

SUBA-Jet

A New Coherent Jet Energy Loss Model For Heavy Ion Collisions

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Pol-Bernard Gossiaux, and Klaus Werner

[arXiv:2404.14579 \[hep-ph\]](https://arxiv.org/abs/2404.14579)

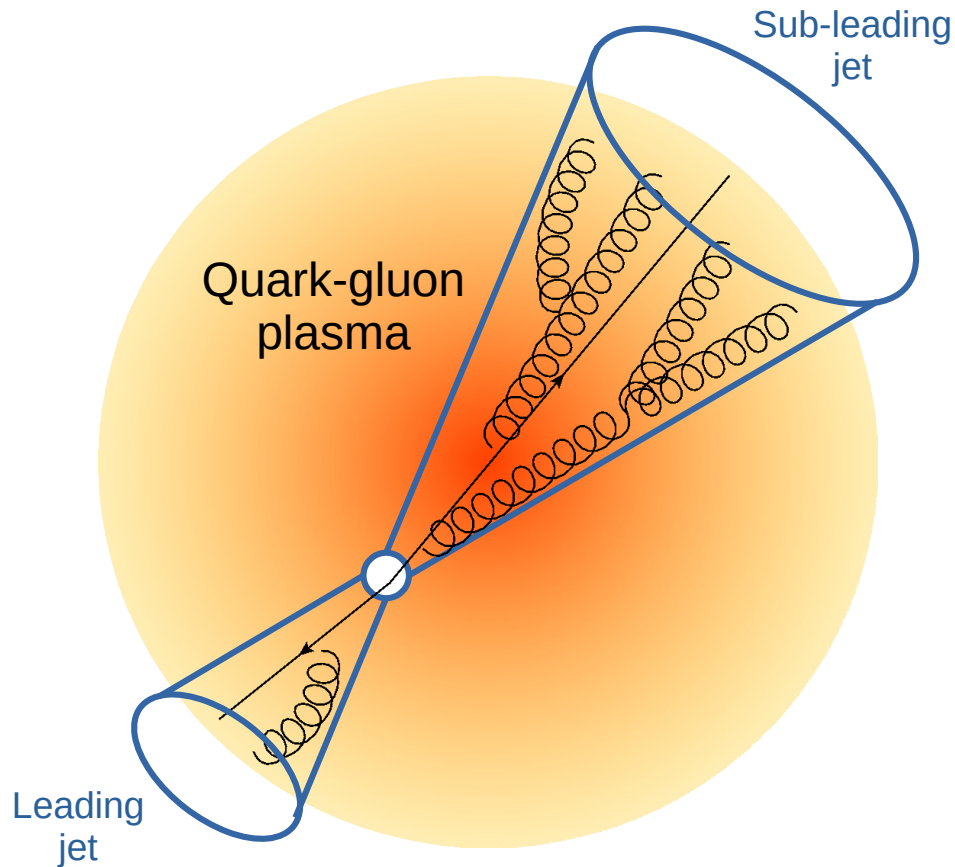


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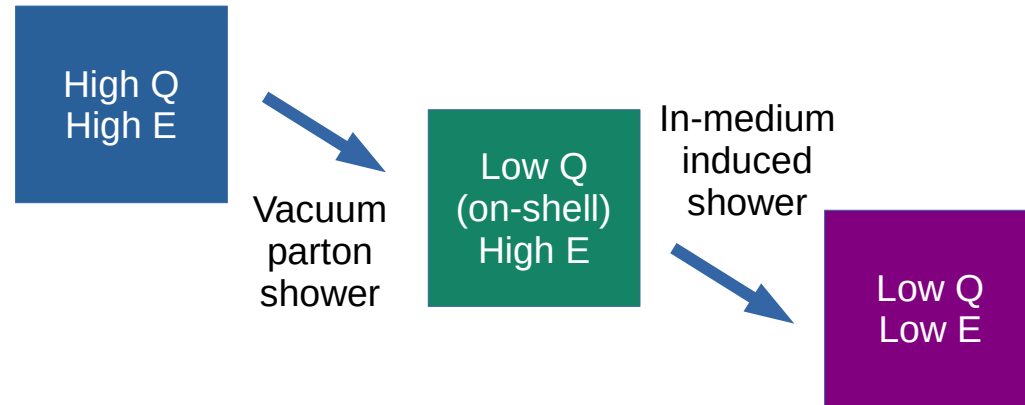
Jets in Heavy Ion Collisions



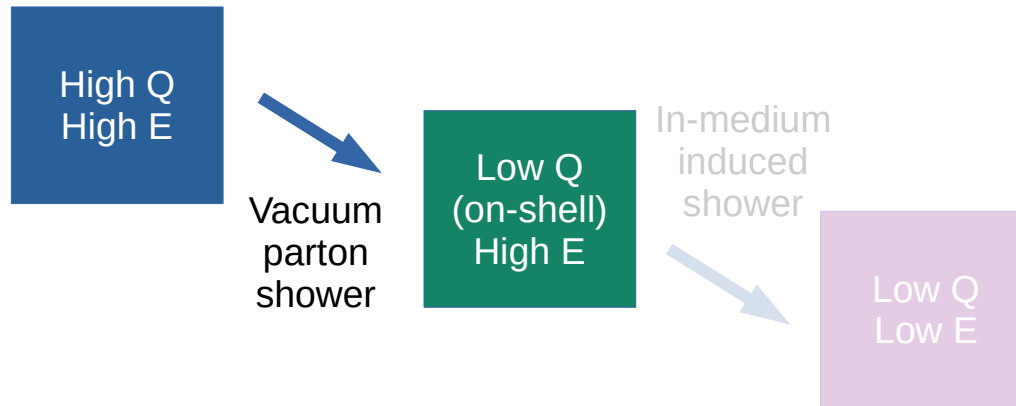
- Interactions between jet partons and the QGP medium leads to modifications of jet properties

→ **Jet Energy Loss / Quenching**

- **SUBA-Jet:**
Monte Carlo for jet energy loss in heavy ion collisions



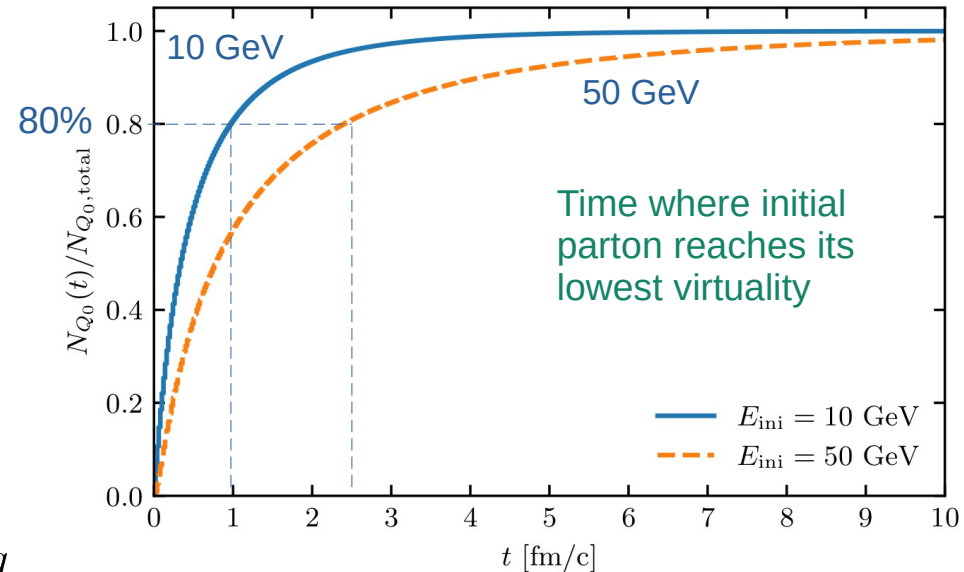
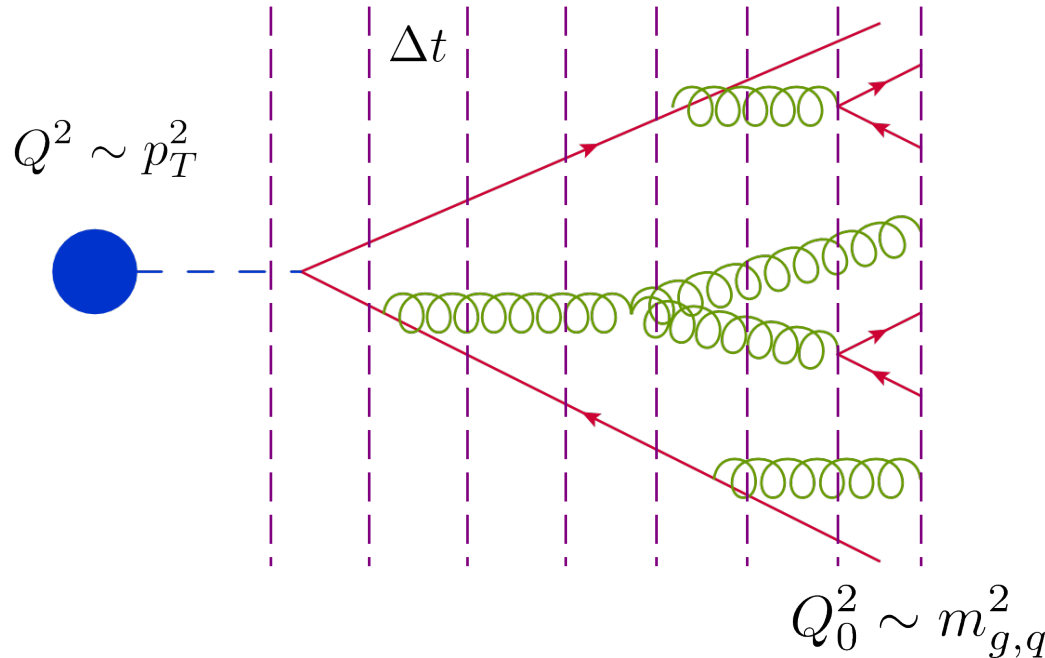
High Virtuality Regime



