Dynamical generation of canonical spin potential in hot QCD

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In collaboration with A. Palermo

Based on: 2407.14345

What spin tensor should we use?

Interactions can make the choice.

The partition function of the finite temperature NJL model

$$\mathcal{L}_{\mathrm{NJL}} = \bar{q} \left(\overrightarrow{\frac{i}{2}} \overrightarrow{D} - \hat{m} \right) q + G_A \left(\bar{q} \gamma_{\mu} \gamma^5 q \right) \left(\bar{q} \gamma^{\mu} \gamma^5 q \right) + \cdots$$

with a mean field pseudo vector current f^{σ} generated by rotation and/or magnetic field



The partition function of non-dissipative spin hydrodynamics of free Dirac field with a canonical spin tensor

$$\mathbf{f}^{\sigma} = \frac{1}{2} \epsilon^{\sigma\mu\nu\rho} (\mathbf{v}_{\mu\nu} - \mathbf{S}_{\mu\nu}) n_{\rho}$$

το : Thermal vorticity

 $\mathfrak{S}_{\mu\nu}$: Canonical spin potential

Outline of talk

- Pseudo-gauge transformations and Spin hydrodynamics
- Analogy with the EM magnetization
- Proof of the result
- Discussion about the QGP

Spin tensor

The spin tensor is the "spin" part of the total angular momentum density operator

$$\widehat{\mathcal{J}}^{\lambda,\mu\nu} = x^{\mu}\widehat{T}^{\lambda\nu} - x^{\nu}\widehat{T}^{\lambda\mu} + \widehat{\mathcal{S}}^{\lambda,\mu\nu}$$

Infinite ways to define the spin tensor through pseudo-gauge transformations

$$\widehat{T}^{\prime\mu\nu} = \widehat{T}^{\mu\nu} + \frac{1}{2} \nabla_{\lambda} \left(\widehat{\Phi}^{\lambda,\mu\nu} - \widehat{\Phi}^{\mu,\lambda\nu} - \widehat{\Phi}^{\nu,\lambda\mu} \right),$$

$$\widehat{S}^{\prime\lambda,\mu\nu} = \widehat{S}^{\lambda,\mu\nu} - \widehat{\Phi}^{\lambda,\mu\nu}, \quad \widehat{\Phi}^{\lambda,\mu\nu} = -\widehat{\Phi}^{\lambda,\nu\mu}$$

The total conserved charges are unaffected but the densities of energy, momentum and angular momentum differ by quantum terms.

Examples (Dirac field):

The canoncial form is directly obtained from the Noether theorem

$$\widehat{\mathcal{S}}_{C}^{\lambda,\mu\nu} = \frac{1}{2} \bar{\psi} \left\{ \gamma^{\lambda}, \, \Sigma^{\mu\nu} \right\} \psi \quad \Sigma_{\mu\nu} = (i/4) [\gamma_{\mu}, \, \gamma_{\nu}]$$

It is dual to the axial current: $\widehat{\mathcal{S}}_{\mathrm{C}}^{\lambda,\mu
u}=\epsilon^{\lambda\mu
u
ho}\widehat{j}_{A\,
ho}$

• The Belinfante form has symmetric energy-momentum tensor and vanishing spin tensor $\widehat{\mathcal{S}}_{\scriptscriptstyle \mathrm{D}}^{\lambda,\mu\nu}=0$

Spin hydrodynamics

Spin hydrodynamics is necessary when the spin relaxation time scale is much longer than the time scale of e.g. kinetic equilibration

F. Becattini, W. Florkowski, E. Speranza, Phys. Lett. B 789 (2019) 419

Include the spin tensor in the hydro equations:

$$\partial_{\mu}T^{\mu\nu} = 0 \qquad \partial_{\lambda}\mathcal{S}^{\lambda,\mu\nu} = T^{\nu\mu} - T^{\mu\nu} \qquad \partial_{\mu}j^{\mu} = 0$$
$$T^{\mu\nu} = T^{\mu\nu}(\beta,\zeta,\mathfrak{S}) \qquad \mathcal{S}^{\lambda,\mu\nu} = \mathcal{S}^{\lambda,\mu\nu}(\beta,\zeta,\mathfrak{S}) \qquad j^{\mu} = j^{\mu}(\beta,\zeta,\mathfrak{S})$$

