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On Hausdorff dimension in inhomogeneous Diophantine approximation over global function fields

We study inhomogeneous Diophantine approximation by elements of a global function field (over a finite field) in its completion for a discrete valuation. Given an (m,n) matrix A with coefficients in this completion and a small $r > 0$, we obtain an effective upper bound for the Hausdorff dimension of the set $\text{Bad}_A(r)$ of r -badly approximable m -dimensional vectors, using an effective version of entropy rigidity in homogeneous dynamics for an appropriate diagonal action on the space of integral grids. We further characterize the matrices A for which $\text{Bad}_A(r)$ has full Hausdorff dimension for some $r > 0$ by a Diophantine condition of singularity on average. This is a joint work with Taehyeong Kim and Seonhee Lim.