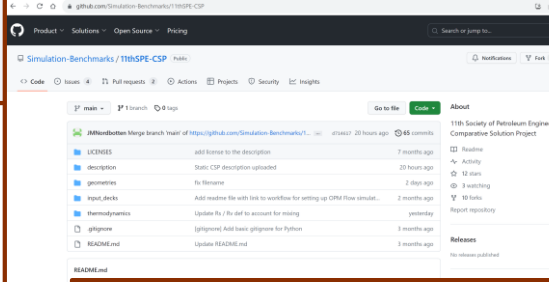
<https://github.com/Simulation-Benchmarks/11thSPE-CSP>

Discussion at SPE Connect:

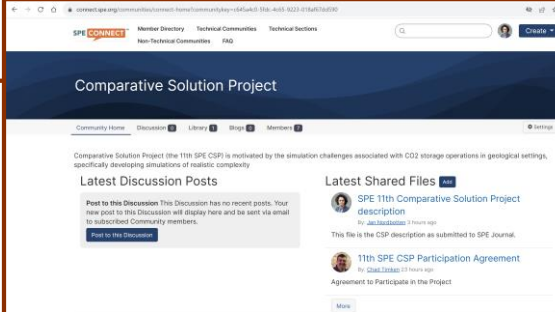
<https://connect.spe.org/home/memberhome>



The screenshot shows the official website for the 11th Society of Petroleum Engineers Comparative Solution Project. The page features a navigation bar with links for Membership, Events, Publications, Training, Resources, and Community. The main heading reads "The 11th Society of Petroleum Engineers Comparative Solution Project". Below this, there is a "Call For Participation" section with a brief description of the project's focus on CO2 storage operations. To the right, a "TIMELINE" section lists key dates: 29 March 2023 (Official announcement), 16-18 October 2023 (Special session at SPE ATCE), and 1 December 2023 (Open call for participation period ends).



The screenshot displays the GitHub repository for "Simulation-Benchmarks / 11thSPE-CSP". The repository is public and includes a README file. The file list shows various sub-directories and files, including LICENSES, description, geometries, input\_decks, thermodynamics, gitignore, and README.md. The commit history is visible, showing recent updates to the README and other files.



The screenshot shows the SPE Connect community page for the Comparative Solution Project. The page includes a navigation bar with links for Member Directory, Technical Communities, and Technical Sections. The main heading is "Comparative Solution Project". Below this, there is a "Latest Discussion Posts" section with a button to "Post to this Discussion". To the right, there is a "Latest Shared Files" section with a button to "Share". The page also features a "Community Home" section with a brief description of the project and a "Members" section with a list of members.

# The 11th SPE Comparative Solution Project

## Timeline

- March 29, 2023: First announcement at the 2023 SPE Reservoir Simulation Conference, Galveston, Texas.
- October 1, 2023: Final date for publication of corrections or amendments to the CSP description.
- October 16-18, 2023: Special session at SPE Annual Technical Conference and Exhibition (ATCE).
- December 1, 2023: Open call for participation period ends.
- **March 1, 2024: Deadline for submission of early CSP simulation results.**
- March, 2024: First intercomparison workshop for all CSP participants (virtual).
- **September 1, 2024: Deadline for submission of final CSP simulation results.**
- September, 2024: Final intercomparison workshop for all CSP participants (hybrid).
- December 2024: Completion of draft report on the results of the CSP.
- February 2025: Report on the results of the CSP finalized and submitted.
- **March, 2025: Special session at the 2025 SPE Reservoir Simulation Conference, Galveston, Texas.**

# The 11th SPE Comparative Solution Project SPE Journal Special Issue

- SPE11 special issue already live!
- Two-year paper submission window.
- Continuous publication.
- Open for all CSP-related research papers!



SPE Journal

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SPE Journal

Covers novel theories and emerging concepts (not including review articles or multi-part articles) spanning all aspects of engineering for oil and gas exploration and production, including drilling and completions, geomechanics, production and facilities, oilfield chemistry, CO<sub>2</sub> sequestration and injection, reservoir evaluation and engineering, numerical simulation, data analytics, economics and externalities including health, safety, environment, and sustainability. [Read more](#)

## The 11th Society of Petroleum Engineers Comparative Solution Project: Problem Definition

Jan M. Nordbotten<sup>1</sup>, Martin A. Ferno<sup>2</sup>, Bernd Flemisch<sup>3</sup>, Anthony R. Kovscek<sup>4</sup>, and Knut-Andreas Lie<sup>5</sup>

<sup>1</sup>Department of Mathematics, University of Bergen; Norwegian Research Center (NORCE)  
<sup>2</sup>Department of Physics and Technology, University of Bergen; Norwegian Research Center (NORCE)  
<sup>3</sup>Institute for Modelling Hydraulic and Environmental Systems, University of Stuttgart  
<sup>4</sup>Energy Science & Engineering, Stanford University  
<sup>5</sup>SINTEF Digital, Mathematics & Cybernetics