Spin potential: 6

Many recent developments

F. Becattini, S. Bhadury, J. Bhatt, A. Das, W. Florkowski, B. Friman, K. Fukushima, J.-H. Gao, C. Gale, K. Hattori, Y. Hidaka, M. Hongo, D. Hou, A. Huang, X.-G. Huang, A. Jaiswal, S. Jeon, M. Kaminski, A. Kumar, S. Li, Z.-T. Liang, J. Liao, Y.-C. Liu, K. Mameda, M. Matsuo, S. Pu, D. H. Rischke, R. Ryblewski, D. She, X.-L. Sheng, S. Shi, R. Singh, E. Speranza, M. Stephanov, H. Taya, Q. Wan, N. Weickgenannt, D.-L. Yang, H. U. Yee

 $|\omega(k)|$ = frequency scale fast modes Non-hydro regime $|\omega_{\rm sound}(k)|$ $|\omega_{\rm shear}(k)|$ $-|\omega_{\rm spin,\perp}(k)|$ $---- |\omega_{\text{spin},||}(k)|$ Spin hydro regime Γ_s Pure hydro regime k = wave number

Review: Becattini, Buzzegoli, Niida et al (2024)

Statistical operator for Spin hydrodynamics

The statistical operator is obtained by maximizing the entropy $S=-\mathrm{tr}\left[\widehat{
ho}\log\widehat{
ho}
ight]$ with the constraints of fixed energy-momentum and angular momentum-boost density

$$n_{\lambda} \operatorname{tr} \left[\widehat{\rho} \, \widehat{T}^{\lambda \nu} \right] = n_{\lambda} T^{\lambda \nu}$$

$$n_{\lambda} \operatorname{tr} \left[\widehat{\rho} \, \widehat{\mathcal{J}}^{\lambda, \mu \nu} \right] = n_{\lambda} \mathcal{J}^{\lambda, \mu \nu} \Rightarrow n_{\lambda} \operatorname{tr} \left[\widehat{\rho} \, \widehat{\mathcal{S}}^{\lambda, \mu \nu} \right] = n_{\lambda} \mathcal{S}^{\lambda, \mu \nu}$$

General covariant local thermodynamic equilibrium density operator

$$\widehat{\rho} = \frac{1}{\mathcal{Z}} \exp \left\{ -\int_{\Sigma} d\Sigma \, n_{\lambda} \left[\widehat{T}^{\lambda\nu} \beta_{\nu} - \frac{1}{2} \mathfrak{S}_{\rho\sigma} \widehat{\mathcal{S}}^{\lambda,\rho\sigma} \right] \right\}$$

The density operator describing local thermal equilibrium is pseudo-gauge dependent

F. Becattini, W. Florkowski, and E. Speranza, Phys. Lett. B 789, 419 (2019)

W. Florkowski, A. Kumar, R. Ryblewski, Prog. Part. Nucl. Phys. 108 (2019) 103709

E. Speranza and N. Weickgenannt, Eur. Phys. J. A 57, 155 (2021)

Hydrodynamics is pseudo-gauge dependent

F. Becattini and L. Tinti, Phys. Rev. D 84, 025013 (2011) and Phys. Rev. D 87, 025029 (2013)

K. Fukushima and S. Pu, Phys. Lett. B 817, 136346 (2021)

A. Das, W. Florkowski, R. Ryblewski and R. Singh, Phys. Rev. D 103, L091502 (2021)

Pseudo-gauge dependence of Spin polarization

For instance, the relation between spin polarization and the properties of the fluid (thermal vorticity, thermal shear, etc) is pseudo-gauge dependent.