Vacuum Parton Shower

- Monte Carlo of a vacuum parton shower originally developed by Martin Rohrmoser
- Evolution according to the DGLAP equations from high virtuality $Q_{\max} \sim p_T$ to low virtuality Q_0
- Time evolution split into time steps, mean life time

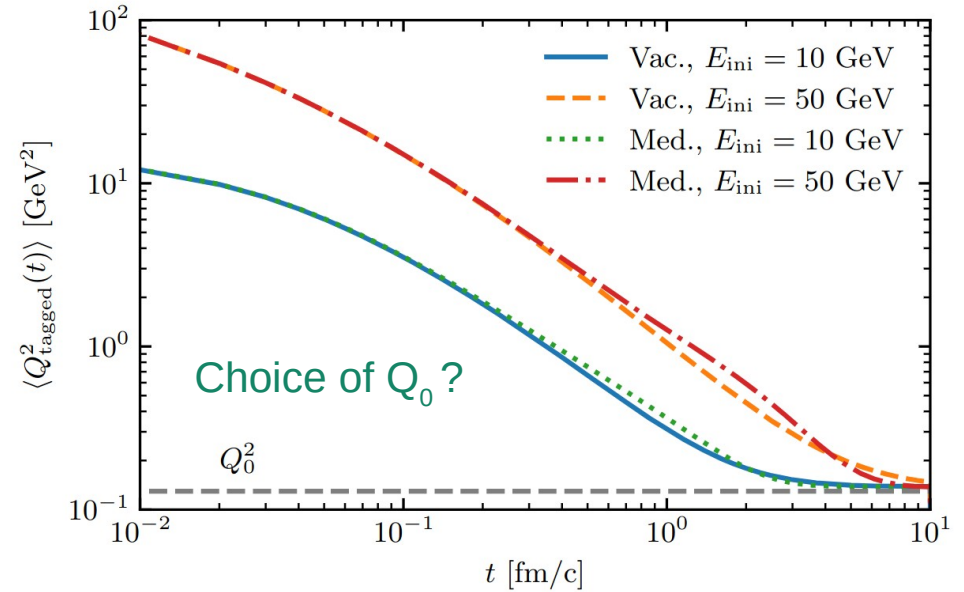
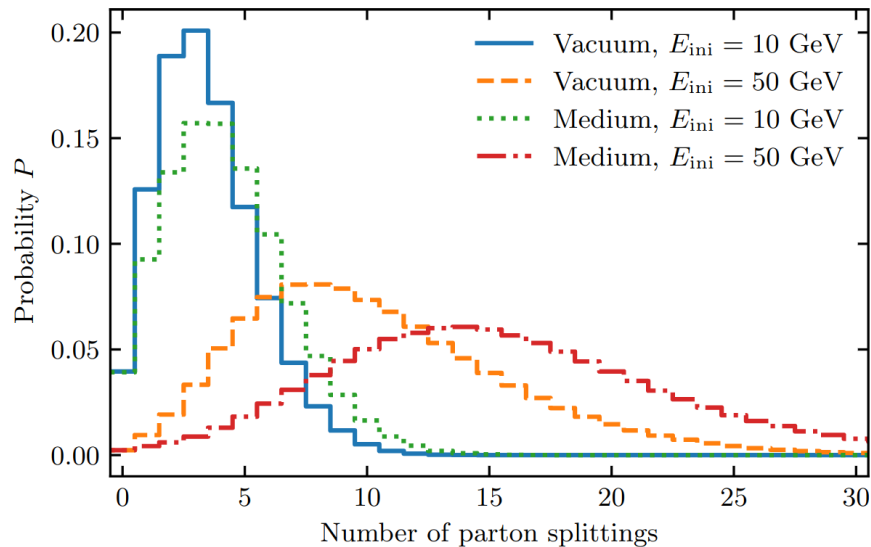
$$\Delta t = \tau = \frac{E}{Q^2}$$



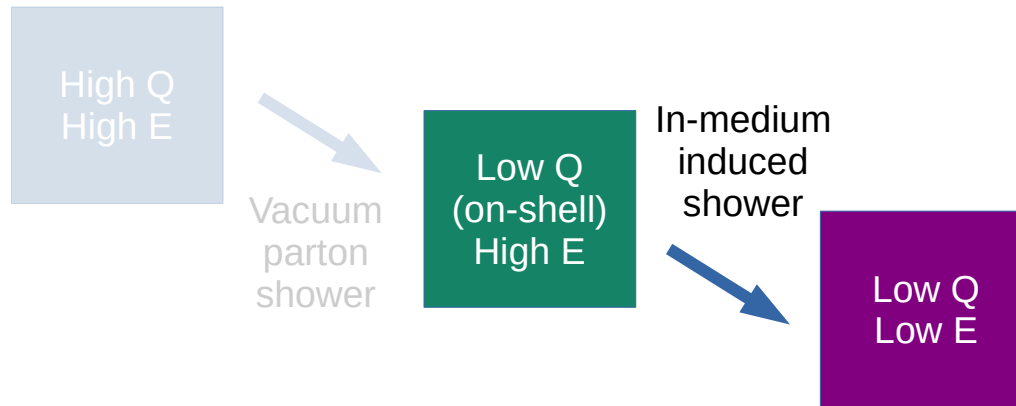
“Vacuum” Parton Shower in Medium

- Medium interactions for high Q regime resulting in virtuality increase, similar to YaJEM (T. Renk, 2008)

$$\frac{dQ^2}{dt} = \hat{q}(T)$$

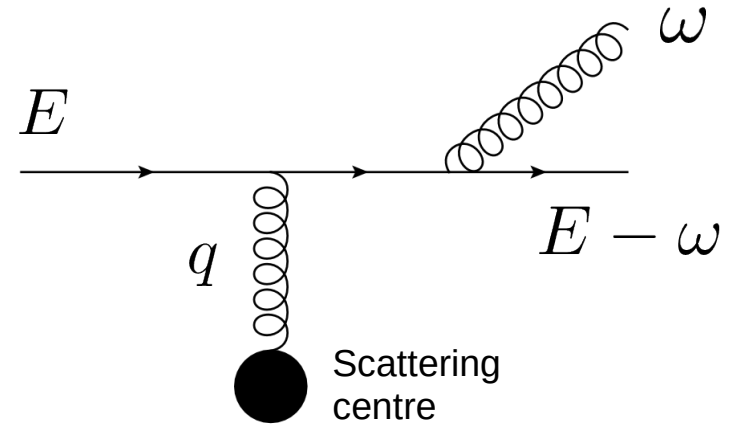


Low Virtuality Regime



Medium-Induced Single Radiation

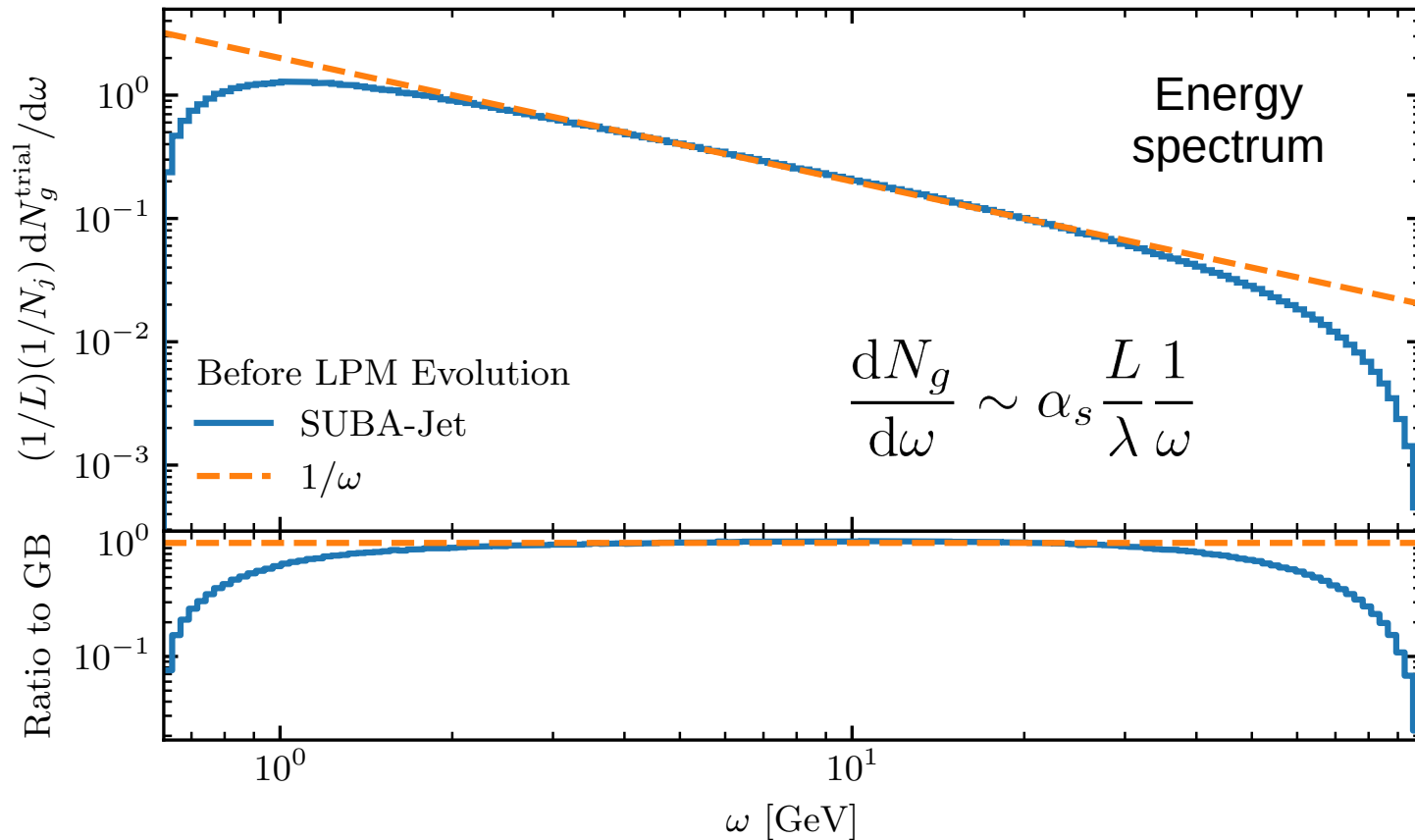
- **Inelastic collision:**
Single gluon emission from single medium scattering
- **Original result from Gunion-Bertsch (1982)**
Generalised to massive case by Aichelin, Gossiaux, Gousset (2014)
- **Initial Gunion-Bertsch seed:** i.e. radiation of a **preformed gluon** from a single scattering (Each parton can generate a number of preformed gluons)
- Gunion-Bertsch cross-section from scalar QCD



