

Diophantine Approximation, Fractal Geometry and Related topics / Approximation diophantienne, géométrie fractale et sujets connexes

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On the b -ary expansion of e

Let $b \geq 2$ be an integer. The exponent v_b (resp., v_b') and the uniform

rational numbers whose denominator is a power of b (resp., is of the form $b^r(b^s - 1)$). Said differently and informally, we look at the lengths of the blocks of digit 0 (or of digit $(b - 1)$) and at the lengths of repeated blocks in the base- b expansion of a

exponent $v_{\infty,b}$ (resp., v_{∞}) measure the quality of approximation to a real number by b

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real number. We discuss several results on these four exponents and explain how an inequality between v and v_{∞} implies that the base- b expansion of any real number whose irrationality exponent is sufficiently close to 2 cannot be too 'simple', in the sense that it contains at least cn different blocks of digits of length n , for some $c > 1$ and every integer n sufficiently large. In particular, the b -ary expansion of e contains at least $10n/9$ different blocks of digits of length n , if n is large enough.