MB, PRC 105 (2022) 4, 044907

Belinfante

$$S_{\mathrm{B}}^{\mu}(k) \simeq S_{\varpi}^{\mu}(k) + S_{\xi}^{\mu}(k)$$

$$S_{\varpi}^{\mu}(k) = -\frac{1}{8m} \epsilon^{\mu\rho\sigma\tau} k_{\tau} \frac{\int_{\Sigma} d\Sigma \cdot k \, n_{F} (1 - n_{F}) \, \varpi_{\rho\sigma}}{\int_{\Sigma} d\Sigma \cdot k \, n_{F}}$$

$$S_{\xi}^{\mu}(k) = -\frac{1}{4m} \epsilon^{\mu\lambda\sigma\tau} \frac{k_{\tau}k^{\rho}}{\varepsilon_{k}} \frac{\int_{\Sigma} d\Sigma \cdot k \, n_{F} (1 - n_{F}) \, \hat{t}_{\lambda} \xi_{\rho\sigma}}{\int_{\Sigma} d\Sigma \cdot k \, n_{F}}$$

Canonical

$$S_{\mathrm{C}}^{\mu}(k) \simeq S_{\mathrm{B}}^{\mu}(k) + \Delta_{\Theta}^{\mathrm{C}} S^{\mu}(k)$$

$$\Delta_{\Theta}^{\mathrm{C}} S^{\mu}(k) = \frac{\epsilon^{\lambda \rho \sigma \tau} \hat{t}_{\lambda} (k^{\mu} k_{\tau} - \eta^{\mu} m^{2})}{m \varepsilon_{k}} \frac{\int_{\Sigma} \Sigma(x) \cdot k \, n_{\mathrm{F}} (1 - n_{\mathrm{F}}) \left(\varpi_{\rho \sigma} - \mathfrak{S}_{\rho \sigma}\right)}{\int_{\Sigma} \Sigma \cdot k \, n_{\mathrm{F}}}$$

Also obtained in Y. C. Liu, X. G. Huang, Sci. China Phys. Mech. Astron. 65 (2022)

Note that the difference has linear independent terms in momentum and it is impossible to reconcile the two descriptions with a redefinition of thermodynamic fields.

MB, PRC 105 (2022) 4, 044907

What spin tensor should we use?

EM Magnetization

Also the electric current has a pseudo-gauge symmetry

$$\widehat{j}^{\prime\mu} = \widehat{j}^{\mu} + \underbrace{\nabla_{\lambda}\widehat{\mathcal{M}}^{\lambda\mu}}_{\text{bound current}}$$
, Magnetization: $\widehat{\mathcal{M}}^{\lambda\mu} = -\widehat{\mathcal{M}}^{\mu\lambda}$

Electric current definitions

- Fundamental: minimally coupled to gauge field
- Effective: one splits the bound and free currents to describe magnetized systems

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Electric current definitions

- Fundamental: minimally coupled to gauge field
- Effective: one splits the bound and free currents to describe magnetized systems

The magnetization tensor can also be induced by interactions. Textbook example: Long range Ising model

$$\widehat{H} = -\frac{J}{2N} \sum_{i,j} S_i S_j \longrightarrow \widehat{\rho} = \sqrt{\frac{N\beta J}{2\pi}} \int_{-\infty}^{\infty} d\mu \exp\left[-\frac{N\beta J}{2}\mu^2 + \beta J\mu \widehat{M}\right]$$

After an Hubbard-Stratonovich transformation

The following magnetization $\widehat{M} = \sum S_i$

$$\widehat{M} = \sum_{i} S_i$$

Fundamental definition of the spin tensor

In conventional gravitational physics the spin d.o.f. are not included: the spin connection is enslaved to the metric and the energy momentum tensor is symmetric.