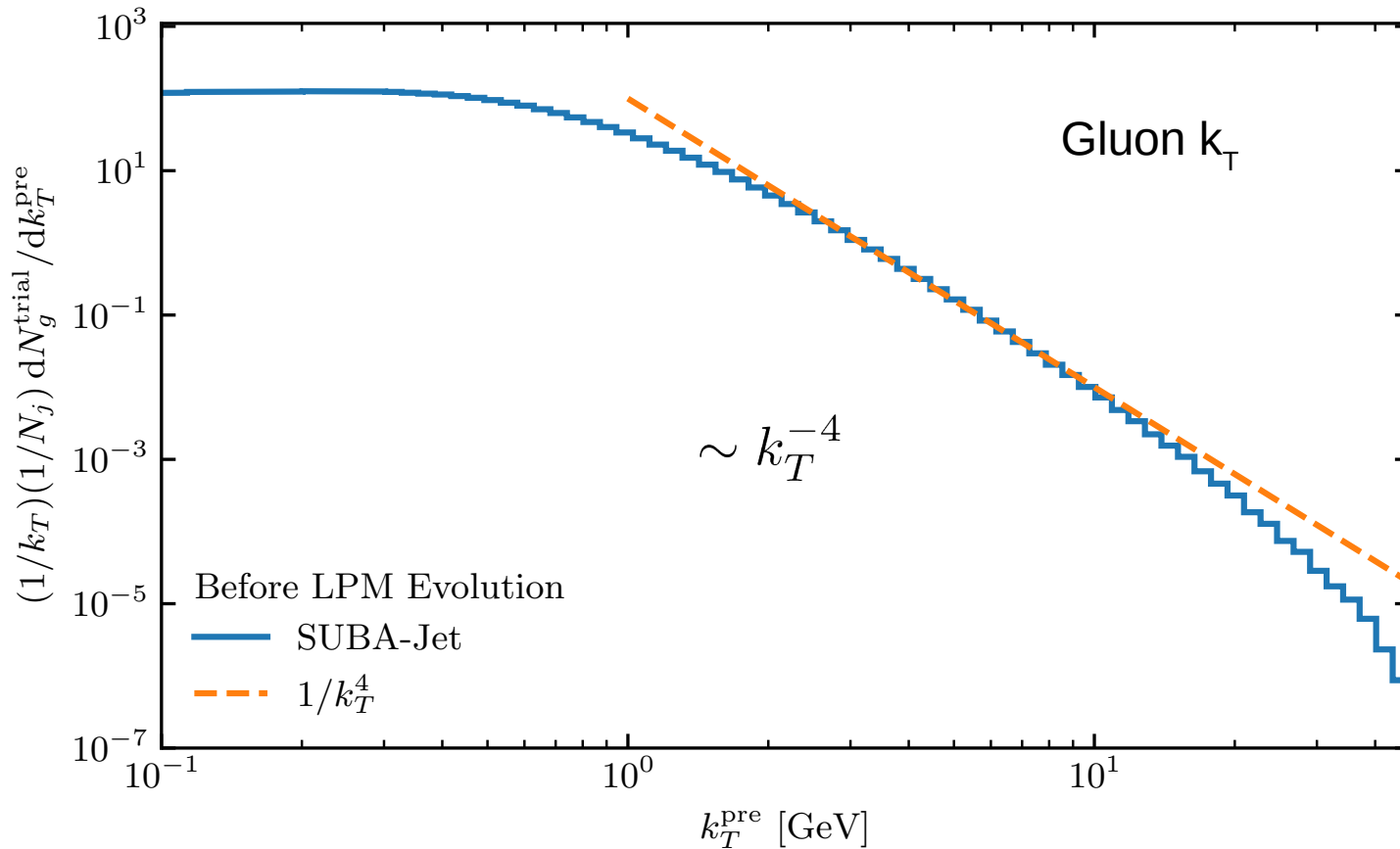
$$\frac{d\sigma^{Qq \rightarrow Qqg}}{dx d^2k_T d^2l_t} = \frac{d\sigma_{\text{el}}}{d^2l_t} P_g(x, k_T, l_T) \theta(\Delta)$$

$$\frac{d\sigma_{\text{el}}}{d^2l_t} \sim \frac{8\alpha_s^2}{9(l_T^2 + \mu^2)^2}$$

Medium-Induced Single Radiation



Medium-Induced Single Radiation



Coherency and the LPM Effect

- The formation of the radiated gluon is a quantum mechanical process

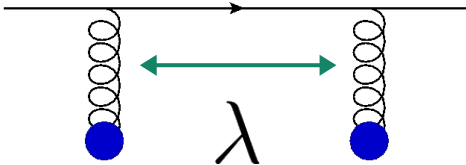
Formation time: $t_f \sim \sqrt{\frac{\omega}{\hat{q}}}$

- Coherence effects:
Landau-Pomeranchuk-Migdal (LPM) effect

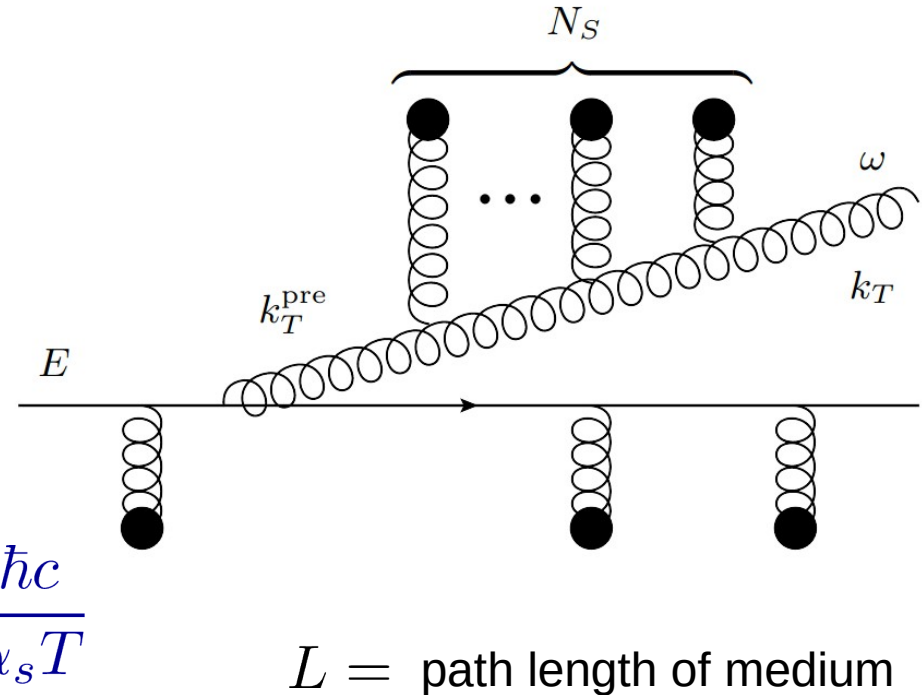
- Have to take into account multiple scatterings with the medium during the formation time

ω = gluon energy

\hat{q} = medium modifications

$$N_s = \frac{t_f}{\lambda}$$


$$\lambda \simeq \frac{\hbar c}{\alpha_s T}$$



Implementation of the LPM Effect

- At each timestep:

- Elastic scattering with prob. $\Gamma_{\text{el}}\Delta t$

$$\Gamma_{\text{el}}^q = \left(1 + \frac{N_f}{N}\right) \frac{(N^2 - 1)T^3}{\pi\hbar c} \frac{4\alpha_s^2}{\mu^2}$$

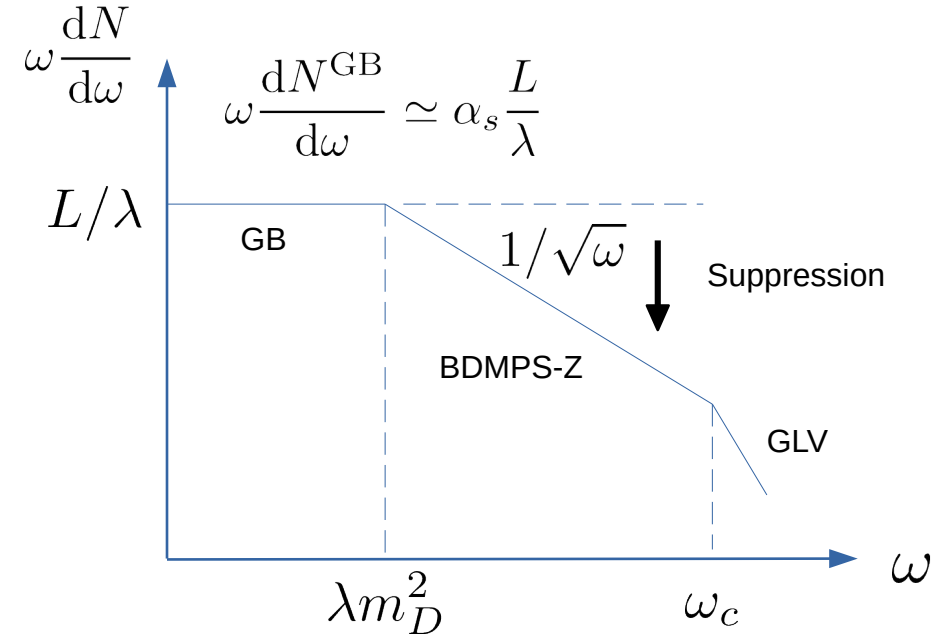
- Radiation of preformed gluon with prob. $\Gamma_{\text{inel}}\Delta t$

