Cell Decomposition from L^2 -Delaunay Triangulations?

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 Idea: Translation surfaces with the same gluing datum of the triangles belong to the same "cell".

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- Idea: Intersect this cell decomposition with the locus of translation surfaces.

 \rightarrow Conditions:

$$\prod_{\dots} \frac{\sin(\dots)}{\sin(\dots)} = 1$$