In the Einstein-Cartan theory space-times with torsion are considered instead. This allows to define a spin tensor from the action varying the spin connection:

E. Speranza, N. Weickgenannt, Eur. Phys. J. A (2021) M. Hongo, X.-G. Huang, M. Kaminski, M. Stephanov, H.-U. Yee, JHEP 11 (2021) A. D. Gallegos, U. Gürsoy, and A. Yarom, SciPost Phys. 11, 041 (2021) S. Floerchinger and E. Grossi, Phys. Rev. D 105, 085015 (2022)

$$\delta S = \int d^4x |e| \left(T^{\mu}_{\ a} \delta e^{a}_{\ \mu} + \frac{1}{2} S^{\lambda}_{\ ab} \delta \omega_{\lambda}^{\ ab} \right)$$

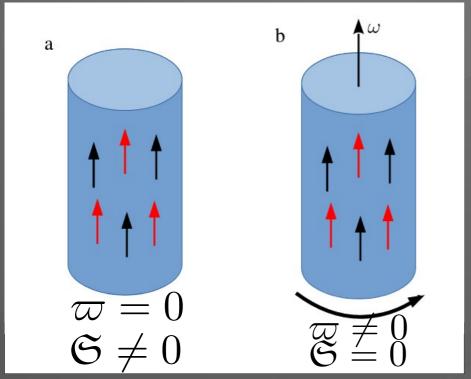
The canonical spin tensor is obtained in a minimal coupling with gravity.

Effective definition of the spin tensor

The spin potential emerges when imposing the constraint on the angular momentum of the system

$$n_{\lambda} \operatorname{tr} \left[\widehat{\rho} \widehat{\mathcal{S}}^{\lambda,\mu\nu} \right] = n_{\lambda} \mathcal{S}^{\lambda,\mu\nu}$$

Effective definition: choose the spin tensor that fits the phenomenological description of the system.



- a) Spin polarization and no rotation Impossible to describe with Belinfante (No spin tensor)
- b) Spin polarization and rotation Possible with Belinfante

Effective definition of the spin tensor

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Effective definition: choose the spin tensor that fits the phenomenological description of the system.

Phenomenological Landau theory

The landau function is a free energy obtained constraining the magnetization.

$$e^{-\beta L\{M_{\Lambda}(\boldsymbol{x})\}} = \operatorname{tr} \left\{ e^{-\beta H\{S_i\}} \delta \left[\sum_{i \in \boldsymbol{x}} S_i - M_{\Lambda}(\boldsymbol{x}) \right] \right\}$$

Also spin hydrodynamics free energy is obtained constraining the spin tensor.

Can interactions select the form of the spin tensor?

(similar to the Ising model)

Partition function in <u>Canonical</u> ideal spin hydrodynamics

$$\widehat{\rho} = \frac{1}{\mathcal{Z}} \exp \left\{ -\int_{\Sigma} d\Sigma \, n_{\lambda} \left[\widehat{T}_{B}^{\lambda\nu} \beta_{\nu} + \frac{1}{2} (\varpi - \mathfrak{S})_{\rho\sigma} \widehat{\mathcal{S}}_{\mathbf{C}}^{\lambda,\rho\sigma} \right] \right\}$$

The partition function of local thermal equilibrium is obtained as a path integral in a auxiliary curved space-time constructed with the thermodynamic fields

T. Hayata, Y. Hidaka, T. Noumi and M. Hongo, PRD 92 (2015) M. Hongo, Annals Phys. 383 (2017)

 \tilde{x} : new thermal coordinates Using imaginary time (Euclidean):

$$\mathcal{Z} = \int \mathcal{D}\psi \mathcal{D}\bar{\psi} e^{-S_E - S_{\mathfrak{S}}}, \quad S_E = \int_0^{|\beta|} d\tau d^3 \tilde{x} \sqrt{\tilde{g}_E} \left[\bar{\psi} \left(\frac{\overrightarrow{\mathcal{D}} - \overleftarrow{\mathcal{D}}}{2} + m \right) \psi + V(x) \right]$$

$$\overrightarrow{D}_{\tilde{0}} = \partial_{\tilde{0}} + (1/2) \varpi_{\tilde{0}}^{ab} \Sigma_{ab}, \quad \overleftarrow{D}_{\tilde{0}} = \partial_{\tilde{0}} - (1/2) \varpi_{\tilde{0}}^{ab} \Sigma_{ab}, \quad \overrightarrow{D}_{\tilde{i}} = \overleftarrow{D}_{\tilde{i}} = \partial_{\tilde{i}}$$