- BDMPS-Z spectrum at intermediate energies achieved by suppressing GB seed by

$$1/N_s$$

Like in Zapp, Stachel, Wiedemann, JHEP 07 (2011), 118

Radiation energy spectrum:



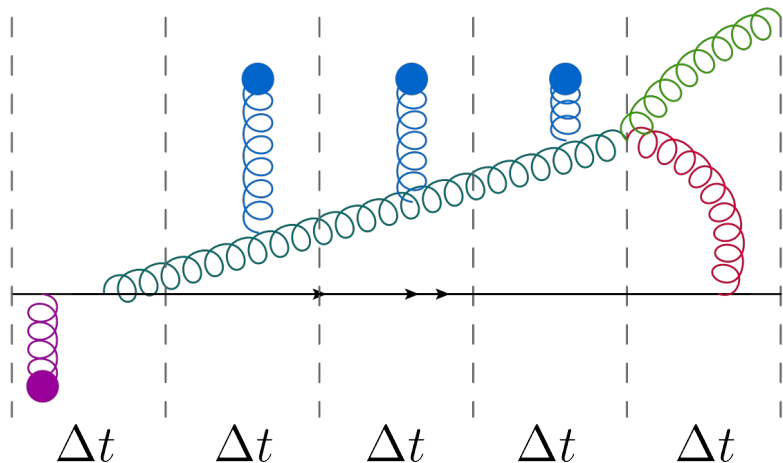
$$\omega \frac{dN^{\text{BDMPS-Z}}}{d\omega} \simeq \alpha_s \sqrt{\frac{\hat{q} L^2}{\omega}}$$

The Algorithm

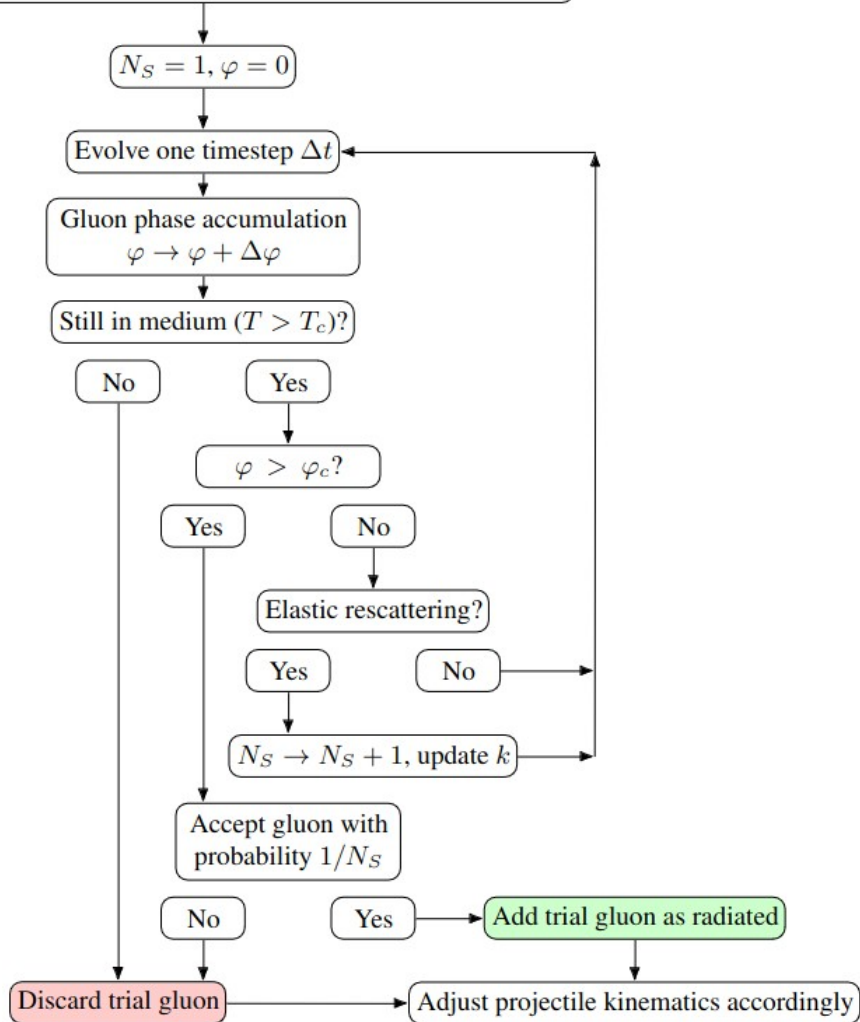
Flow diagram:

Algorithm for the coherent medium-induced gluon radiation in our model

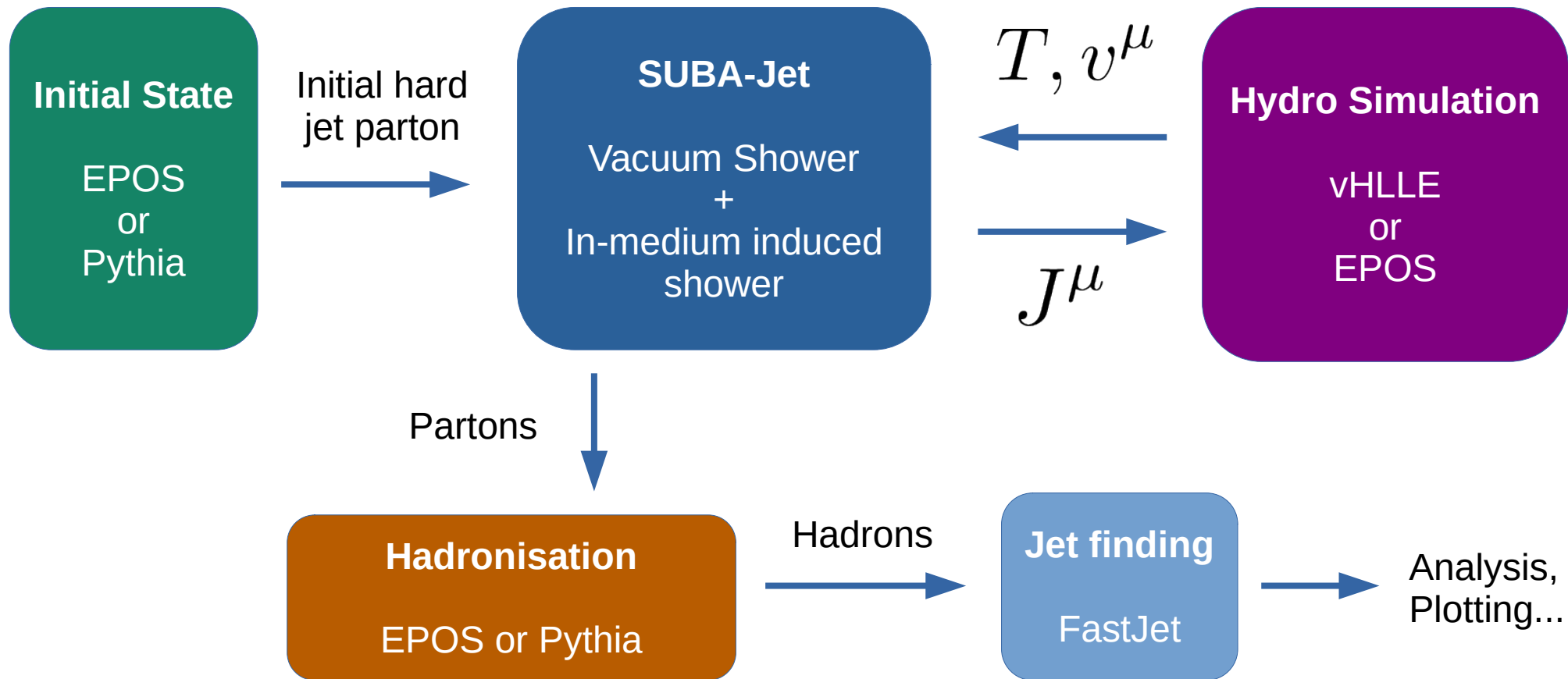
Various parameters and settings can be changed and tuned to compare distributions



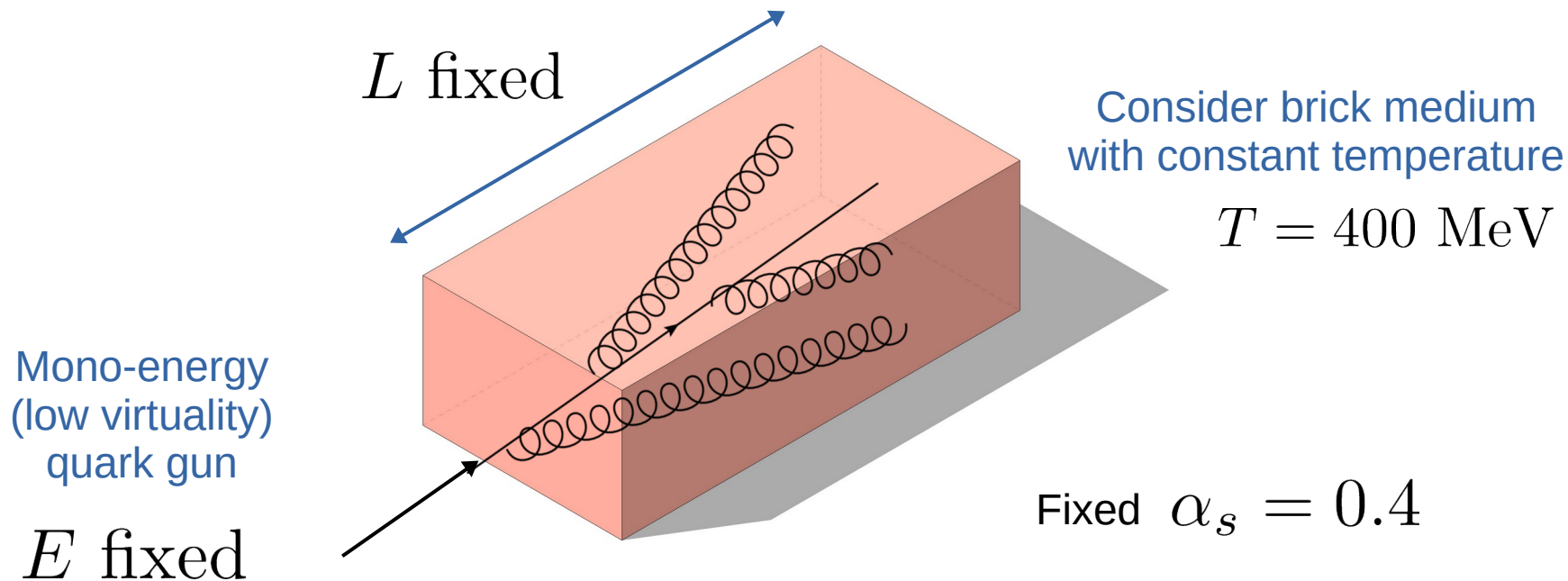
Trial (preformed) incoherent gluon formation according to GB seed