### Summary

This article contains the description of, and call for participation in, the 11th Society of Petroleum Engineers Comparative Solution Project (the 11th SPE CSP, <https://spe.org/csp/>). It is motivated by the simulation challenges associated with CO<sub>2</sub> storage operations in geological settings of realistic complexity. The 11th SPE CSP contains three versions: Version 11A is a 2D geometry at the laboratory scale, inspired by a recent CO<sub>2</sub> storage forecasting and validation study. For Version 11B, the 2D geometry and operational conditions from 11A are rescaled to field conditions characteristic of the Norwegian Continental Shelf. Finally, for Version 11C, the geometry of Version 11B is extruded to a full 3D field model. The CSP has a two-year timeline, being launched at the 2023 SPE Reservoir Simulation Conference and culminating at the 2025 SPE Reservoir Simulation Conference. A community effort is run in parallel to develop utility scripts and input files for common simulators to lower the threshold of participation; see the link to supplementary material on the CSP website. At the time of writing, complete input decks for one simulator are already ready for all three versions.

### Introduction

Safe and efficient implementation of geological carbon storage (GCS) necessarily relies on reservoir simulators applied to uncertain geological data. While the strengths and limitations of reservoir simulation are well appreciated within petroleum production, GCS raises new challenges both in terms of physical processes and timescales. As an example, the enhancement of dissolution from a CO<sub>2</sub>-rich supercritical phase to the aqueous phase through convective mixing ensures important long-term storage security, relevant on timescales from decades to centuries.

One consequence of the relative youth of the GCS industry, combined with the long timescales and new physical processes of interest, is that available field data for validation of simulation technology is still rare. This increases the importance of validation against proxy systems and code verification through comprehensive benchmarking efforts among simulators.

**Background and Motivation.** During 2021–22, three of the present organizers led a forecasting and validation study within the academic GCS community (Nordbotten et al. 2022; Flemisch et al. 2023), as illustrated in Fig. 1. The primary intent was to validate the long-term performance of numerical simulators for GCS, with particular emphasis on the post-injection period, and to assess the ability to state accurately well-calibrated forecasting intervals. The study also revealed several numerical challenges, both in terms of numerical accuracy when resolving the reservoir dynamics and in terms of obtaining good solver performance (see, e.g., Flemisch et al. (2023); Saló-Salgado et al. (2023); Wapperom et al. (2023)).

Separately, the development of numerical simulation capabilities for subsurface applications has historically benefited substantially from common reference simulation cases, notably the series of 10 CSPs organized within the SPE between 1981 and 2001 [see Islam and Sepulchero (2013) for a review]. These observations provided the initial motivation for developing a set of benchmark cases for CO<sub>2</sub> storage within the concept of a new SPE CSP.

In developing this 11th SPE CSP (<https://spe.org/csp/>), we hope to provide a common platform and reference case for numerical simulation of GCS. Specifically, we anticipate that the following topics will be discussed relative to this baseline:

- Development and verification of accurate and efficient discretization methods for multiphase, multicomponent flow and transport.
- Development and verification of space-time adaptive gridding and domain decomposition methods.
- Development of upscaling methods for convective mixing and dispersion in the context of CO<sub>2</sub> dissolution into water.
- Development and verification of robust and efficient linear and nonlinear solvers and solution and timestepping strategies for 2D and 3D at laboratory and field conditions and well models.
- Assessment of the importance of physical processes omitted from this study, including (but not limited to) geochemical reactions, mechanical response, and more realistic boundary conditions.

Furthermore, as of the date of launching this CSP, we do not anticipate that a fully converged solution (in the sense of grid refinement) will be achievable for any of the three versions of the CSP by means of standard numerical methods on desktop hardware. This anticipation is justified in part based on the experiences from the previous academic benchmark cited above and in part due to the known challenges associated with accurately simulating the dissolution and convective mixing of CO<sub>2</sub> into water, in particular outside the context of

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# Outline

1. Motivation
2. Categorization
3. Selected GCS Benchmark Studies
  - a. The Classic
  - b. So Simple, Yet So Hard
  - c. Reality Meets Modeling
  - d. Back To Normal, But Bigger
4. **Summary and Conclusion**

# Summary and Conclusion

## Take-Home Messages

- Verification and validation are **indispensable** for computational model development.
- Available benchmarks **facilitate** V&V tasks.
- Conducting benchmark studies helps to **bond/build/grow** communities.
- **No standardized V&V protocols** for the “GCS modeling community” exist.
- Standard models capture the **physical processes correctly**.
- Modelers tend to be **overconfident** in their own predictions.
- Predicted confidence intervals are typically **too narrow**.



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Department of Hydromechanics and Modelling of Hydrosystems

**Thank you!**



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University of Stuttgart

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J. Nordbotten, M. Fernø, M.

Jørgensen, R. Juanes

+ co-workers

+ all participants

- **11<sup>th</sup> SPE CSP:**

J. Nordbotten, M. Fernø, A. Kovscek,

K.-A. Lie

T. H. Sandve, D. Landa Marban

H. Nilsen, O. Andersen, O. Møyner,

V. Nevland

M.A. Giddins, J. Haukås

H. Class, D. Gläser, K. Wendel