The spin connection $arpi_{ ilde{\lambda}}^{\ ab}$ is linked to the thermal vorticity: $arpi_{ ilde{0} ilde{i} ilde{j}}=-rac{1}{2|eta|}\left(\partial_{ ilde{i}}eta_{ ilde{j}}-\partial_{ ilde{j}}eta_{ ilde{i}}
ight)$

$$S_{\mathfrak{S}} = \frac{1}{2} \int_{0}^{|eta|} \mathrm{d} au \mathrm{d}^{3} \tilde{\boldsymbol{x}} \sqrt{\tilde{g}_{E}} \; n_{\tilde{\lambda}} (\varpi_{\tilde{
ho}\tilde{\sigma}} - \mathfrak{S}_{\tilde{
ho}\tilde{\sigma}}) \widehat{\mathcal{S}}_{\mathrm{C}}^{\tilde{\lambda},\tilde{
ho}\tilde{\sigma}}$$

Spin potential action

Geometrical interpretation

$$\mathbf{S}_{\mathbf{\mathfrak{S}}} = \frac{1}{2} \int_{0}^{|\beta|} d\tau d^{3} \tilde{\mathbf{x}} \sqrt{\tilde{g}_{E}} \, \bar{\psi} \left[e_{a}^{\tilde{\mu}} \gamma^{a} \, \vec{\mathfrak{s}}_{\tilde{\mu}}^{\rightarrow} - \vec{\mathfrak{s}}_{\tilde{\mu}}^{\alpha} e_{a}^{\tilde{\mu}} \gamma^{a} \right] \psi$$

$$\vec{\mathfrak{s}}_{\tilde{\mu}} = \frac{1}{2} \omega_{\tilde{\mu}ab} \Sigma^{ab}$$

$$\omega_{\tilde{\lambda}}^{bc} = \frac{1}{2} e_{\tilde{\mu}}^{b} e_{\tilde{\nu}}^{c} n_{\tilde{\lambda}} (\varpi^{\tilde{\mu}\tilde{\nu}} - \mathfrak{S}^{\tilde{\mu}\tilde{\nu}})$$

The spin potential can be included as a contribution to spin connection that is independent of the metric, i.e. like a space-time with torsion

$$D_{\tilde{\mu}} \to D_{\tilde{\mu}} + \mathfrak{s}_{\tilde{\mu}} \qquad \omega' = \varpi + (\varpi - \mathfrak{S}) = 2\varpi - \mathfrak{S}$$

A fundamental (proper) definition of the canonical spin tensor is the minimal coupling with torsion!

At global equilibrium the spin potential is equal to the thermal vorticity, thus no extra terms at global equilibrium.

Spin potential action

Geometrical interpretation

$$\mathbf{S}_{\mathfrak{S}} = \frac{1}{2} \int_{0}^{|\beta|} d\tau d^{3} \tilde{\mathbf{x}} \sqrt{\tilde{g}_{E}} \, \bar{\psi} \left[e_{a}^{\tilde{\mu}} \gamma^{a} \, \vec{\mathfrak{s}}_{\tilde{\mu}}^{-} - \vec{\mathfrak{s}}_{\tilde{\mu}}^{-} e_{a}^{\tilde{\mu}} \gamma^{a} \right] \psi$$

$$\vec{\mathfrak{s}}_{\tilde{\mu}} = \frac{1}{2} \omega_{\tilde{\mu}ab} \Sigma^{ab}$$

$$\omega_{\tilde{\lambda}}^{bc} = \frac{1}{2} e_{\tilde{\mu}}^{b} e_{\tilde{\nu}}^{c} n_{\tilde{\lambda}} (\varpi^{\tilde{\mu}\tilde{\nu}} - \mathfrak{S}^{\tilde{\mu}\tilde{\nu}})$$