The Monte Carlo

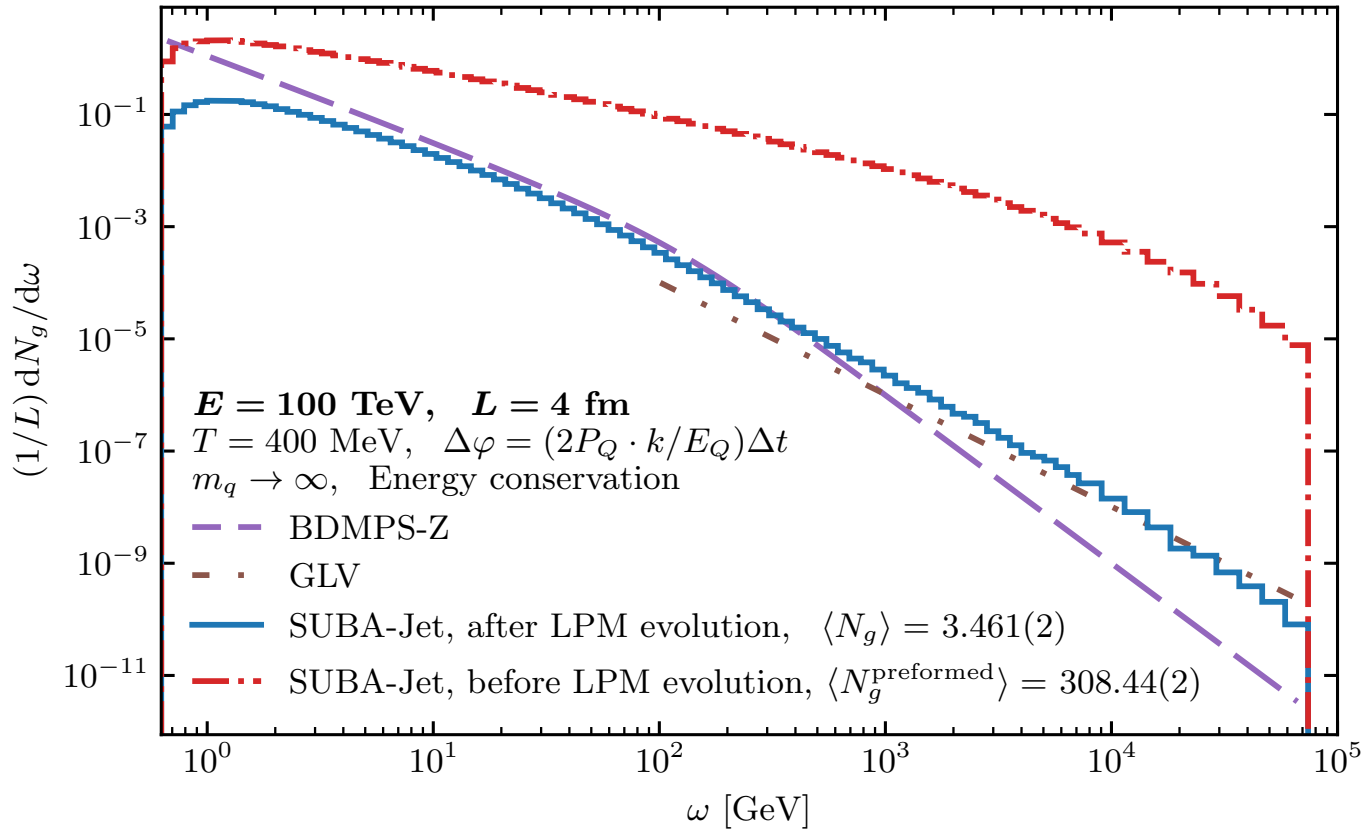


First Results



We want to reproduce theoretical expectation and check effect of model parameters

Reproduction of the LPM and GLV regimes



Gluon energy ω spectrum

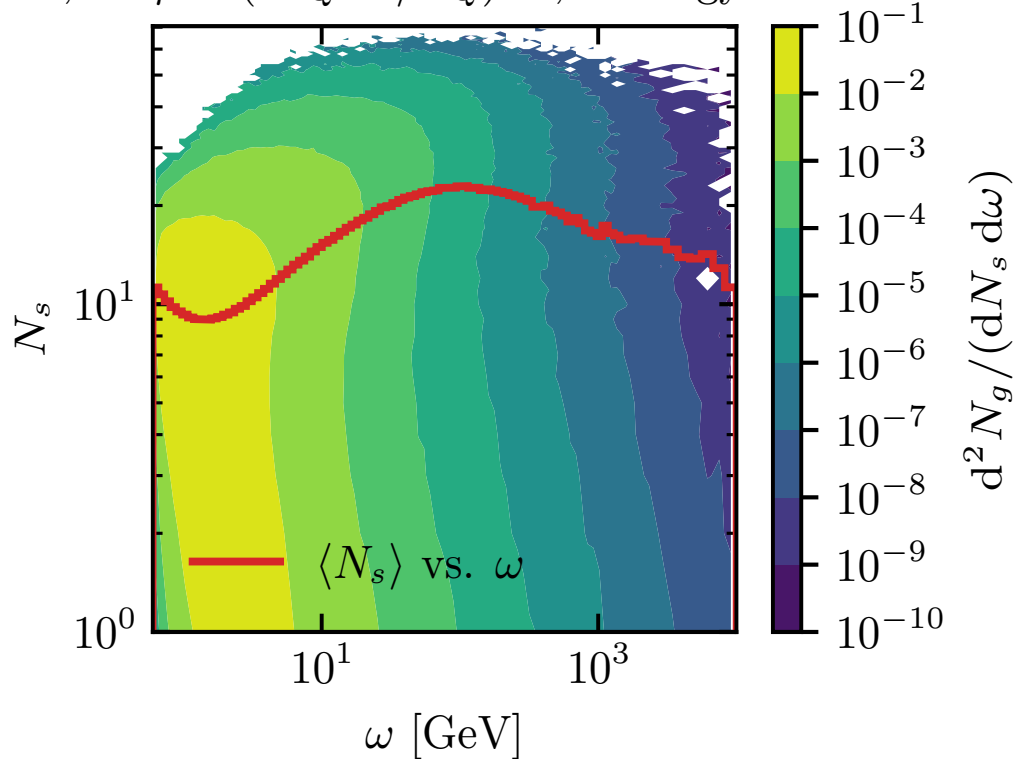
$$\frac{dN^{\text{LPM}}}{d\omega} \sim \frac{1}{\omega^{3/2}}$$

$$\frac{dN^{\text{GLV}}}{d\omega} \sim \frac{1}{\omega^2}$$

Reproduction of the LPM and GLV regimes

$E = 100 \text{ TeV}$, $L = 4 \text{ fm}$, $T = 400 \text{ MeV}$

$m_q \rightarrow \infty$, $\Delta\varphi = (2P_Q \cdot k/E_Q)\Delta t$, Energy conservation



