

Diophantine Approximation, Fractal Geometry and Related topics /  
Approximation diophantienne, géométrie fractale et sujets connexes

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“Simultaneously dense and non-dense” orbits in homogeneous dynamics and  
Diophantine approximation

Consider a non-compact homogeneous space  $X$  with the action of a diagonal one-parameter subgroup. It is known that the set of points in  $X$  with bounded forward orbits has full Hausdorff dimension. Question: what about points with forward orbits both bounded and accumulating on a given  $z \in X$ ? We prove that, barring a certain obvious obstruction, those points also form a set of large Hausdorff dimension. This is motivated by the subject of improving Dirichlet’s Theorem in Diophantine approximation. Joint work with Manfred Einsiedler and Anurag Rao.