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The Canonical spin tensor is dual to the axial current

$$S_{\mathfrak{S}} = -\int_{0}^{|eta|} \mathrm{d} au \mathrm{d}^{3} ilde{x}\sqrt{ ilde{g}_{E}}\;j_{A}^{ ilde{\mu}}f_{ ilde{\mu}}$$

where

$$\mathbf{f}^{\tilde{\boldsymbol{\sigma}}} \equiv \frac{1}{2} \epsilon^{\tilde{\sigma}\tilde{\mu}\tilde{\nu}\tilde{\rho}} (\varpi_{\tilde{\mu}\tilde{\nu}} - \mathfrak{S}_{\tilde{\mu}\tilde{\nu}}) n_{\tilde{\rho}}$$

Partition function of thermal NJL model

We start from the zero temperature NJL model, including spin-spin interactions

$$\mathcal{L}_{\mathrm{NJL}} = \bar{q} \left(\frac{i}{2} \overleftrightarrow{\partial} - \hat{m} \right) q + \mathbf{G}_{A} \left(\bar{q} \gamma_{\mu} \gamma^{5} q \right) \left(\bar{q} \gamma^{\mu} \gamma^{5} q \right) + \cdots$$

At **global equilibrium with thermal vorticity** the partition function is written as an Euclidean path integral in the emergent thermal space-time

$$\mathcal{Z}_{\text{NJL}} = \int \mathcal{D}q \mathcal{D}\bar{q} \, e^{-S_{\text{NJL}}[q,\,\bar{q};\,e_a^{\tilde{\mu}}]} = \int \mathcal{D}q \mathcal{D}\bar{q} \, \mathcal{D}f \, e^{-S_f[q,\,\bar{q},\,f_{\tilde{\mu}};\,e_a^{\tilde{\mu}}]}$$

Hubbard-Stratonovich transformation

$$S_f = \int_0^{|\beta|} d au \int d^3 \tilde{x} \, \sqrt{\tilde{g}_E} \, \left[\mathcal{L}_0 + \frac{1}{4G_A} f_{\tilde{\mu}} f^{\tilde{\mu}} - j_{\mathbf{A}\tilde{\sigma}} f^{\tilde{\sigma}} \right]$$

The resulting partition function from the pseudo-axial field f is equivalent to the partition function of spin hydrodynamics in the mean field limit identifying

$$f^{\sigma} = \frac{1}{2} \epsilon^{\sigma\mu\nu\rho} (\mathbf{w}_{\mu\nu} - \mathbf{S}_{\mu\nu}) n_{\rho}$$

Mean pseudo-vector: CSE and AVE

Non-vanishing
$$f^{\sigma}$$
 = mean axial current $\langle \hat{j}^{\mu}_{\mathrm{A}} \rangle$ = mean canonical spin tensor $\langle \hat{\mathcal{S}}^{\lambda,\mu\nu}_{\mathrm{C}} \rangle = \epsilon^{\lambda\mu\nu\rho} \langle \hat{j}_{\mathrm{A}\,\rho} \rangle$

In order to have a non-vanishing mean pseudo vector f^{σ} we need something that provides:

- Rotational symmetry breaking
- Parity breaking

This can be done by the magnetic field B and the rotation Ω through the Chiral Separation Effect (CSE) and the Axial Vortial Effect (AVE)