Double differential plot
in N_s and ω

Red line: $\langle N_s \rangle$ vs. ω

$$N_s \sim t_f \sim \sqrt{\omega}$$

Convolution of different
distributions

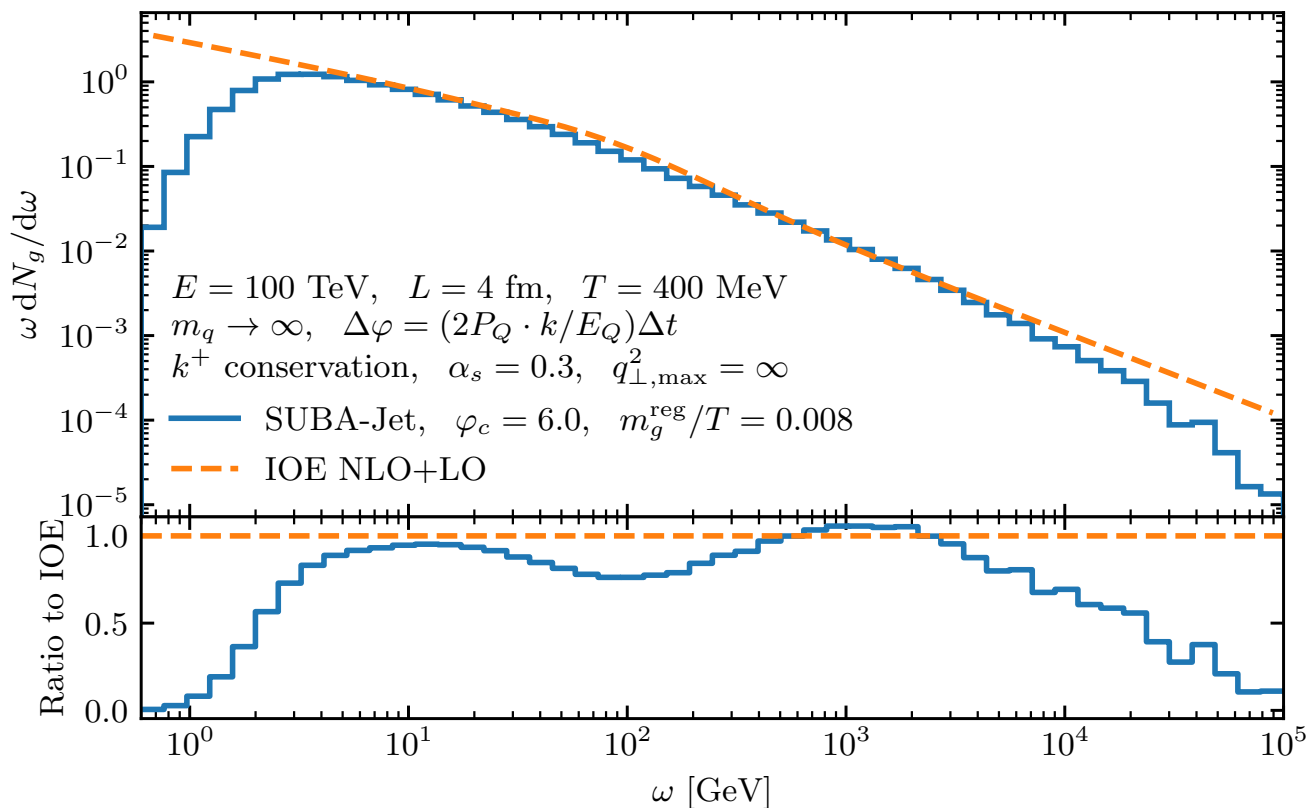
Reproduction of the IOE

Improved Opacity Expansion

arXiv:1910.02032 [hep-ph]

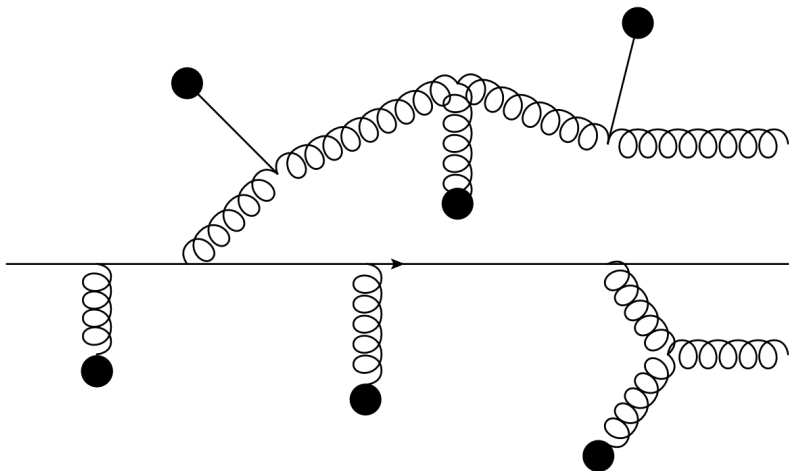
$$\frac{dN^{\text{IOE}}}{d\omega} = \frac{dN_{\text{LO}}^{\text{IOE}}}{d\omega} + \frac{dN_{\text{NLO}}^{\text{IOE}}}{d\omega}$$

$$\omega \frac{dN_{\text{NLO}}^{\text{IOE}}}{d\omega} \simeq \frac{1}{2} \frac{\alpha_s C_R}{\pi} \hat{q}_0 \text{Re} \int_0^L ds \frac{1}{k^2(s)} \left[\ln \frac{k^2(s)}{Q^2} + \gamma_E \right]$$



The Role of the Phase Accumulation

Choice of phase accumulation
of the preformed (trial) gluons:



- **More general formula:**

$$\Delta\varphi = \frac{2P_Q \cdot k}{E_Q} \Delta t$$

- **What is used in JEWEL:**

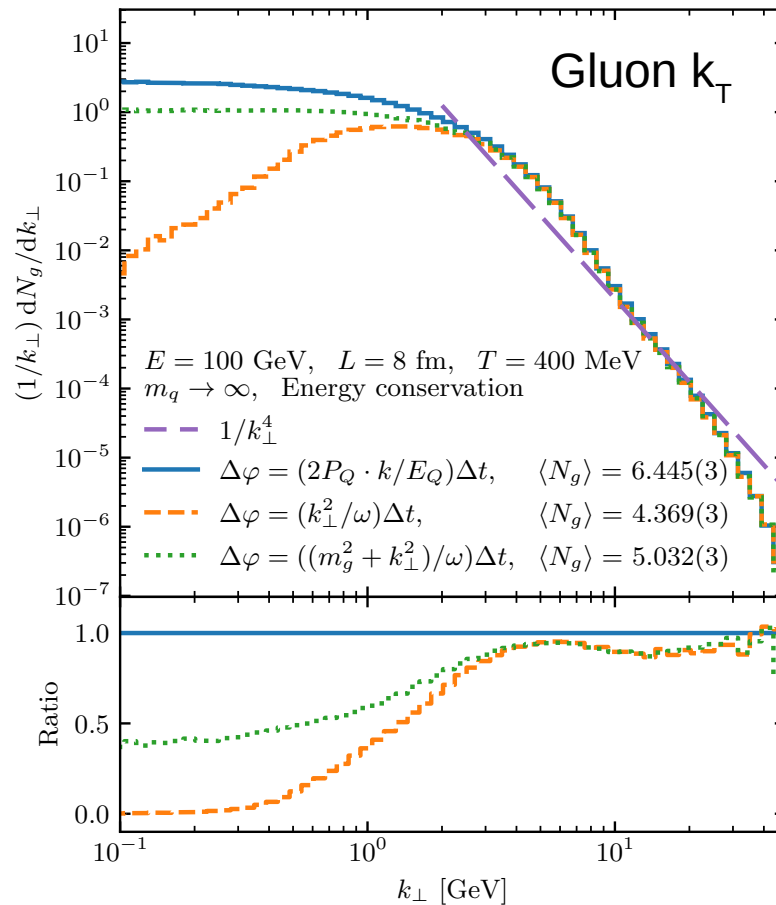
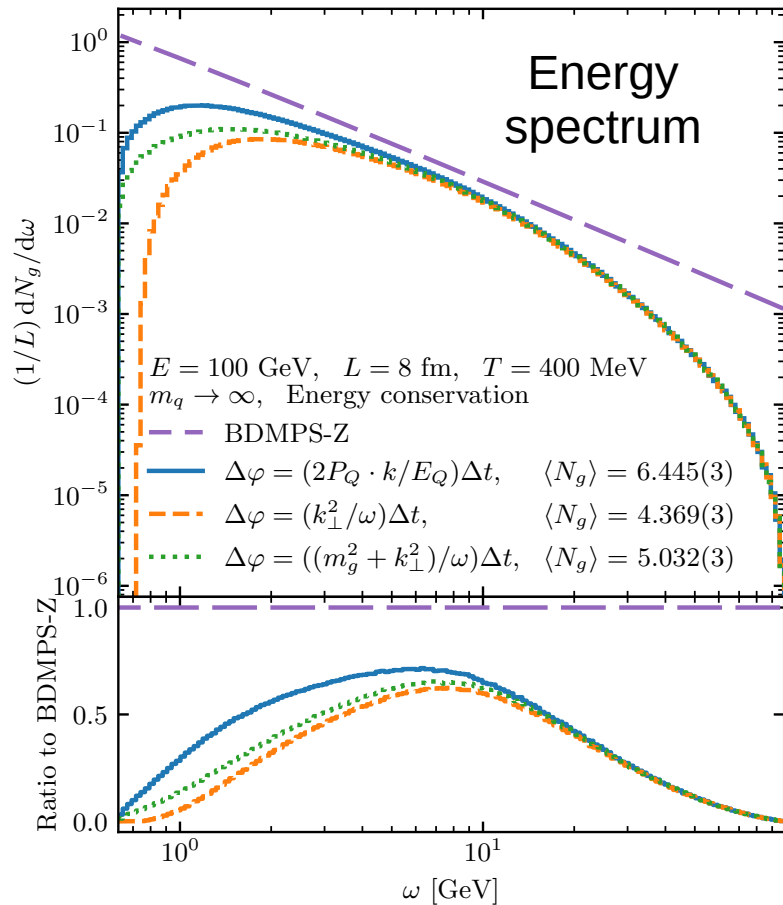
$$\Delta\varphi = \frac{k_T^2}{\omega} \Delta t$$