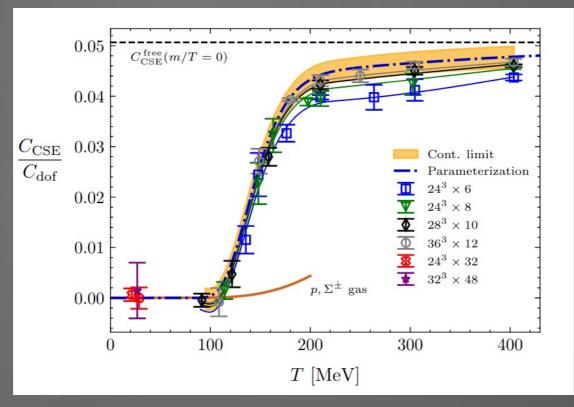
For a massless fermion:

$$\langle \widehat{m{j}}_{
m A}
angle = rac{\mu}{2\pi^2} m{B} + \left(rac{T^2}{6} + rac{\mu^2}{2\pi^2}
ight) m{\Omega}$$

See talk of Eduardo Garnacho Velasco on Thursday

In the chiral symmetric phase of hot QCD, lattice calculations at the physical point obtained a CSE conductivity approaches the one calculated for free massless

fermions.



B. B. Brandt, G. Endrodi, E. Garnacho-Velasco and G. Marko, JHEP 02 (2024), 142

We expect the same behavior for the AVE (with possible radiative corrections)

 $\begin{array}{cccc} \operatorname{Hot}\operatorname{QCD} & & & & \\ & + & & \\ B,\,\Omega & \operatorname{AVE,\,CSE} & & \end{array}$

Mean canonical spin tensor

Spin-Spin interactions

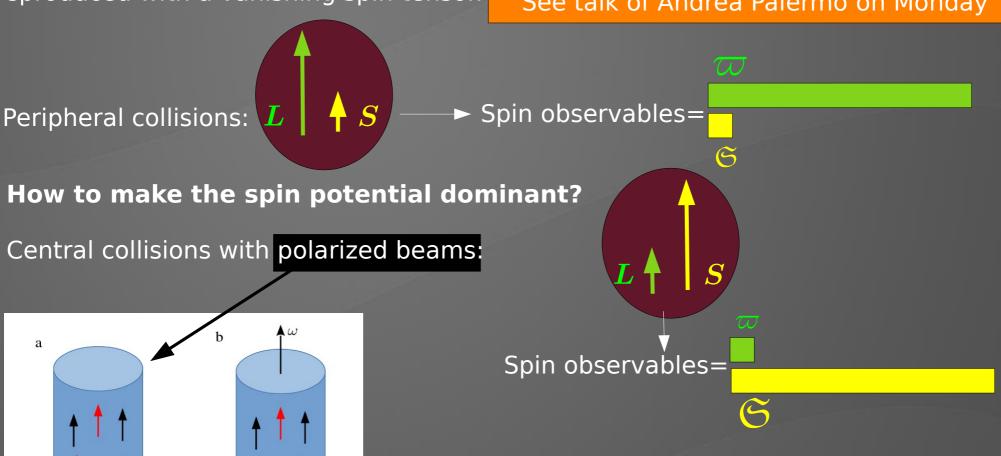
Spin fluid and canonical spin potential

Detecting the spin potential

Not strong indications of spin potential in heavy-ion collisions.

Most measurements are dominated by thermal vorticity and shear and can be reproduced with a vanishing spin tensor.

See talk of Andrea Palermo on Monday



Summary and outlook

- The spin tensor is a fundamental quantity to study out-of-equilibrium spin properties.
- Problem: pseudo-gauge symmetry allows many formulation of spin hydrodynamics with different physical predictions.
- Solution: a specific form of the spin tensor emerges from the microscopic description of spin-spin interactions.
- A rotating system with NJL interactions is described by the nondissipative spin hydrodynamic in the canonical pseudo-gauge.

$$Z|_{\mathrm{NJL}+\varpi} = Z|_{\mathrm{Spin hydro with canonical spin}}$$

- Indication that also the spin d.o.f. of hot QCD are described by a canonical spin tensor and spin potential: New direction to study spin properties of heavy-ion collisions
- Idea: dedicated experiments with polarized beams to make the spin potential stands out.

Thank you!