- **Including thermal gluon mass:**

$$\Delta\varphi = \frac{m_g^2 + k_T^2}{\omega} \Delta t$$

The Role of the Phase Accumulation

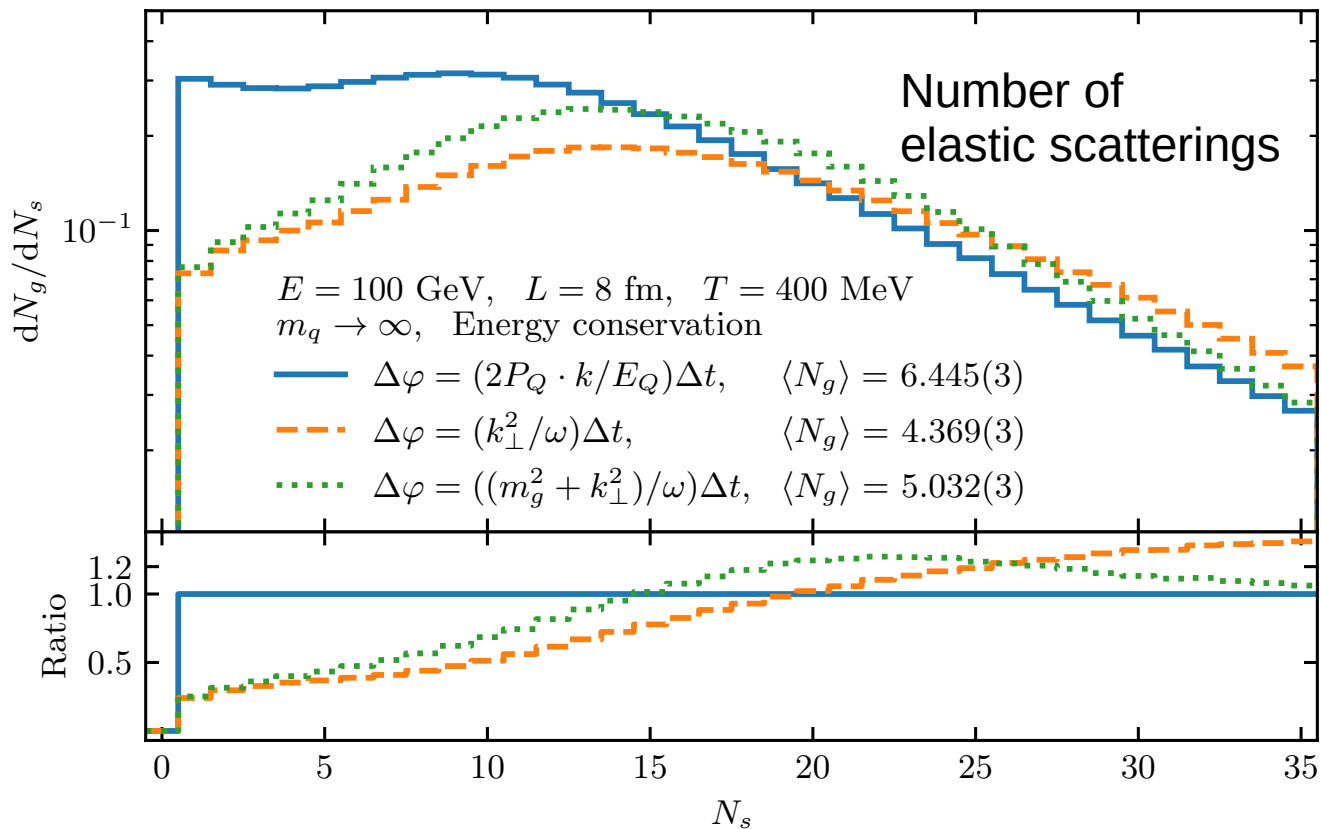
Effects at low energy & low k_T



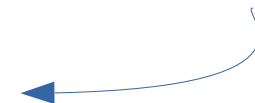
Number of radiated gluons per jet $\sim 5 - 6$

The Role of the Phase Accumulation

Effects at low N_s

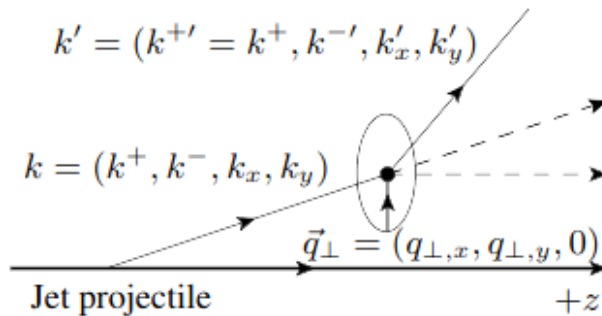


When neglecting the gluon mass in the phase accumulation, a larger path length is required to have a comparable overall number of radiations

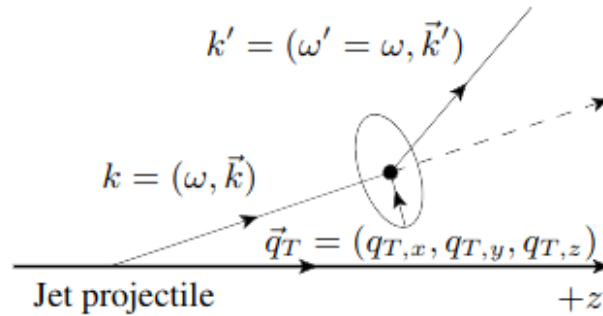


The Role of the Elastic Scatterings

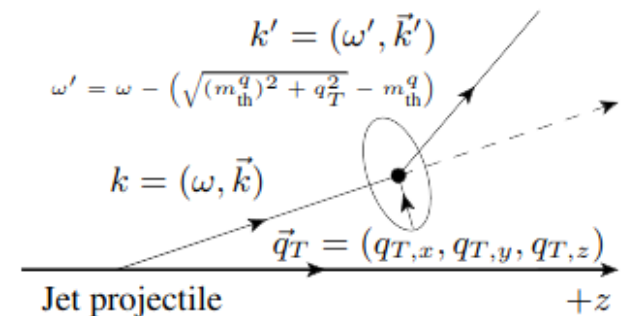
Choice of prescription in elastic scatterings:



k^+ conservation

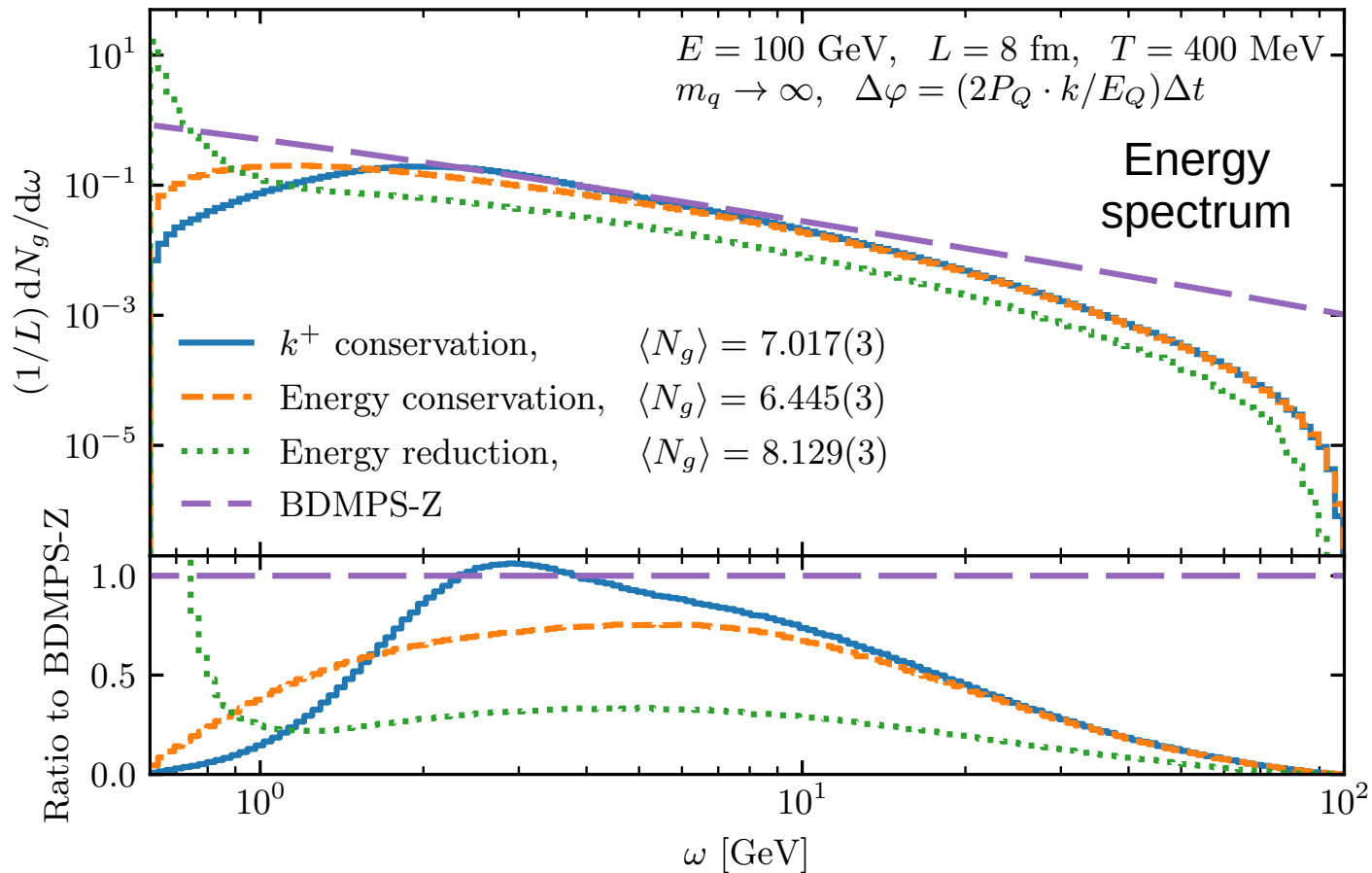


Energy conservation



Energy reduction

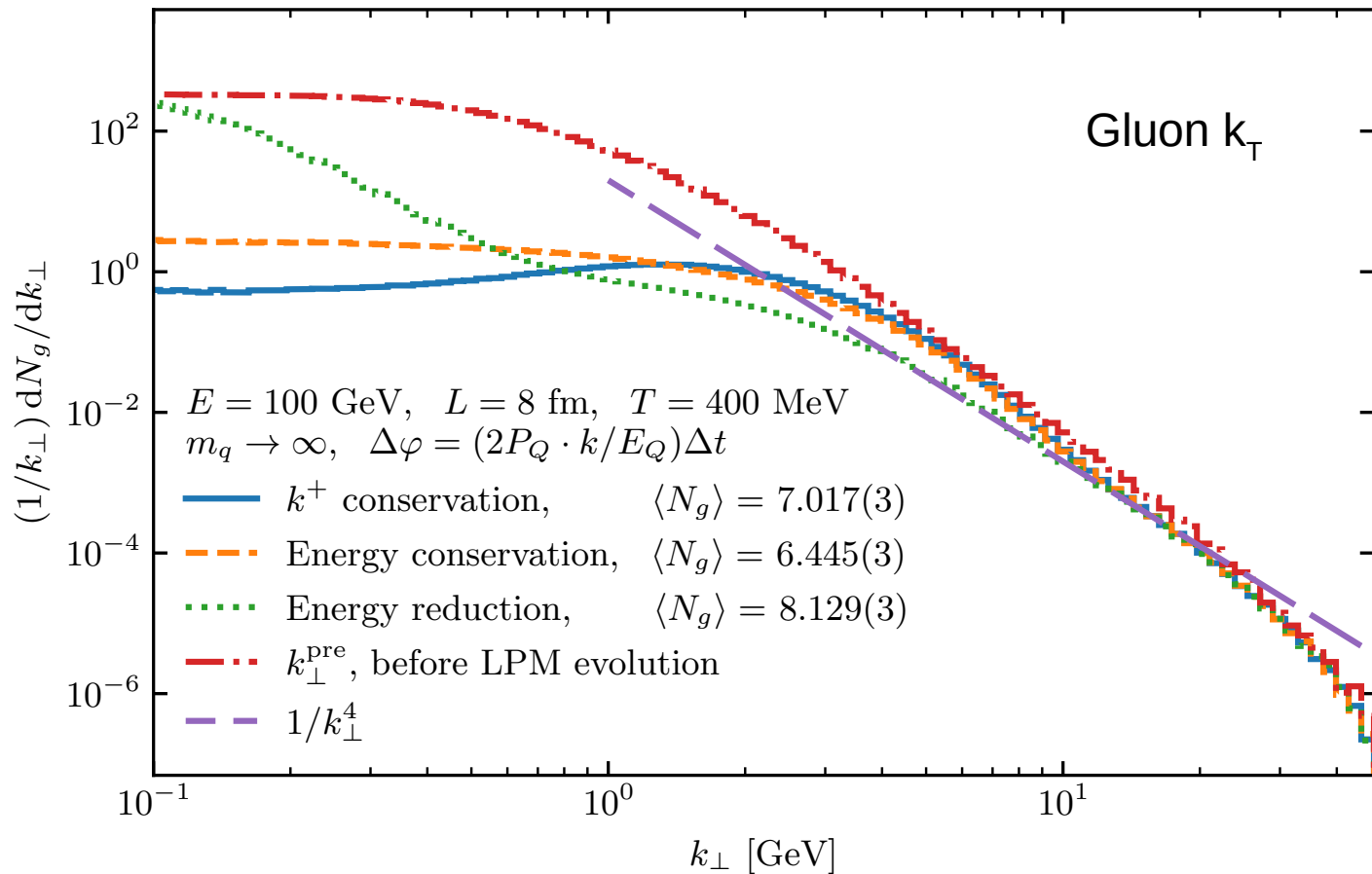
The Role of the Elastic Scatterings



Same BDMS behaviour at intermediate energies

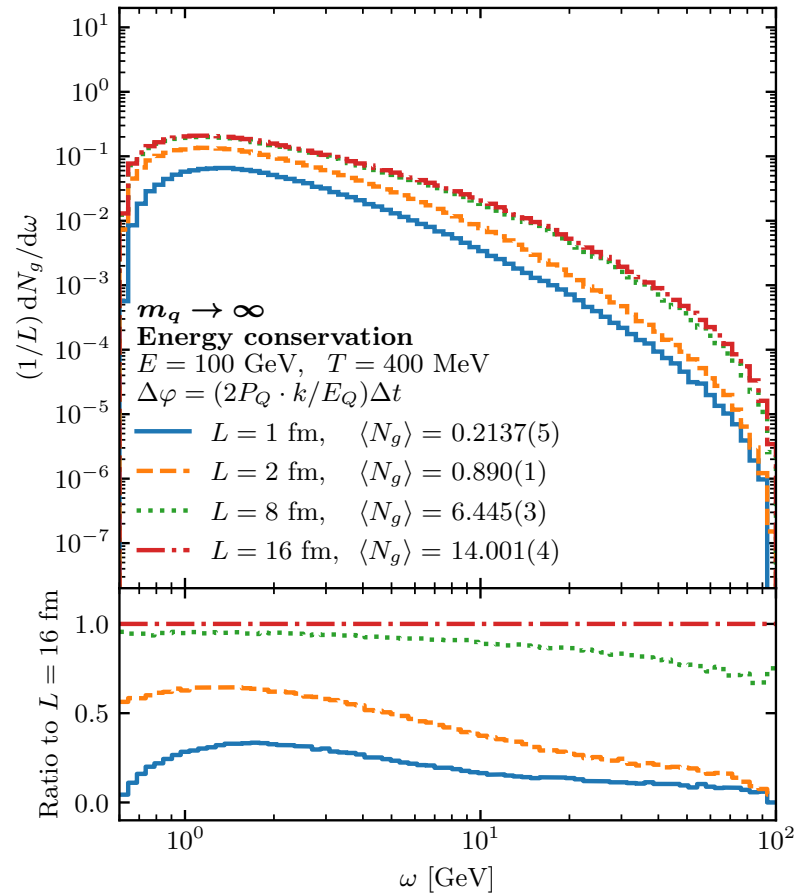
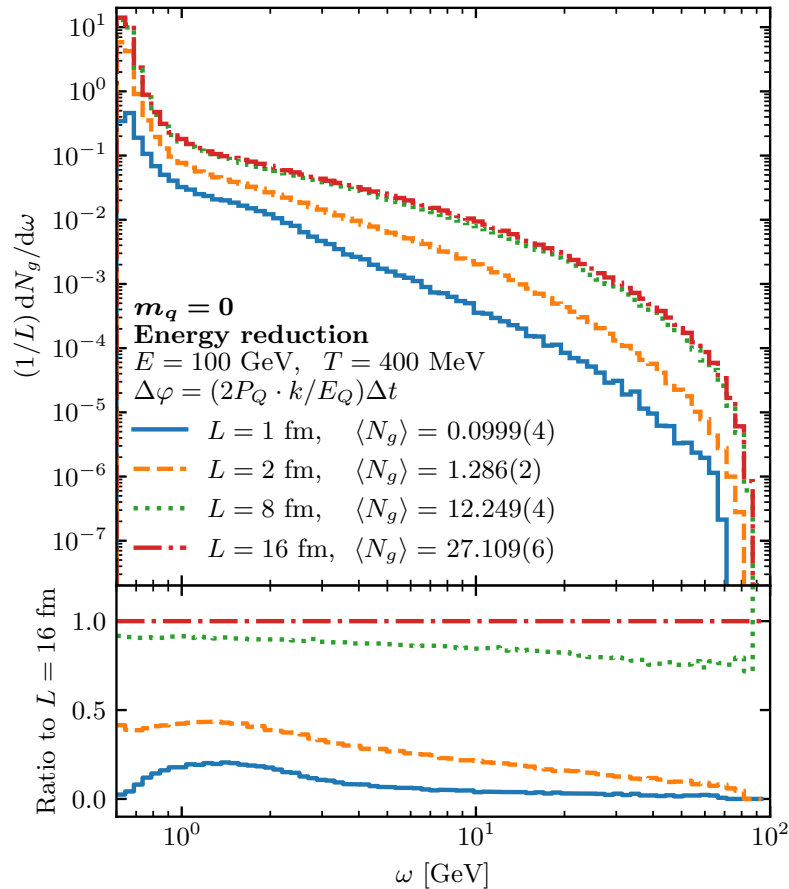
Difference at small energies

The Role of the Elastic Scatterings



Large difference at small k_{\perp}

The Role of the Path Length



$$\frac{dN}{d\omega} \stackrel{L \rightarrow \infty}{\approx} L$$

Looking Forward: Towards More Realism

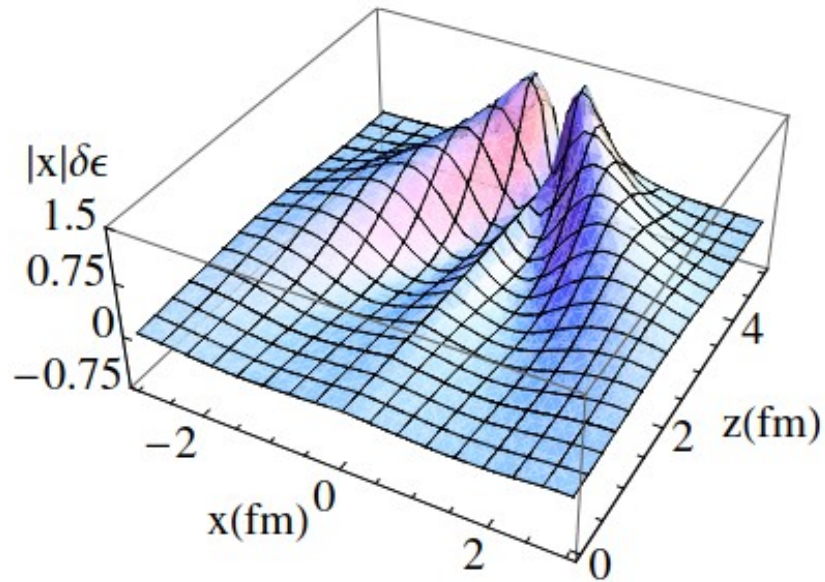
Next step:

- Implementation in two different MC frameworks:
 - SUBA-Jet + EPOS4
 - SUBA-Jet + Pythia 8
- Realistic QGP evolution
- Pre-equilibrium stage
- Hadronisation
- Hadronic phase



Looking Forward: Effect on the Medium

The jet also affects the medium



'Wake wave'
in the medium
due to the jet



G.-Y. Qin, A. Majumder, H. Song, U. Heinz
0903.2255 [nucl-th]

Summary

- We have presented a new model for jet energy loss in heavy ion collisions
- Implementation in a Monte Carlo framework
- **First step done:**
 - Reproduction of the BDMS radiation energy spectrum
 - Shown effects of different model assumptions
- **Next step:** Implementation within the new EPOS4
 - **EPOS4+JETS** – Initial state, hydro, and hadronisation from EPOS4

Thank you for your attention!

